## Inflation as a Long-run Optimal Policy in an Open Economy

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## Inflation $\rightarrow$ Production $\rightarrow$ Terms of trade

Fact 1: Trend inflation (in many countries)
Fact 2: Price rigidity: X-country, X-good diffs

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- Fact 1: Trend inflation (in many countries)
- Fact 2: Price rigidity: X-country, X-good diffs
- Question: Long-run implications w/ trade
- Model: Trend Calvo + Ricardo (-Viner) trade
  No previous papers

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- Fact 1: Trend inflation (in many countries)
- Fact 2: Price rigidity: X-country, X-good diffs
- Question: Long-run implications w/ trade
- Model: Trend Calvo + Ricardo (-Viner) trade
  No previous papers
- $\star$  Inflation affects trade pattern
  - Breaking the dichotomy
- $\star$  Welfare enhancing inflation
  - Contrast to closed or small-open models
  - Effect of the terms of trade

- $t=0,1,...,\infty$ , analyze stationary state
- Home & foreign (w/ \* if necessary)
- Stand-in HH in each country
- Final goods *i*, costless-tradeable
- Continuum  $\upsilon \in (0,1)$  of non-tradeable intermediate goods for each i
- No intl asset trade & balanced trade
- Money-less economy

# Model environment: Closed-economy



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# Model environment: CRS (Ricardian trade)



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# Model environment: DRS (Ricardo-Viner trade)



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# Home & the rest of the world

- foreign: the rest of the world
- Symmetry except for
  - Size: N.  $N^*$
  - Exog. tech of int. good:  $\theta_{it}$ ,  $\theta_{it}^*$  Prob. of price change:  $\omega_i$ ,  $\omega_i^*$

  - Tax/subsidy rates:  $\tau_{Lt}, \tau_{Lt}^*, \tau_{it}, \tau_{it}^*$  Inflation rate:  $\Pi, \Pi^*$
- Not consider strategic situation
  - $\Pi$ : treated as a policy parameter
  - $\Pi^*$ : exogenously fixed

# Households

$$\begin{split} & \max \, \mathrm{E}_0 \sum_{t=0}^{\infty} \beta^t u \bigg( \bigg( \sum_i \alpha_i c_{it}^{\frac{\rho-1}{\rho}} \bigg)^{\frac{\rho}{\rho-1}}, l_t \bigg), \\ & \text{s.t.} \ \frac{\sum_i P_{it} c_{it}}{P_t} + b_t + \tau_{Lt} = \frac{1+i_{t-1}}{\Pi_t} b_{t-1} + w_t l_t + f_t, \\ & \text{where} \ u(c,l) = c^{\psi} (1-l)^{1-\psi}. \end{split}$$

- $b_t$ : intra-country nominal bond
- $\tau_{Lt}$ : lump-sum tax
- $i_t$ : nominal int. rate
- $\Pi_t = P_t/P_{t-1}$ : gross inf. rate
- $f_t$ : firms' real prfts

# Final goods firms

$$\max P_{it}y_{it} - \int_0^1 P_{it}(v)y_{it}(v)dv,$$
  
s.t.  $y_{it} = \left(\int_0^1 y_{it}(v)^{\frac{\eta-1}{\eta}}dv\right)^{\frac{\eta}{\eta-1}}$ 

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# Intermediate good firms

- Each int. firm produces differentiated product • Index v
- Facing the demand curve
- Using labor
  - RTS:  $\gamma \in (0, 1]$
- Input subsidy  $\tau_{it} \in [0, 1)$
- $\theta_{it}$ : productivity, common w/i industry
- Can update price w/ prob.  $1-\omega_i$
- Intertemporal problem of prfts max
  - discounting:  $\Lambda_{tt+j} \equiv \beta^j \frac{u_{ct+j}}{u_{ct}}$

# Intermediate good firms

$$\max_{\substack{P_{it}(\upsilon),\{l_{it+j}(\upsilon),y_{it+j}(\upsilon)\}_{j=0}^{\infty}}} \mathcal{E}_{t} \sum_{j=0}^{\infty} \Lambda_{tt+j} \omega_{i}^{j}$$
$$\times \left[ \frac{P_{it}(\upsilon)}{P_{t+j}} y_{it+j}(\upsilon) - (1-\tau_{it+j}) w_{t+j} l_{it+j}(\upsilon) \right],$$

s.t.

