# Old, Sick Alone, and Poor: A Welfare Analysis of Old-Age Social Insurance Programs 

## R. Anton Braun

Federal Reserve Bank of Atlanta

Karen A. Kopecky

Federal Reserve Bank of Atlanta

## Tatyana Koreshkova

Concordia University and CIREQ

CIGS Conference on Macroeconomic Theory and Policy
June 2013

## Overview

In 1972, Friedman argued:

- There is no need for a universal social security (SS) program in the US.
- Means-tested social insurance (SI) programs are sufficient in insuring against old-age risks.

Feldstein (1987) showed:

- SS can be better than means-tested SI when individuals are heterogenous because means-tested SI has large negative incentive effects on the savings behavior of the poor.


## Overview

- Objective: Assess the welfare and incentive effects of SS and means-tested SI programs in the US.
- In particular, we ask
- Is there a role for any SI for retirees?
- If yes, what combination of programs is preferred?


## Overview

We answer these questions using a model in which retirees are subject to

- health
- medical expense and
- spousal death risk
in addition to
- lifetime earnings and
- survival risk.


## Our Answers

Is there a role for any SI for retirees?

- Yes, individuals prefer an economy with SI programs of the size currently offered in the US to one without.
- Medical expenses and their associated risks play an important role in this result.


## Our Answers

What combination of programs is preferred?

- Despite that
- Means-tested SI has the negative incentive effects on poorer households emphasized by Feldstein
- and SS dampens these effects

We find results consistent with Friedman's claim:
All newborn prefer means-tested SI of the scale in the US to either SS alone or both programs.

- Why? Insurance benefits of means-tested SI are large even for rich.


## Motivation: Risks

We model old-age health, medical expense, and spousal death risk because:

- Fact: Poor health, hospital stays, nursing home stays and widowhood are all associated with higher probabilities and persistence of impoverishment.
- We measure impoverishment as movement into the 1st quintile of the wealth distribution.


## Motivation: Risks

- Nursing home stays are associated with higher probabilities and persistence of impoverishment.


## Percentage of Retirees Moving from Each Quintile to Quintile 1

|  |  |  | 65-74 Year-olds |  | $75-84$ Year-olds |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $85+$ Year-olds |  |  |  |  |  |  |
| Quintile | None | NH Stay | None | NH Stay | None | NH Stay |
| 1 | 75.7 | 87.9 | 74.6 | 86.0 | 69.3 | 75.6 |
| 2 | 18.0 | 25.6 | 17.4 | 23.7 | 20.2 | 31.8 |
| 3 | 3.8 | 9.6 | 4.5 | 11.8 | 7.1 | 14.3 |
| 4 | 1.0 | 5.3 | 1.8 | 5.0 | 3.5 | 8.2 |
| 5 | 0.5 | 3.3 | 0.5 | 3.9 | 1.5 | 4.6 |

[^0]
## Motivation: Risks

We model old-age health, medical expense, and spousal death risk because:

- Fact: Poor health, hospital stays, nursing home stays and widowhood are all associated with higher probabilities and persistence of impoverishment.
- We measure impoverishment as movement into the 1 st quintile of the wealth distribution.
- And SS and means-tested SI partially insure individuals against these risks.


## Model: Key Features

- Full-lifecycle, OLG, GE model
- Households
- become active at age 21 (period $=2$ years)
- While working:
- are married couples
- differ by education status of members
- face uncertainty over male and female's labor productivity
- choose consumption, savings, female labor supply


## Model: Key Features

- Households
- retire exogenously at age 65
- While retired:
- married, widows, widowers
- have uncertain
- death (foreseen 1 period in advance)
- health status
- medical expenses
- choose consumption, savings
- die with certainty at age 100


## Model: Key Features

- Survival and health status
- are exogenous shocks
- determined by age, sex, marital status, and previous health status
- Medical expenses
- are exogenous expense shocks
- do not affect household utility
- depend on age, sex, marital status, current health status and death
- include a small prob. but large expense "nursing home" shock


## Model: Key Features

- Social insurance (SI) includes
- progressive PAYG social security program (includes spousal and survivor benefits)
- means-tested social insurance program (Medicaid/other old-age SI)
- Medicare (all expenses are net of Medicare, include Medicare earnings tax)
- SI financed (along with government expenditures) by
- progressive income taxes
- payroll tax
- proportional capital income tax
- No private insurance and no borrowing


