

# **Money in the Production Function**

## **Some Policy Implications**

**Edward C. Prescott**

**May 27, 2019**

**10<sup>th</sup> Annual CIGS Conference on  
Macroeconomic Theory and Policy**



# Microeconomic Science

---

- Microeconomics and Macroeconomics are different Sciences
- Microeconomics is a powerful science for addressing micro issues
- But in addressing macro problems it has failed spectacularly (Lucas and Sargent)

# Macroeconomic Science

---

- It is a unified hard quantitative science
- Conceptually it is simple
  - Smart undergraduates can master the basic concepts in a single course
  - Supply and demand are not used in this science
  - General equilibrium reasoning is used with agents on both sides of every transaction
  - All accounting identities must hold for the model economy being used to address the given question

- To answer the question: What is the aggregate consequences of some interest rate targeting regime?
- Until recently when the President of the Minneapolis Federal Reserve Bank asked me what the Fed should do, my answer was that economic theory does not provide an answer.
- Today I will report on a recent advance of macro theory that can be helpful to answer such questions.

# Motivation

---

- Technology is rapidly advancing in the information processing area
- This is changing the monetary/payment system
- A currency-less fiat monetary system is now feasible (Sweden)
- U.S. is moving in this direction

# History of Aggregate Monetary Theory

---

- Using the Stokey and Lucas (1981) framework, money was introduced into dynamic macroeconomics
- The finding was that with this household transaction framework monetary policy had virtually no consequences for real output and employment (Cooley and Hansen, 1989)

# History of Value

---

- The price of a good is in units of value
- Commodity value system
  - Value is in units of a commodity, e.g. ounces of gold/silver
  - Used in U.S. before 1933

- Fiat currency value system
  - Value is in units of currency, e.g. dollar, pound, etc.
  - Its use economizes on resources needed to acquire gold
  - Used in U.S. after 1933

**What is the unit of value in a currency-less system?**



# Fiat Value System

---

- Fiat value is a form of government debt
- Prices are in units of *fiat value*
- Name of units of value is unimportant

# Fiat Value System

---

- Use valuation equilibrium theory of Debreu (1954)
  - Commodity space is a linear topological space
  - “Value services” is a commodity
- Use sequence of valuation equilibria
  - This is the way statistics are collected (quarterly)

- Fiat value is the numeraire
  - GE theory prior to Debreu had finite number of goods and only *relative* values of commodities were determined
  - In fiat value system, prices are in units of fiat value

# Traditional and Commercial Banks

---

- Traditional Banks
  - Played important role in commodity value system
  - Fractional reserves reduced the amount of commodity used by the payment system

- Commercial Banks
  - Play important role in fiat currency value system
  - Accept demand deposits, originate loans, and have fractional reserves
  - But, managing assets is their major activity

# **Banks in a Fiat Value System**

---

**Proposal: totally separate transaction services from asset management services**

# Transaction Services

---

- Businesses hold large amounts of cash reserves
- Businesses hold over \$10 trillion in highly liquid assets that earn zero real return
- Services of these “cash reserves” are a factor of production
- Just like human capital and other capital services

# Asset Management

---

- Trusts that do not accept demand deposits
- They pool savings and make investments
- This is the way most lending to finance business is done
  - Checkable deposits only 0.08 **annual** GNP
  - Time and savings deposits only 0.57 GNP
  - Yet business borrowing is 2.5 GNP (*Flow of Funds L104, L105*)
- BlackRock alone manages 0.25 GNP of debt assets



# Key Features of System

---

- Fiat value is a form of government debt
- Prices are in units of fiat value
- Fiat value is a capital stock
- It is rented to the business sector

Note: Money is short for fiat value in what follows

**The Model Used to  
Explore How Such a  
System Would Operate**

# Aggregate Production Properties

---

- Want marginal product of money to be zero if money services input is large enough
- Want standard production function properties (McKenzie)
  - Constant returns to scale (CRS)
  - Concavity
  - Increasing
  - Differentiable
- An isoquant defines a production function, given CRS

