

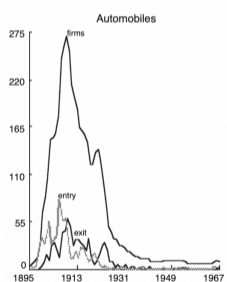
THE LIFE-CYCLE OF CONCENTRATED INDUSTRIES

Martin Beraja (Berkeley)

Francisco Buera (WashU)

MOTIVATION

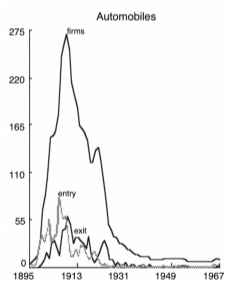
- ▶ Firms in cutting-edge industries often engage in *dynamic competition for the market*
- ▶ Many such industries have had a **life-cycle**: **Entry** → **Shakeout** → **Concentration**



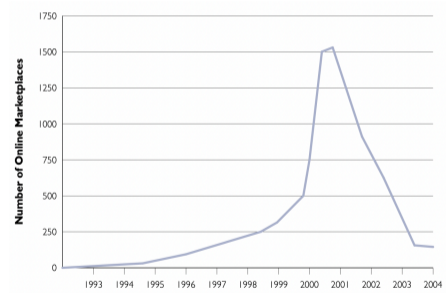
Source: Klepper and Simons (2005)

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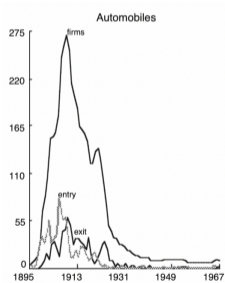
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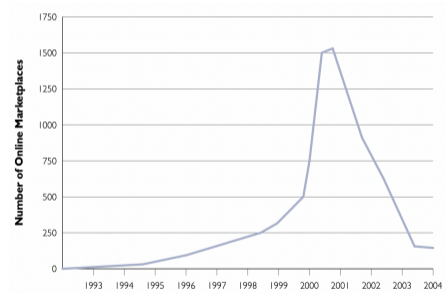
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- ▶ Also, OS or search engine industries. Windows or Google far ahead in a decade...

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Questions

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- ▶ How should **policies to promote competition** over the life-cycle differ?

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- ▶ How should **policies to promote competition** over the life-cycle differ?
 - ▶ **Common belief in policy circles:** for digital / AI industries, gov'ts should intervene preemptively and early on in the life-cycle, before concentration becomes “irreversible”

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2. **Application:** Digital and AI industries in the US (dataset from VentureScanner)

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Assumption 1: **Flow profit** function is:

- decreasing in \underline{N} and \bar{N} ,
- increasing in z ,
- converges to fixed cost $-f$ as $z \rightarrow 0$ and $\bar{N} \rightarrow \infty$, and
- such that at least one firm enters $\pi(1, 0; \underline{z}) + \lambda \pi(0, 1; \bar{z}) / r > 0$.

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Special case:

- Cost function: $\Gamma(q; z) = \frac{1}{z}q + f$
- Inverse demand function:

$$p_i = \frac{\sigma - 1}{\sigma} \left[\sum_{j=1}^{\underline{N}_t + \bar{N}_t} (q_j)^{\frac{\epsilon - 1}{\epsilon}} \right]^{\frac{\epsilon}{\epsilon - 1} \frac{\sigma - 1}{\sigma} - 1} (q_i)^{-\frac{1}{\epsilon}}$$

- Cournot competition in q

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Special case:

$U = Q_t + X_t$, with quantity Q_t and outside good X_t ,

$$\text{and } Q_t = \left[\sum_{i=1}^{\underline{N}_t + \bar{N}_t} (q_{it})^{\frac{\epsilon-1}{\epsilon}} \right]^{\frac{\epsilon}{\epsilon-1}} \frac{\sigma-1}{\sigma}$$

Solve backward (recursively) for value functions and exit/entry policies

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► A long-run concentrated industry equilibrium $(0, \bar{N}_\infty^{LF})$ is given by \bar{N}_∞^{LF} :

1. **Large** firms don't exit in the long-run $\iff J(0, \bar{N}_\infty^{LF}; \bar{z}) = \frac{\pi(0, \bar{N}_\infty^{LF}; \bar{z})}{r} \geq 0$,