## Retired Household's Problem

## Retired household solves

$$
\begin{gathered}
V\left(j, a, \overline{\mathbf{e}}, \mathbf{h}, \varepsilon_{M}, d, d^{\prime}\right)=\max _{c, a^{\prime}}\left\{u^{R}(c, d)\right. \\
\left.+\beta E\left[\sum_{d^{\prime \prime}=0}^{2} \pi_{j}\left(d^{\prime \prime} \mid \mathbf{h}^{\prime}, d^{\prime}\right) V\left(j+1, a^{\prime}, \overline{\mathbf{e}}, \mathbf{h}^{\prime}, \varepsilon_{M}^{\prime}, d^{\prime}, d^{\prime \prime}\right) \mid \mathbf{h}, \varepsilon_{M}\right]\right\}
\end{gathered}
$$

subject to ...
age
assets
average earnings
health status
household medical expense shocks
marital status
j
a

$$
\overline{\mathbf{e}} \equiv\left\{\bar{e}^{m}, \bar{e}^{f}\right\}
$$

$$
\mathbf{h} \equiv\left\{h^{m}, h^{f}\right\}
$$

$$
\varepsilon_{M} \equiv\left\{\varepsilon_{M, 1}, \varepsilon_{M, 2}\right\}
$$

$$
d \in\{0,1,2\}
$$

## Retired Household's Problem

## Retired household solves

$$
\begin{gathered}
V\left(j, a, \overline{\mathbf{e}}, \mathbf{h}, \varepsilon_{M}, d, d^{\prime}\right)=\max _{c, a^{\prime}}\left\{u^{R}(c, d)\right. \\
\left.+\beta E\left[\sum_{d^{\prime \prime}=0}^{2} \pi_{j}\left(d^{\prime \prime} \mid \mathbf{h}^{\prime}, d^{\prime}\right) V\left(j+1, a^{\prime}, \overline{\mathbf{e}}, \mathbf{h}^{\prime}, \varepsilon_{M}^{\prime}, d^{\prime}, d^{\prime \prime}\right) \mid \mathbf{h}, \varepsilon_{M}\right]\right\}
\end{gathered}
$$

subject to

$$
\begin{aligned}
& c \geqslant 0, \quad a^{\prime} \geqslant 0 \\
& c+M+a^{\prime}=a+y^{R}-T_{y}^{R}+T^{R} .
\end{aligned}
$$

$$
M \equiv \Phi\left(j, \mathbf{h}, \varepsilon_{M}, d, d^{\prime}\right)
$$

$$
y^{R} \equiv S(\overline{\mathbf{e}}, \mathrm{~d})+\left(1-\tau_{\mathrm{c}}\right) \mathrm{ra}
$$

$$
T_{y}^{R} \equiv \tau_{y}^{R}\left(\left(1-\tau_{c}\right) a r, S(\overline{\mathbf{e}}, d), d, M\right) \quad \text { income taxes }
$$

$$
\mathrm{Tr}^{R}
$$

medical expenses income
means-tested SI transfer

## Retired Household's Problem

Means-tested SI transfers to retirees are given by

$$
\operatorname{Tr}^{R} \equiv \begin{cases}\max \left\{\underline{y}^{\mathrm{d}}+\varphi M-I^{\mathrm{R}}, \underline{c}^{\mathrm{d}}+M-\mathrm{I}^{\mathrm{R}}, 0\right\}, & \text { if } \underline{y}^{\mathrm{d}}>\mathrm{I}^{\mathrm{R}}-M \\ 0, & \text { otherwise }\end{cases}
$$

where $I^{R} \equiv a+y^{R}-T_{y}^{R}$ is cash-in-hand.

- Retirees on Medicaid must pay a Medicaid copayment of $(1-\varphi) M$.
- We cap the copayment such that the minimum level of consumption is $\underline{c}^{\mathrm{d}}$.


## Competitive Equilibrium

We consider a steady-state competitive equilibrium of a small open economy.

## Calibration: A few highlights

- We calibrate the model to reproduce this demographic structure:



## Calibration: A few highlights

## Pre-Medicaid Medical Expense Process

- Stochastic component of expenses is calibrated to estimates from French and Jones (2004) and data on NH stays and expenses.
- We estimate the deterministic component using HRS data.
- Cohort and income effects are controlled for in the estimation.


## Calibration: A few highlights

- Estimated effects of various factors on pre-Medicaid expenses:



## Assessment: A few highlights

- We set the consumption floors for retirees to target Medicaid take up rates by marital status.
- The model does a good job reproducing them by age groups.