# Technology

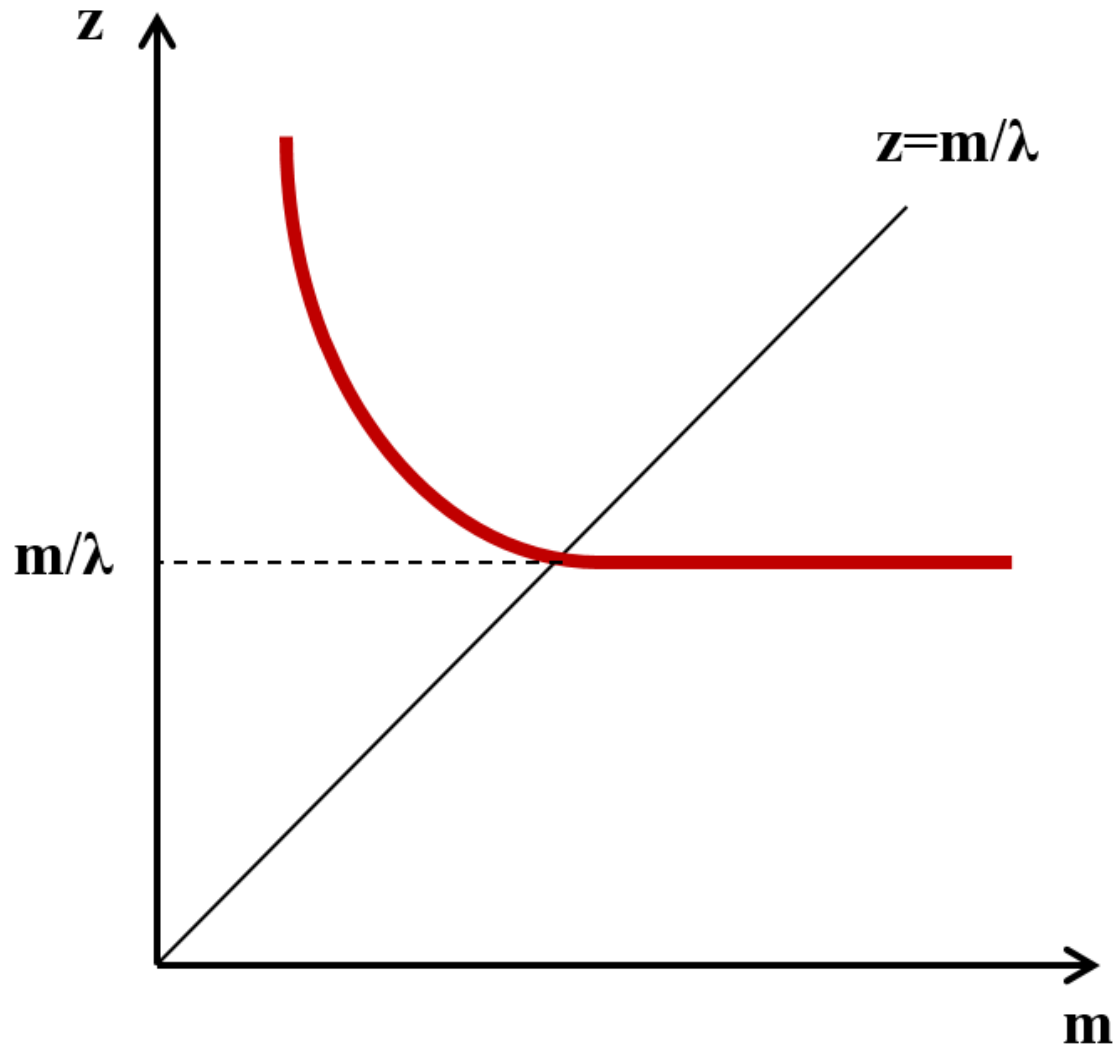
---

- $h$  labor,  $k$  capital services,  $m$  money services,  $y$  output,  $A$ ,  $\lambda$  and  $\theta$  parameters, and  $z_t = k_t^\theta h_t^{1-\theta}$
- CRS aggregate production function

$$y_t = f(m_t, z_t) = \begin{cases} A\lambda^{1-f} z_t & \text{if } m_t = \lambda z_t \\ Az_t^f m_t^{1-f} & \text{if } m_t < \lambda z_t \end{cases}$$

# A Production Function Isoquant

---



# Technology

---

- When  $m/z = \lambda$  , the marginal product of money is zero
- We term this “**satiation**”
- When satiation, the marginal product of money is zero

# Households and Their Preference Ordering

---

- Measure one of identical households
- Preferences ordered by

$$\sum_{t=0}^{\infty} (1 + \rho)^{-t} [\log c_t + \alpha \log(1 - h_t)]$$

- $h$  is the fraction of time allocated to the market

# Government Policy Variables

---

- Variables
  - $\pi$  : inflation rate
  - $\tau$  : labor tax rate
  - $g$  : gov't purchases of final product
  - $\psi$  : transfers to household
  - $m$  : stock of money
  - $b$  : stock of gov't bonds issued
  - $i_m$  : interest rate on money
  - $i_b$  : interest rate on gov't bonds



# Government

---

- Government pays interest on two types of debt:
  - $i_m$  : **nominal** interest paid on money
  - $i_b$  : **nominal** interest paid on bonds
  - Absent monetary satiation  $i_b$  is the bigger

## Note

- An equilibrium condition is  $r_m + i_m = i_b$
- When monetary satiation, the rental price of money services is zero and  $i_m = i_b$

# Budget Constraints

---

- All quantities are real
- All prices are **nominal**

# Budget Constraints

---

- Household budget constraint is

$$c + [k' - (1 - \delta)k] + [(1 + \pi)m' - m] + [(1 + \pi)b' - b] = (1 - \tau)wh + r_k k + r_m m + i_m m + i_b b + \psi$$

- HH consume and invest in capital, money, and bonds
- HH income from business sector (wage, capital rental, money rental) and from government (interest received on money and bonds, transfers)

# Budget Constraints

---

- Firm budget constraint is

$$y = wh + r_k k + r_m m$$

- Constant returns to scale so no economic profits in equilibrium

# Budget Identity

---

- Government budget identity is

$$g + \psi + i_m m + i_b b = \tau wh + [m'(1 + \pi) - m] + [b'(1 + \pi) - b]$$

- Gov't consumes, transfers to HH and pays interest on  $m$  and  $b$
- Gov't finances its expenditures from labor taxes, producing money (inflation tax), and new debt.