$$y_{it+j}(\upsilon) = \theta_{it+j} l_{it+j}(\upsilon)^{\gamma},$$
  
$$y_{it+j}(\upsilon) = \left(\frac{P_{it+j}}{P_{it}(\upsilon)}\right)^{\eta} y_{it+j}.$$

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• Those who adjust price: pick  $ilde{P}_{it}$ 

$$\left(\frac{\tilde{P}_{it}}{P_t}\right)^{1-\eta+\frac{\eta}{\gamma}} = \frac{\eta}{\eta-1}$$

$$\times \frac{\mathrm{E}_t \sum_{j=0}^{\infty} \Lambda_{tt+j} \omega_i^j \left(\frac{P_{it+j}}{P_{it}}\right)^{\frac{\eta}{\gamma}} (1-\tau_{it+j}) \frac{w_{t+j}}{\gamma} \left(\frac{y_{it+j}}{\theta_{it+j}}\right)^{\frac{1}{\gamma}}}{\mathrm{E}_t \sum_{j=0}^{\infty} \Lambda_{tt+j} \omega_i^j \frac{P_{it+j}}{P_{t+j}} \left(\frac{P_{it+j}}{P_{it}}\right)^{\eta-1} y_{it+j}}$$

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# • Industry-price, law of motion $P_{it} = \left(\omega_i P_{it-1}^{1-\eta} + (1-\omega_i)\tilde{P}_{it}^{1-\eta}\right)^{\frac{1}{1-\eta}}$

# • LoM of $p_{it} \equiv P_{it}/P_t$ determined

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#### Price dispersion leads to resource costs

$$y_{it} \left(\frac{P_{it}}{P_{it}(\upsilon)}\right)^{\eta} = y_{it}(\upsilon) = \theta_{it} l_{it}(\upsilon)^{\gamma}$$

Integration over v



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#### Stationary state

Consider  $\theta_{it} = \theta_i$ ,  $\Pi_t = \Pi$ • Agg. & industry-level variables: constant  $y_i = \frac{\theta_i}{s_i^{\gamma}} l_i^{\gamma}$ ,  $p_i = (1 - \tau_i) v_i \frac{s_i^{\gamma} w}{\theta_i \gamma} l_i^{1-\gamma}$ 

where

$$s_{i} = \frac{1 - \omega_{i}}{1 - \omega_{i} \Pi^{\frac{\eta}{\gamma}}} \left( \frac{1 - \omega_{i} \Pi^{\eta-1}}{1 - \omega_{i}} \right)^{\frac{\eta}{\eta-1}\frac{1}{\gamma}},$$
$$v_{i} = \frac{\eta}{\eta - 1} \frac{1 - \beta \omega_{i} \Pi^{\eta-1}}{1 - \beta \omega_{i} \Pi^{\frac{\eta}{\gamma}}} \frac{1 - \omega_{i} \Pi^{\frac{\eta}{\gamma}}}{1 - \omega_{i} \Pi^{\eta-1}}.$$

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- $\Pi>1$  ,  $\omega>0$   $\rightarrow$  markup gradually  $\downarrow$
- Price re-setter picks larger markup
- Avg markup  $(v_i)$ , gradually  $\downarrow$
- Given price dispersion, output dispersion
- Ex ante symmetric, ex post not
- Allocation inefficiency,  $s_i$

## Dispersion costs (against annual $\Pi$ )



- min: s = 1 (when  $\Pi = 1$  or  $\omega = 0$ ) Asymmetrically increasing as  $\Pi$  deviate
- Asymmetrically increasing as  $\Pi$  deviates

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# Markup (against annual $\Pi$ )



- Decreasing in  $\Pi$  around  $\Pi=1$
- Often abstracted (thru tax adjustment)

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# Relative price (against annual $\Pi$ )



- Min: slightly larger than  $\Pi = 1$
- Small impact of  $v \rightarrow Assume (1 \tau_i)v_i = 1$