## Medicaid Take-Up Rates

| Age | $65-74$ | $75-84$ | $85+$ |
| :---: | :---: | :---: | :---: |
| Marital Status <br> Married <br> data | 0.07 | 0.07 | 0.11 |
| model <br> Widows <br> data | 0.05 | 0.07 | 0.12 |
| model <br> Widowers <br> data | 0.22 | 0.19 | 0.24 |
| model | 0.19 | 0.23 | 0.25 |

## Assessment: A few highlights

The model also matches well

- Flows into Medicaid by age and marital status
- Average OOP medical expenses by age and marital status
- The conditional probabilities and persistence of impoverishment already discussed


## Review of Questions

## What does the model say about the following questions:

- Is there any role for public SI programs for retirees?
- If yes, what combination of programs is preferred?


## Experiments

## To find out we:

- Consider 4 versions of the baseline model: 'no Sl', 'SS only', 'means-tested SI only', and 'both (U.S. economy)'
- Consider same economies but with no medical expenses to understand their role.


## How we shut-down each program:

- SS: Remove benefits and reduce payroll taxes
- Means-tested SI: Set consumption floor very low $(\approx \$ 50$ a year) and reduce income taxes


## Experiments

## Some details:

- All experiments are revenue-neutral: G/Y fixed
- Use proportional income tax/transfer to satisfy govt budget const.
- Welfare is measured as an equivalent \% variation in lifetime consumption.


## Role of Public SI in Our Model

- First, is there any role for public SI programs for retirees?
- To find out compare the 'no SI' economy to the economy with both programs...


## Role of Public SI in Our Model

When both programs are introduced into the 'no Sl' economy:

- Output, consumption, wealth and female labor supply all fall

|  | No SI | Both (U.S. Economy) |
| :--- | :---: | :---: |
| Output | 1.00 | 0.74 |
| Consumption | 0.71 | 0.50 |
| Wealth | 3.47 | 1.22 |
| Working Females' Hours | 0.39 | 0.34 |
| Female LFP | 0.49 | 0.46 |

## Role of Public SI in Our Model

When both programs are introduced into the 'no Sl' economy:

- Output, consumption, wealth and female labor supply all fall
- Despite this average newborn welfare increases

|  | No SI | Both (U.S. Economy) |
| :--- | :---: | :---: |
| Output | 1.00 | 0.74 |
| Consumption | 0.71 | 0.50 |
| Wealth | 3.47 | 1.22 |
| Working Females' Hours | 0.39 | 0.34 |
| Female LFP | 0.49 | 0.46 |
| Welfare, \% | 0.00 | 2.22 |

## Role of Public SI in Our Model

## Why does newborn welfare increase?

- Medical expenses and their associated risks increase the insurance value of SS and means-tested SI.
- When medical expenses are zero:
average welfare decreases from the introduction of both programs by $10.0 \%$.


## Which combination is preferred? Both v. SS Only

- Given that there is a role for old-age public SI: What combination of programs is preferred?
- To find out compare the economy with both programs to economies with either means-tested SI or SS removed.
- First consider removing means-tested SI...


## Which combination is preferred? Both v. SS Only

## When means-tested SI is removed:

- Output, consumption, wealth and female labor supply all increase.

Both (U.S. Economy) SS Only

| Output | 0.74 | 0.81 |
| :--- | :--- | :--- |
| Consumption | 0.50 | 0.56 |
| Wealth | 1.22 | 1.80 |
| Working Females' Hours | 0.34 | 0.38 |
| Female LFP | 0.46 | 0.52 |

## Which combination is preferred? Both v. SS Only

## When means-tested SI is removed:

- Output, consumption, wealth and female labor supply all increase.
- But removing means-tested SI leads to a large welfare loss.

|  | Both (U.S. Economy) | SS Only |
| :--- | :---: | :---: |
| Output | 0.74 | 0.81 |
| Consumption | 0.50 | 0.56 |
| Wealth | 1.22 | 1.80 |
| Working Females' Hours | 0.34 | 0.38 |
| Female LFP | 0.46 | 0.52 |
| Welfare, \% | 0.00 | -7.33 |

## Which combination is preferred? Both v. SS Only

## Why does newborn welfare fall so much?

- Retirees face more risk in our baseline model due to the presence of medical expenses.
- Means-tested SI is a very valuable form of insurance against medical-expense-related risks even when SS is available.
- When medical expenses are zero:
average welfare falls from the removal of means-tested SI by $0.3 \%$.


# Which combination is preferred? Both v. Means-tested SI Only 

- Now let's consider what happens when SS is removed...


## Which combination is preferred? Both v. Means-tested SI Only

## When SS is removed:

- Take-up rates of means-tested SI by poorer households increase significantly.
- Both at later ages and the fraction who roll on at 65.