# Balanced Growth Analysis

---

- Dynasty and overlapping generations in our model economies are essentially equivalent
- We use dynasty because it simplifies the presentation
- In balanced growth, stocks are constant relative to output, so we will drop the prime on beginning of next period's stocks

# A Note on Government Financing

---

- In balance growth, the government budget constraint is

$$g + \psi + i_m m + i_b b = \tau wh + \pi m + \pi b$$

- Government revenue is from the labor tax and from the inflation “tax”
- Money production is a government monopoly

# Equilibrium

- Prices are  $\{w_t, r_{kt}, r_{mt}, i_{mt}, i_{bt}\}_{t=0}^{\infty}$
- Equilibrium conditions are
  - Given prices and budget constraint, **household** chooses its best  $\{c_t, h_t, k_{t+1}, m_{t+1}, b_{t+1}\}_{t=0}^{\infty}$
  - Given prices, **firm** chooses  $\{k_t, h_t, m_t\}$  that maximizes its value for every  $t$
  - The **government** selection of  $\{g_t, \psi_t, b_{t+1}, m_{t+1}, \pi_t, \tau_t\}_{t=0}^{\infty}$  are such that its budget identity is satisfied for all  $t$
- We study balanced growth only



# Baseline Economy

---

- We have specified a parametric set of economies
- We choose a set of parameters so that model matches selected U.S. National Income and Product Account data (following Larry Klein)
- Targets:
  - Consumption/investment shares
  - Fraction of time worked
  - Asset stocks to output ratios
  - Factor income shares

# Baseline Economy: *Parameters*

---

---

## Preference and Technology Parameters

$\alpha$	relative preference for leisure	0.68
$\beta$	discount rate (annual)	0.98
$\delta$	depreciation rate (annual)	0.04
$\theta$	capital cost share	0.35
$\varphi$	money cost share	0.01
$A$	TFP	1.13
$\lambda$	money satiation parameter	2

---

# Baseline Economy: *Parameters*

---

## Policy Parameters

$g / y$	gov't public goods share	0.05
$\psi / y$	transfer share	0.25
$m / y$	money output ratio	1.50
$b / y$	gov't privately held debt to output	0.50
$\tau$	labor tax rate	0.52
$i_m$	interest rate on money	6.54%
$i_b$	interest rate on gov't bonds	7.21%
$\pi$	inflation rate (annual %)	2.00%

---

# Baseline Economy: *National Accts*

---

- This theory necessitates a change in how National Accounts are constructed

# National Accounts

---

**Product** **1.08**

HH Consumption 0.68

Gov't C & Invest. 0.05

HH Invest. in k 0.27

Money Production 0.08

**Income** **1.08**

Wages 0.64

Depreciation of Capital 0.15

Capital Rental Income 0.19

Money Rental Income 0.01

Central Bank Profits 0.08

# Government Accounts

---

**Receipts** **0.44**

Tax Revenue 0.33

Money Issuance 0.08

Debt Issuance 0.03

**Expenditures** **0.44**

Gov't Consumption 0.05

Transfers to HH 0.25

Bond Interest Payments 0.04

Money Interest Payments 0.10

# Three Explorations

- Government policy variables  $\left\{ \pi, \tau, i_m, \frac{m}{y}, \frac{b}{y}, \frac{\psi}{y}, \frac{g}{y} \right\}$
- We are concerned with MONETARY policy not FISCAL policy.
- Therefore, fix government debt, spending, and transfers relative to output  $y$
- Gov't policy variables  $\left\{ \pi, \tau, i_m, \frac{m}{y} \right\}$
- Restriction on two MONETARY policy variables
  - interest on money and money stock cannot both be fixed.



# 1. Monetary Policy with Endogenous Tax

## Rate

- What consequences do money supply policies have?