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CRS, single-good autarky

- CRS ( $\gamma = 1$ ), single-good, autarky
- Welfare

$$u \propto \left(\frac{\theta}{s}\right)^{\psi}$$

• s = 1 (by  $\Pi = 1$ ) achieves max

 Result not much affected by cost of hitting zero-lower bound (Schmitt-Grohé & Uribe 11, Coibion et al. 12)

# CRS, two-good autarky

- CRS, two-good autarky
- Welfare
  - Max at  $\Pi = 1$
- Relative price

$$\frac{p_A}{p_B} = \frac{\frac{s_A}{\theta_A}}{\frac{s_B}{\theta_B}}$$

• Relative price depends on  $\Pi$ ,  $\omega_i,$  ... thru s (& v)

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## CRS, two-good costless trade eqm

Labor market

$$\sum_i l_i = l$$

Bond market

$$b_i = 0$$

Costless trade goods market for i = A, B

$$Nc_i + N^*c_i^* = Ny_i + N^*y_i^*$$

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Two-good model, trade pattern (Prop. 1)

- CRS ightarrow Ricardian trade
- Home exports good A if

$$\frac{\frac{s_A}{\theta_A}}{\frac{s_B}{\theta_B}} = \frac{p_A}{p_B} < \frac{p_A^*}{p_B^*} = \frac{\frac{s_A^*}{\theta_A^*}}{\frac{s_B^*}{\theta_B^*}}$$

- Inf. rate affects trade pattern
  thru s (& v)
- Eqm rel. price = home's terms of trade (TOT)

## Prop 2: TOT $\uparrow$ by $\Pi$ 's deviation from 1



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# Prop 2: TOT $\uparrow$ by $\Pi$ 's deviation from 1 $p_A/p_B$ $\tfrac{(1\!-\!\tau_A^*) v_A^* s_A^* \theta_B^*}{(1\!-\!\tau_B^*) v_B^* s_B^* \theta_A^*}$ $\frac{(1-\tau_A)v_As_A\theta_B}{(1-\tau_B)v_Bs_B\theta_A}$ $Ny_A + N^*y_A^*$ $N\frac{\theta_A}{s_A} + N^* \frac{\theta_A^*}{s^*}$ $N\frac{\theta_A}{\epsilon}$

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• Home's welfare

$$u = \left(\frac{\psi}{1-\psi}\right)^{\psi-1} \left(\frac{\theta_A}{s_A}\right)^{\psi} \times \left(\alpha_A^{\rho} + \alpha_B \alpha_A^{\rho-1} \left(\frac{\theta_B^*}{\theta_A} \frac{s_A}{s_B^*} \frac{N^*}{N}\right)^{\frac{\rho-1}{\rho}}\right)^{\frac{\psi}{\rho-1}}$$

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# Prop 3: Welfare enhancing inflation

$$\begin{split} \frac{\partial u}{\partial \Pi} &= -\Phi_0 \Phi_1 \frac{1}{s_A} \frac{\partial s_A}{\partial \Pi} \\ \text{where } \Phi_0 > 0 \text{ (constant) and} \\ \Phi_1 &= 1 - \frac{1 - \rho}{\rho} \frac{\alpha_B}{\alpha_A} \left( \frac{\theta_B^*}{\theta_A} \frac{s_A}{s_B^*} \frac{N^*}{N} \right)^{\frac{\rho - 1}{\rho}} \end{split}$$

• If  $\Phi_1 > 0$ ,  $\Pi = 1$ : maximizer • If  $\Phi_1 < 0$ ,  $\Pi = 1$ : (local) minimizer

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Mechanism known as immiserizing growth

- Deviation of ∏ from 1: effective TFP ↓
  (a) Production capacity ↓
  (b) Example ↓ Example ↓ TOT
- (b) Exports  $\downarrow \rightarrow$  Export price  $\uparrow \rightarrow$  TOT  $\uparrow$
- (Reverse version) known as "immiserizing growth" (Johnson 55; Bhagwati, 58)
- Closed & Small-open: only (a)
- Condition on  $\Phi_1$ : making (b) stronger
  - A key parameter:  $\rho$  (subst. b/w A & B)

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#### Comparison: small-open vs. two-country



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DRS case: Ricardo-Viner trade model