2. **Small** firms don't enter in the long-run $\iff J(1, \bar{N}_\infty^{LF}; \bar{z}) = \frac{\pi(1, \bar{N}_\infty^{LF}; \bar{z}) + \lambda \times J(0, \bar{N}_\infty^{LF} + 1; \bar{z})}{r + \lambda} < 0$,

3. **Small** firms enter before $\iff J(1, \bar{N}_\infty^{LF} - 1; \bar{z}) = \frac{\pi(1, \bar{N}_\infty^{LF} - 1; \bar{z}) + \lambda \times J(0, \bar{N}_\infty^{LF}; \bar{z})}{r + \lambda} \geq 0$.

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Lemma 1. The equilibrium number of large firms \bar{N}_∞^{LF} in a concentrated industry state $(0, \bar{N}_\infty^{LF})$ is uniquely determined by (1)-(3).

Intuition: profit functions decreasing in \bar{N} , and hence so is value function $J(1, \bar{N}; \bar{z})$

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 rJ(\underline{N}, \bar{N}; \underline{z}) = & \pi(\underline{N}, \bar{N}; \underline{z}) + \lambda \times (J(\underline{N} - 1, \bar{N} + 1; \bar{z}) - J(\underline{N}, \bar{N}; \underline{z})) \\
 & + \lambda \times (\underline{N} - 1) \times (J(\underline{N} - 1, \bar{N} + 1; \underline{z}) - J(\underline{N}, \bar{N}; \underline{z})) \\
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Let $\underline{N}^{\text{LF}}(\bar{N})$ be the max # of **small** firms that industry with \bar{N} **large** firms can sustain

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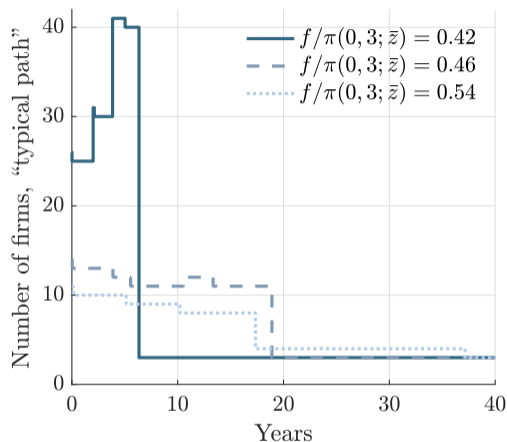
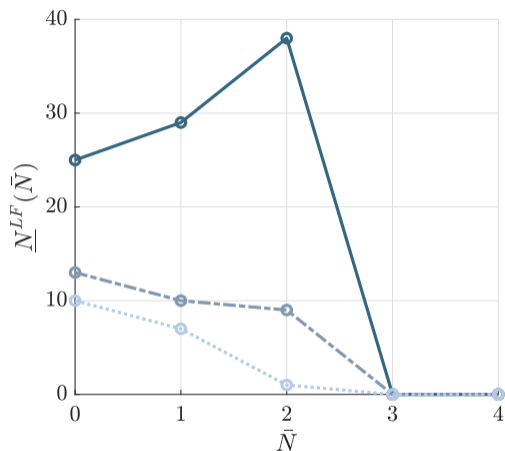
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ENTRY, SHAKEOUT, AND CONCENTRATION: A NUMERICAL ILLUSTRATION



► In a competitive industry, the life-cycle is monotonic. **Why the non-monotonicity?**

► Cost of delaying entry: more large firms present; e.g., $\pi(\underline{N}, 1; \underline{z}) - \pi(\underline{N}, 0; \underline{z}) < 0$

► Benefit: Large gains right before the shakeout; e.g., $\pi(0, 3; \bar{z}) - \pi(\underline{N}, 3; \bar{z}) > 0$

► Intuition

EQUILIBRIUM INDUSTRY LIFE-CYCLE: SCALE DIFFERENCES BETWEEN FIRMS

- ▶ **Relative scale** → nature of competition (static v. dynamic) and **optimal policy**
- ▶ **Scale economies** key driver of US concentration/markups (Autor et al, Philippon et al)
 - ▶ Particularly important in **digital/AI** industries (Goldfarb-Tucker)