### Policy Regimes

Fixed across regimes

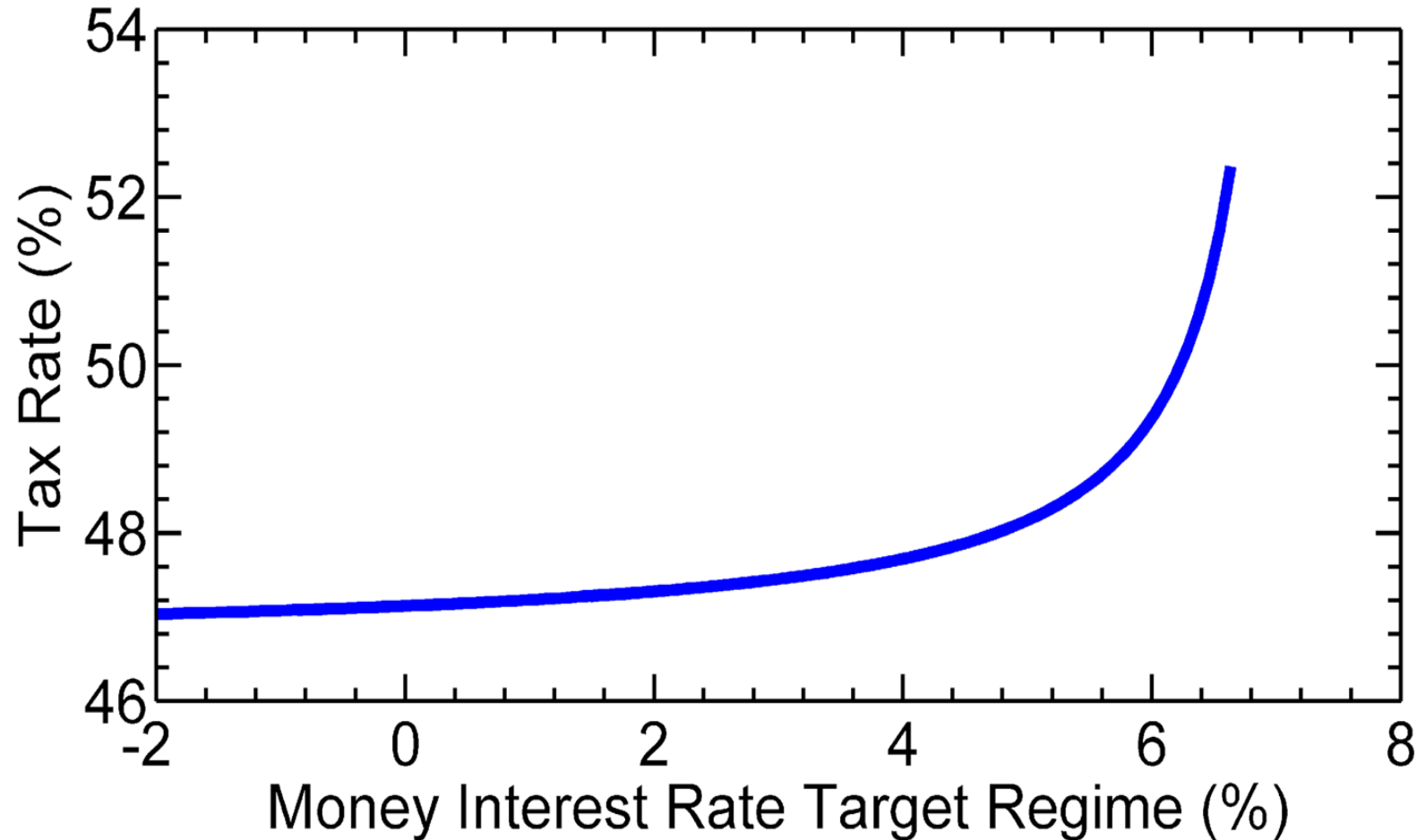
$$\left\{ \frac{g}{y} = 0.05, \frac{\psi}{y} = 0.25, \frac{b}{y} = 0.50, \pi = 0.02 \right\}$$

Varies across regimes

$$\left\{ \frac{m}{y}, i_m, \tau \right\}$$

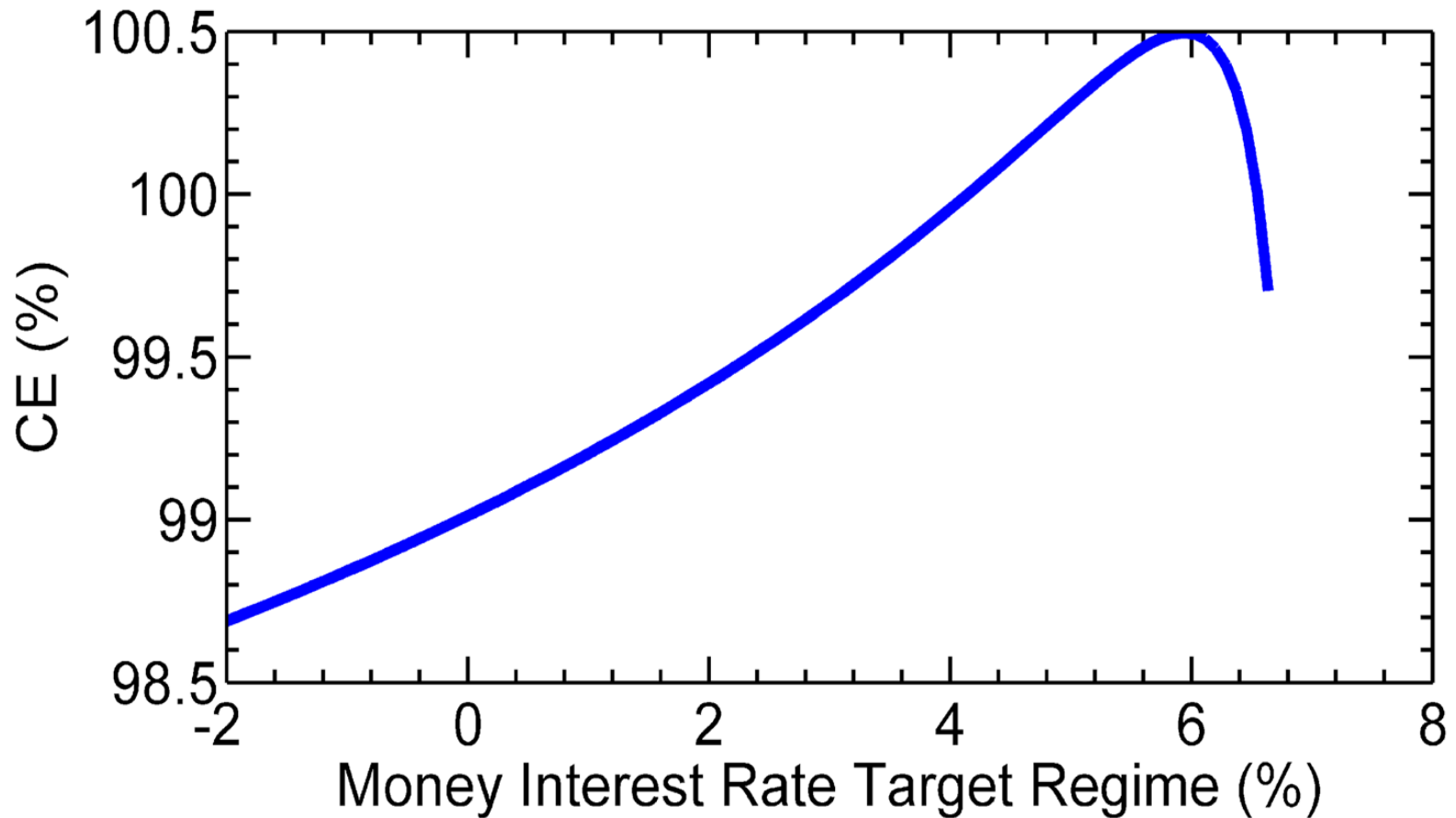
# Labor tax rates for different interest rate targets