- DRS ( $\gamma < 1$ )
  - Both countries produce both goods
  - Ricardo-Viner (also known as specific factors) trade model
  - Consider home exports A, imports B

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  - Consider home exports A, imports B
- Prop 4: Unique eqm exists under costless trade
- Prop 5: TOT  $\uparrow$  when  $\Pi$ 's deviation from 1 if

$$\frac{\partial s_A^{\gamma}}{\partial \Pi} \frac{\Pi}{s_A^{\gamma}} \bigg| \geq \bigg| \frac{\partial s_B^{\gamma}}{\partial \Pi} \frac{\Pi}{s_B^{\gamma}} \bigg|$$

- Exporting industry responds more to  $\Pi$  (i.e., more sticky)

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- $\mathrm{d}u/\mathrm{d}\Pi \gtrless 0$
- $\mathrm{d}p/\mathrm{d}\Pi$  depends on various parameters
- Closed or small-open: only 2nd term
   Π = 1 always optimal



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# Back of the envelope calculation

Assume 
$$s_A = s_B$$

 $\frac{\mathrm{d}u}{\mathrm{d}\Pi}\frac{\Pi}{u} \propto \frac{\mathrm{IM}}{\mathrm{GDP}} \times \frac{\mathrm{d}p}{\mathrm{d}\Pi}\frac{\Pi}{p} - \frac{\partial s^{\gamma}}{\partial\Pi}\frac{\Pi}{s^{\gamma}}$  $= 0.11 \times 0.63 - 0.57$ 

• 
$$\frac{\text{IM}}{\text{GDP}} = 0.11$$
 US data  
•  $\frac{\text{d}p}{\text{d}\Pi} \frac{\Pi}{p} = 0.63$  regression using US time series  
•  $\frac{\text{d}s^{\gamma}}{\text{d}\Pi} \frac{\Pi}{s^{\gamma}} = 0.57$  calculated by setting  $\gamma = 0.95$ ,  
 $\eta = 10$ ,  $\omega = 0.753$ ,  $\Pi^{1/12} = 1.03$ 

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Why important?: positive optimal inf.

- Long-run optimality of zero-inf. in closed economy
  - Eliminating price dispersion cost (King & Wolman 99, Schmitt-Grohé & Uribe 11, Coibion et al. 12)

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  - Short-run: nominal exchange rate, terms of trade (e.g., Benigno 04, Corsetti et al. 11, Bergin & Corsetti, 16)

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- ★ Provide long-run optimal in open-economy thru the terms of trade change

Why important?: digging up TFP

- Ricardian models: empirically good
  - Trade pattern & X-country prosperity (Eaton & Kortum 02, Alvarez & Lucas 07, Waugh 10, Costinot et al. 12)
  - TFP (= labor productivity): the driver

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- The source of sector-level TFP (LP)?
  - Trade context (Matsuyama 05, Ishise 16)
  - Amplification thru allocation (e.g., Hsieh & Klenow 09) given exogenously hetero TFP

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- $\star$  Provide a story of sector-level TFP
- $\star$  Breaking the classical dichotomy

# Summary & future works

- Trend-Calvo & Ricardo (-Viner) trade
- Inf. rate affects trade pattern
- TOT attenuates the welfare loss
- Optimal inflation rate
  - $\Pi=1 \mbox{ may not be optimal under some parameters}$
- More empirical assesment
  - $\Pi$ 's role of determining trade pattern
  - TOT on the long-run welfare

# Model structure (c.f., Obstfeld-Rogoff)



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# Law of motion of the price dispersion

$$s_{it} = (\omega_i)^0 (1 - \omega_i) \left(\frac{P_{it}}{\tilde{P}_{it}}\right)^\eta + (\omega_i)^1 (1 - \omega_i) \left(\frac{P_{it}}{\tilde{P}_{it-1}}\right)^\eta + (\omega_i)^2 (1 - \omega_i) \left(\frac{P_{it}}{\tilde{P}_{it-2}}\right)^\eta + \dots = (1 - \omega_i) \left(\frac{P_{it}}{\tilde{P}_{it}}\right)^\eta + \omega_i \left(\frac{P_{it}}{P_{it-1}}\right)^\eta s_{it-1}$$

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