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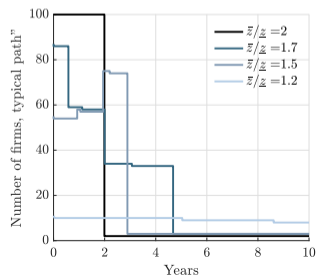
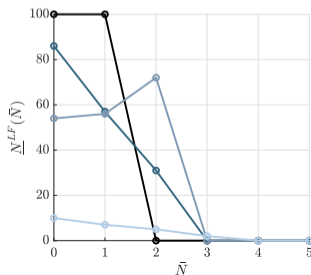
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 - ▶ That is, it cannot directly address quantity distortions due to imperfect competition
- ▶ Such interventions would implement a **first best** but are seldom used in practice
- ▶ Governments favor policies that **promote competition** via **firm entry** or **antitrust**
 - ▶ These are the type of policies currently being discussed for digital/AI industries (Khan, 2016; Philippon, 2019; Tirole, 2023; Varian, 2018)

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 - ▶ Capture policies that promote competition and firm entry in a **reduced form way**
 - ▶ Subsidies **early** in the life-cycle \implies Act before industries become too concentrated
Tax credits to startups / financing for small firms (Bloom et al., 2019; Itskhoki and Moll, 2019).
Laxer regulations on data privacy in digital industries (Goldfarb and Tucker, 2012)

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- ▶ **Goal**: analyze how **nature of competition** affects **optimal policy** over the life-cycle
 1. Are subsidies designed for promoting competition in static industries also appropriate for innovative industries where **dynamic competition for the market** is key?
 2. If not, how should subsidies over the life-cycle **differ**?

Theoretical results in two limit cases:

1. $\bar{z}/\underline{z} \rightarrow \infty$, with $\underline{z} \rightarrow 0$. Innovation leads to large scale diffs; competition for the market

2. $\bar{z}/\underline{z} = 1$. Small scale differences; static competition in the market

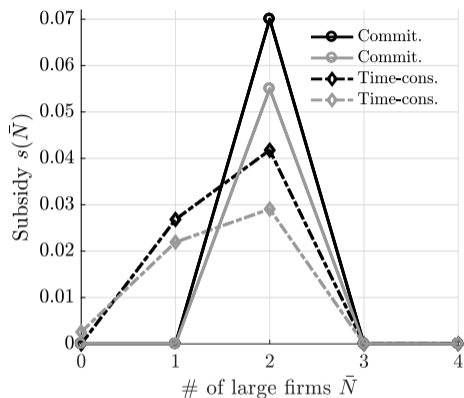
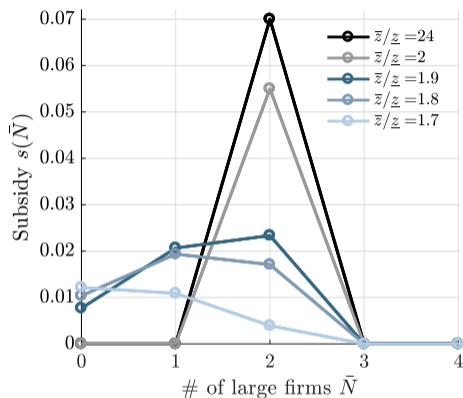
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 - ▶ The government must subsidize firms in a nascent industry too
 - ▶ Subsidies are uniform over the life-cycle

RELATIVE SCALE AND OPTIMAL POLICY



- ▶ Firm entry/exit mostly driven by option value of taking over the market
⇒ Governments can [wait to intervene](#) later in the life-cycle
- ▶ If the government cannot commit, the time-consistent policy must subsidize earlier

HOW DO THESE RESULTS HELP INFORM COMPETITION POLICY DEBATES?

Established belief in policy circles: innovative industries are “harder” to regulate

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 - ▶ Instead, gov't must **subsidize early on** when static competition in the market is important

1. Collusion and antitrust

$$\pi(\underline{N}, \bar{N}; \bar{z}) = \frac{1}{\bar{N}} \pi^{\text{Cartel}}(\underline{N}, \bar{N}; \bar{z})$$

2. Blocking competitors and antitrust

Large firms pay c to lower profits of small firms $\pi(\underline{N}, \bar{N}; \bar{z})$

3. Endogenous Rate of Innovation λ at cost $c(\lambda)$ ▶ numerical example

$$J(\underline{N}^{LF}(\bar{N} + 1), \bar{N} + 1; \bar{z}) - J(\underline{N}, \bar{N}; \bar{z}) = c'(\lambda(\underline{N}, \bar{N}))$$

4. Innovation spillovers from large firms $\lambda(\bar{N})$

APPLICATION: DIGITAL & AI INDUSTRIES IN THE US

The question of how to regulate an industry in practice can be understood as:

Are firm choices mostly driven by dynamic competition for the market?
Or, is competition in the market important too?