---



# Welfare for interest rate target regimes

---



# Implications

---

- In a regime with a fixed inflation rate target, FISCAL POLICY must respond to changes in INTEREST RATE POLICY
- Hump shape welfare arises for two reasons
  - Higher interest means more money => more output
  - Higher interest means high labor tax => less output
- Welfare highest when interest on money is 6% *in this economy*

## 2. Monetary Policy with Endogenous **Inflation** Rate

---

- What consequences do money supply policies have?

### Policy Regimes

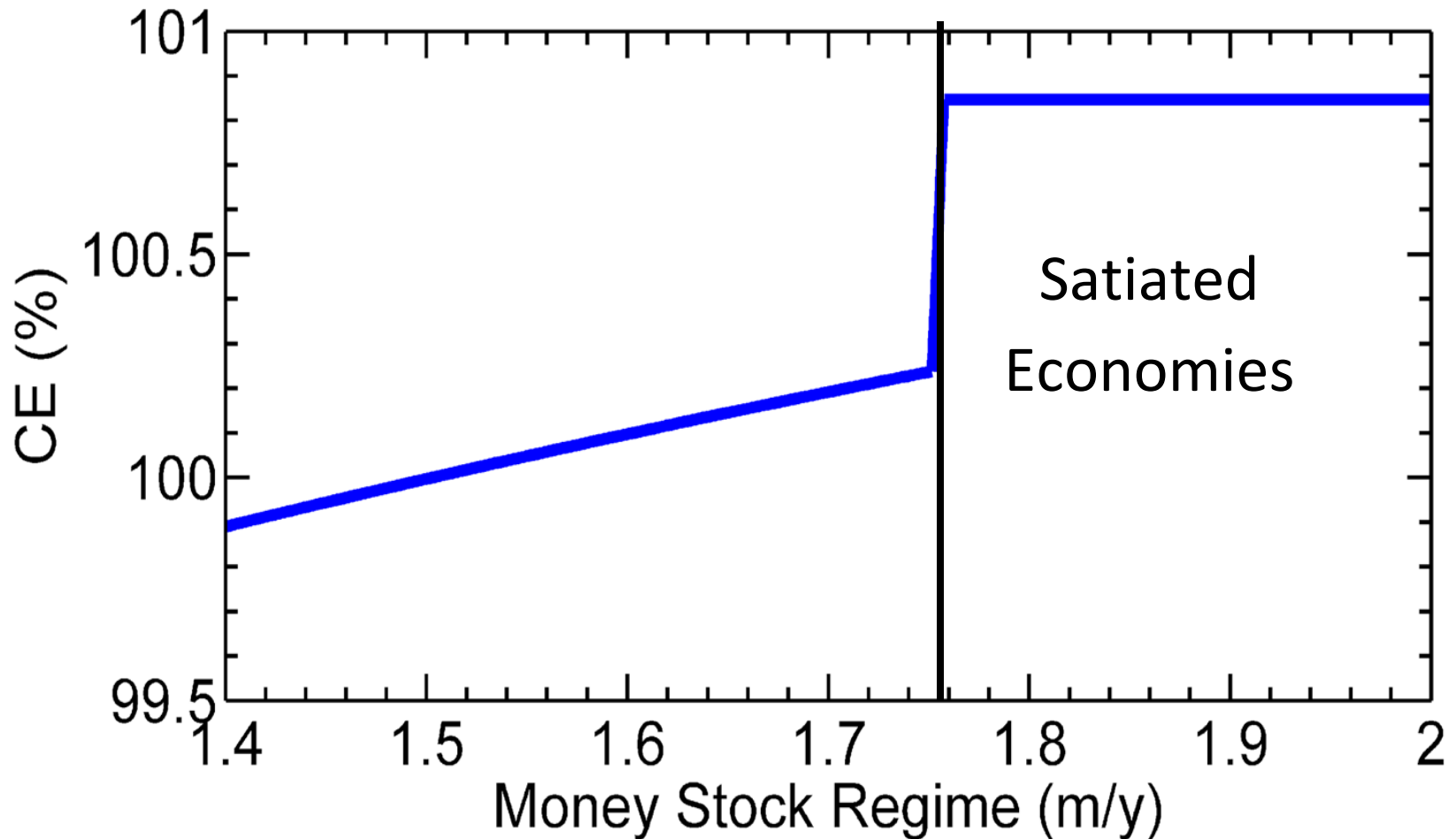
Fixed across regimes

$$\left\{ \frac{g}{y} = 0.05, \frac{\psi}{y} = 0.25, \frac{b}{y} = 0.50, \tau = 0.52 \right\}$$

Varies across regimes

$$\left\{ \frac{m}{y}, i_m, \pi \right\}$$

# Welfare for interest rate target regimes



# Friedman Rule

---

- Friedman Rule calls for nominal return on money equal to social cost of producing money (which is zero for our economies)
- Achieved with deflation equal to real interest rate
- Friedman rule not feasible with a fiat valued currency system (see McAndrews 2015)

# Friedman Satiation

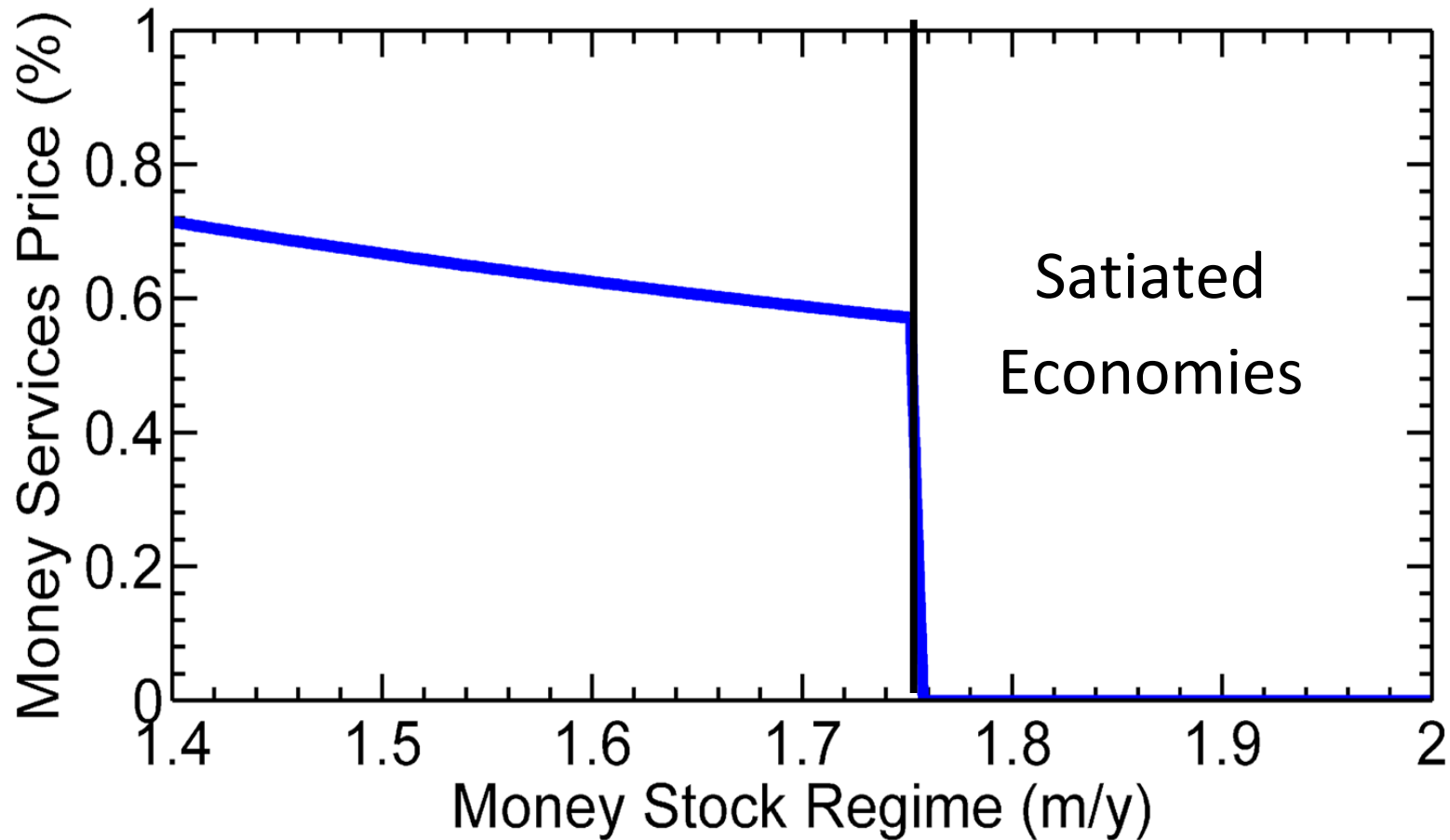
---

- With a fiat value system, **Friedman Satiation** can be implemented with **positive inflation!**
- With satiation  $r_m = 0$  ;  $i_m = i_b$
- Private marginal cost of holding money equals the social cost of producing money



# With satiation, rental price of money is zero

---



### 3. Inflation Rate Targeting Regimes

---

- What are the consequences of different inflation rate targets?