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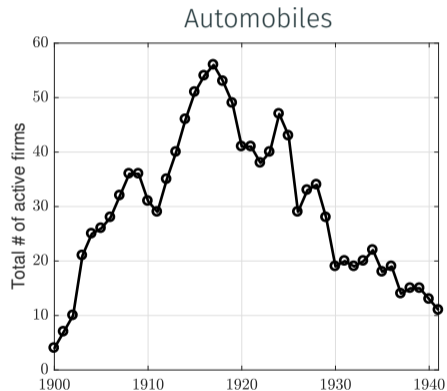
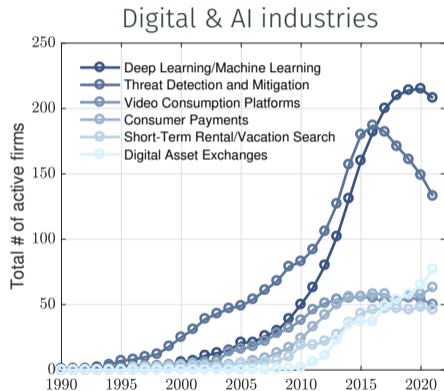
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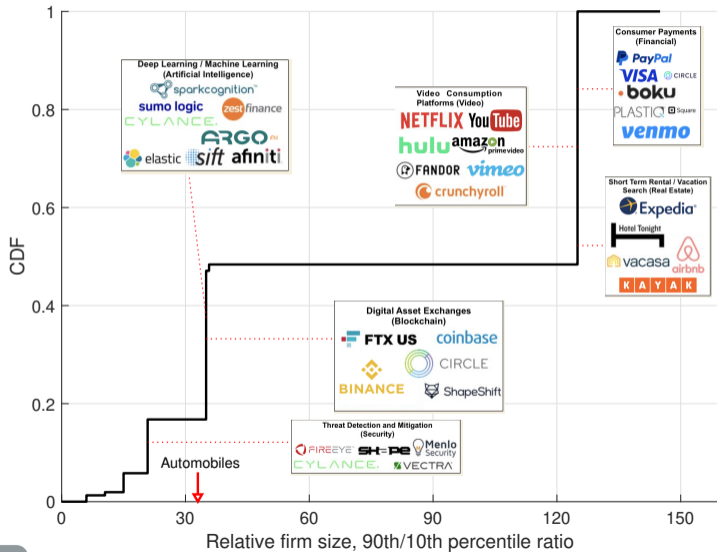
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As a comparison, look at Automobile industry using The 100 Year Almanac

LIFE-CYCLE ACROSS INDUSTRIES



RELATIVE SCALE ACROSS INDUSTRIES



► output-productivity model

INTUITION FOR NON-MONOTONIC LIFE-CYCLE

- ▶ In a **competitive** industry (Jovanovic-MacDonald), the life-cycle is **always monotonic**
No firms exit when quantities are low (price is high). A mass of firms exit once they are high (price is low)
- ▶ In an **oligopolistic** industry (our model), the life-cycle may be **non-monotonic**
- ▶ Incentives to **delay entry**, from $\bar{N} = 1 \rightarrow 2$, given \underline{N} :

$$J(\underline{N}, 2; \underline{z}) - J(\underline{N}, 1; \underline{z}) = \overbrace{\pi(\underline{N}, 2; \underline{z}) - \pi(\underline{N}, 1; \underline{z}) + \frac{\lambda}{r + \lambda \underline{N}} [\pi(\underline{N}, 3; \bar{z}) - \pi(\underline{N}, 2; \bar{z})]}^{\text{cost of competing with an additional large firm } < 0}$$
$$+ \underbrace{\frac{\lambda}{r + \lambda \underline{N}} [\pi(0, 3; \bar{z}) - \pi(\underline{N}, 3; \bar{z})]}_{\text{benefits of entering closer to the shakeout } > 0} .$$