#### Policy Regime

Fixed across regimes

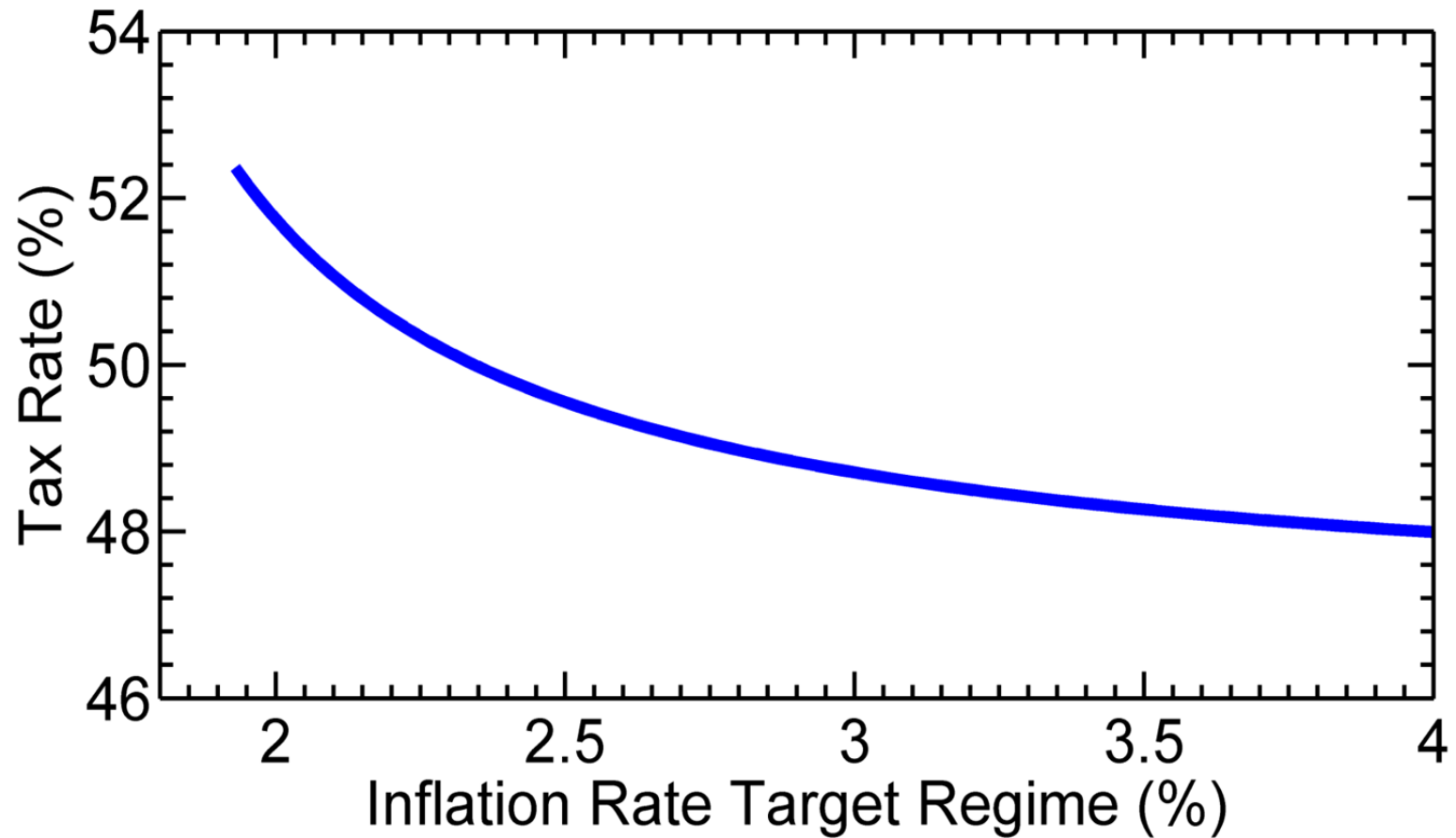
$$\left\{ \frac{g}{y} = 0.05, \frac{\psi}{y} = 0.25, \frac{b}{y} = 0.5, i_m = 0.06 \right\}$$

Varies across regimes

$$\left\{ \pi, \tau, \frac{m}{y} \right\}$$

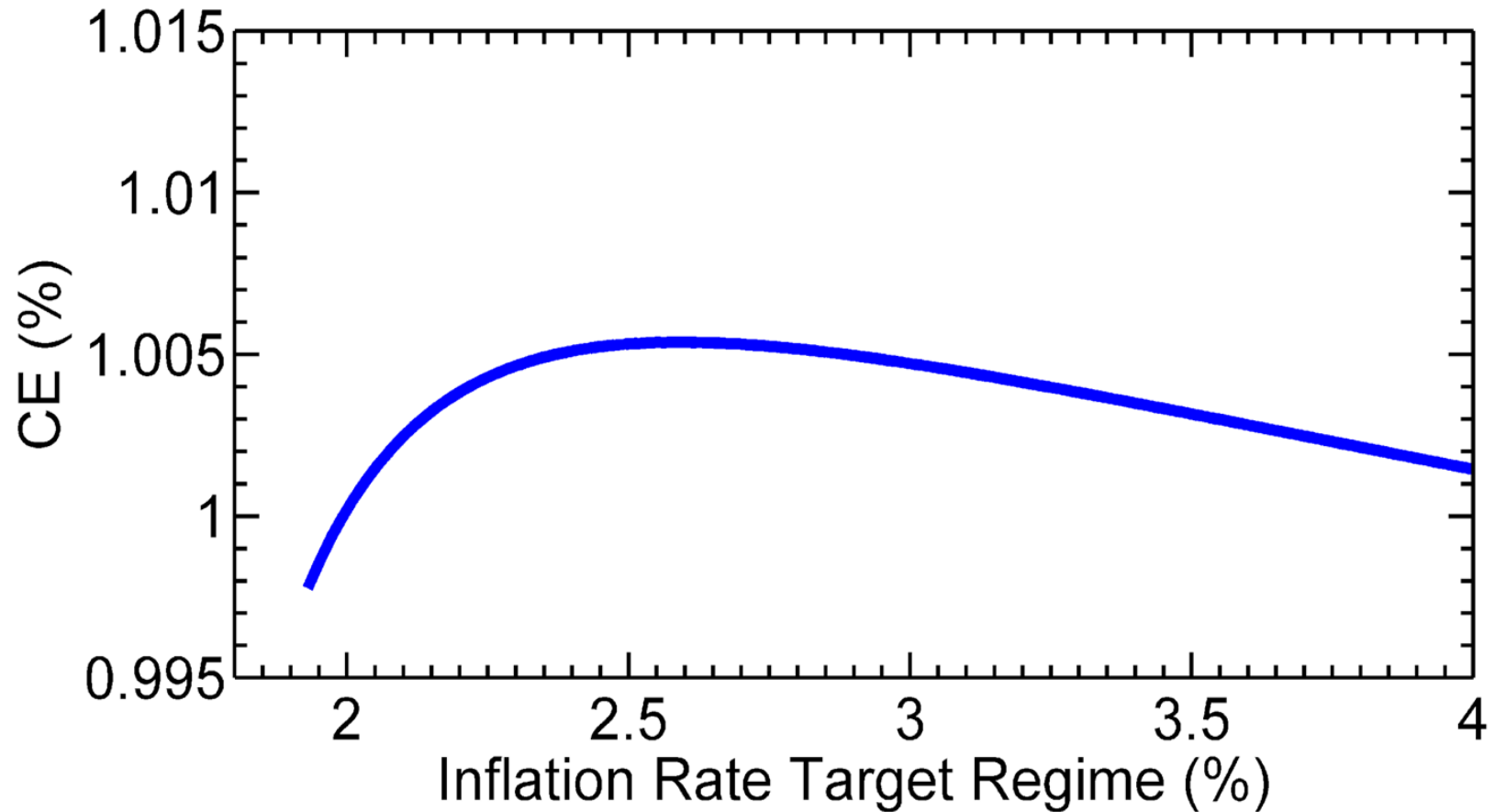
# Labor tax rates for inflation rate target regimes

---



# Welfare for inflation rate target regimes

---



# Implications

---

- Welfare indicator highest when inflation is 2.5% and labor tax rate is 49.5% (lower than baseline)
- Some inflation is an effective method of financing government consumption
- High inflation is not an effective financing option because labor tax rate decreases very little

# **Possible Problems and Advantages**

# Possible Problems with This System

---

Before initiating this system, should consider:

- Privacy protection and time consistency
  - See work of Rabee Tourky (ANU) who makes a case for privacy protection
  - Will not deal with these big problems here
- Shadow Banking
  - There is a way to deal with this problem

# Possible Solution to the Shadow Banking Problem

---

- Tax net interest income at a 100% rate for limited liability businesses
- This effectively eliminates businesses that borrow low from one group and lend high to another



# Advantages of System

---

- No bank runs
- No too-big-to-fail problem
- No need for costly regulation as with the U.S. deposit insurance system
  - These costs are about one-half a percent per year of deposits at banks

# Conclusion

---

- We explored a fiat value system which is technically possible given the current state of information-processing technology
- We put money services in the aggregate production function

# Conclusion Continued

---

- It is consistent with both traditional money demand functions and with zero nominal interest rates for extended periods (Japan, 1992-2018)
- Much more research is needed
- Whether going to a currency-less system is good or bad is an open question

# Conclusion Continued

---

- We have shown that monetary policy and fiscal policy are not independent, and evaluating a policy regime is an advanced exercise in public finance