- ▶ “Business stealing” gains at shakeout occur closer to the time of entry

SOURCES OF INEFFICIENCY

Constrained Planner's value of an additional firm (SB) v. Equilibrium value of staying (LF)

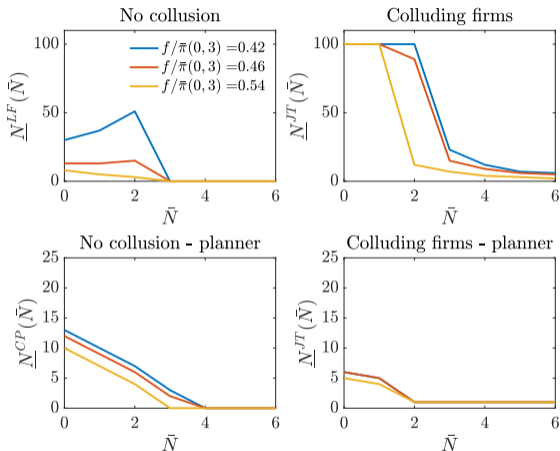
$$\text{SB: } U(\underline{N}, \bar{N}) - U(\underline{N} - 1, \bar{N}) + \lambda (V(\underline{N}(\bar{N} + 1), \bar{N} + 1) - V(\underline{N}, \bar{N}))$$

$$\text{LF: } \pi(\underline{N}, \bar{N}; \underline{z}) + \lambda J(\underline{N}(\bar{N} + 1), \bar{N} + 1; \bar{z}) + \eta(\bar{N})(\underline{N} - 1)J(\underline{N} - 1, \bar{N}; \underline{z})$$

1. **Source of inefficiency I:** Firms care about profits, not surplus $\Rightarrow \uparrow$ # firms
2. **Source of inefficiency II:** Firms do not internalize surplus destruction $\Rightarrow \downarrow$ # firms
3. **Source of inefficiency III:** War of attrition $\Rightarrow \downarrow$ # firms

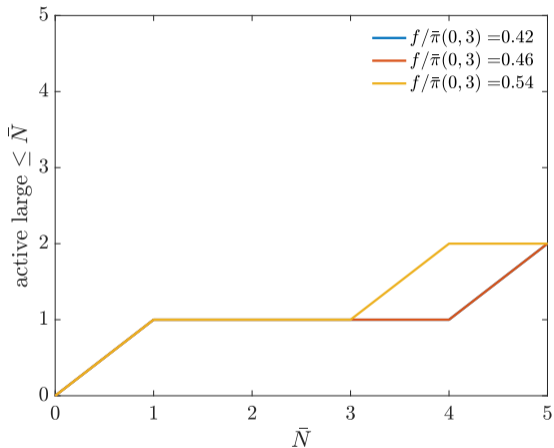
▶ [Jump back](#)

COLLUSION AND ANTITRUST



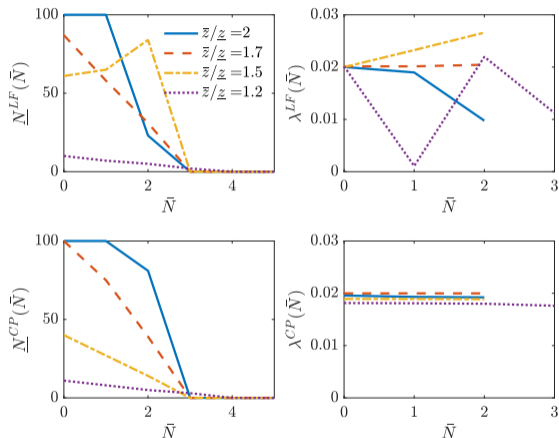
- ▶ More incentives to entry, to participate in the cartel
- ▶ Planner wants to break the cartel, or less entry if it can't

COLLUSION AND ANTITRUST, INNACTIVE PRODUCTIVE FIRMS



► The cartel may not operate all firms/goods

INTENSIVE MARGIN OF INNOVATION, λ ENDOGENOUS



- ▶ $c(\lambda) = c_0 \lambda^{1.1}$, c_0 calibrated so that $\lambda(\underline{N}(0), 0) = 0.02$
- ▶ Life cycle of entry and exit virtually unaffected

RELATIVE OUTPUT VS. RELATIVE PRODUCTIVITY, $\epsilon = 7.5$