Percent increase in means-tested SI take-up rates when SS is removed
Q1-Q5 are male PE quintiles


## Which combination is preferred? Both v. Means-tested SI Only

## Why do means-tested SI take-up rates increase?

Two reasons:

1. Insurance effect: Some of the insurance against survival and medical expense risk provided by SS is now provided by meanstested SI.

## Which combination is preferred? Both v. Means-tested SI Only

## Why do means-tested SI take-up rates increase?

Two reasons:
2. Incentive effect:

- Means-tested SI induces some poorer households not to save for retirement.
- These households roll directly onto means-tested SI at age 65.
- SS forces these households to save increasing their expected return from private savings.
- As a result some households choose to save on their own that would not have otherwise.
Thus removing SS exacerbates the negative incentive effects that means-tested SI has on savings behavior.


## Which combination is preferred? Both v. Means-tested SI Only

The impact of removing SS on take-up rates looks very different when there are no medical expenses.

Percent increase in means-tested SI take-up rates when SS is removed Q1-Q5 are male PE quintiles



## Which combination is preferred? Both v. Means-tested SI Only

## When SS is removed from the 'no medical expense' economy:

- The increase in take-up rates increases monotonically with age.
- Why? Insurance against survival risk that was provided by SS is now provided by means-tested SI.

Percent increase in means-tested SI take-up rates when SS is removed Q1-Q5 are male PE quintiles



## Which combination is preferred? Both v. Means-tested SI Only

## When SS is removed from the 'no medical expense' economy:

- Now only about $10 \%$ of Q1 roll in at age 65
- Why? Without medical expenses the negative incentive effect is small.

Percent increase in means-tested SI take-up rates when SS is removed
Q1-Q5 are male PE quintiles



## Which combination is preferred? Both v. Means-tested SI Only

## Overall, removing SS results in:

- Means-tested SI take-up rates increasing from 13\% to 34\%.
- Government outlays on means-tested SI increase from 0.75\% to $2.5 \%$ of GNP.


## Which combination is preferred? Both v. Means-tested SI Only

## Overall, removing SS results in:

- Means-tested SI take-up rates increasing from $13 \%$ to $34 \%$.
- Government outlays on means-tested SI increase from $0.75 \%$ to $2.5 \%$ of GNP.
- Despite this wealth increases and taxes fall.

|  | Both <br> (U.S. Economy) | Means-tested <br> SI Only |
| :--- | :---: | :---: |
| Output | 0.74 | 0.81 |
| Consumption | 0.50 | 0.56 |
| Wealth | 1.22 | 1.91 |
| Prop. Tax | 0.0 | -0.04 |

## Which combination is preferred? Both v. Means-tested SI Only

## Overall, removing SS results in:

- Means-tested SI take-up rates increasing from $13 \%$ to $34 \%$.
- Government outlays on means-tested SI increase from $0.75 \%$ to $2.5 \%$ of GNP.
- Despite this wealth increases and taxes fall.
- And newborns experience a large welfare gain.

|  | Both <br> (U.S. Economy) | Means-tested <br> SI Only |
| :--- | :---: | :---: |
| Output | 0.74 | 0.81 |
| Consumption | 0.50 | 0.56 |
| Wealth | 1.22 | 1.91 |
| Prop. Tax | 0.0 | -0.04 |
| Welfare, \% | 0.0 | 11.8 |

## So which combination is preferred?

## Our results support Friedman's claim:

- Average newborn welfare is highest in the economy with meanstested SI only.
- Moreover, all newborns prefer this economy.
- This is despite the fact that means-tested SI has large negative incentive effects on the behavior of poorer households and that SS dampens these effects.

|  | Both <br> (U.S. Economy) | SS Only | Means-tested <br> SI Only |
| :---: | :---: | :---: | :---: |
| Welfare, \% | 0.00 | -7.33 | 11.8 |

## Robustness: Changes in the Scale of Means-tested SI

- We have found that households like means-tested SI but what if anything can we say about the optimal scale?
- To see, we consider changing the size of means-tested SI in our baseline economy where SS is of the scale in the U.S.


## Robustness: Changes in the Scale of Means-tested SI

- Whether households want an increase or a decrease depends on how financed.

Tax Adjusting

| U.S. economy | Income | Income | Payroll |
| :--- | :--- | :---: | :---: |
|  | $30 \%$ up | $30 \%$ down | $30 \%$ up |

## Welfare

| Average | -0.44 | 0.04 | 0.54 |
| :--- | :--- | :--- | :--- |

By household education type (female, male):
high school, high school high school, college college, high school college, college

| -0.24 | -0.13 | 0.62 |
| :--- | :--- | :--- |
| -0.91 | 0.45 | 0.35 |
| -0.69 | 0.28 | 0.48 |
| -1.20 | 0.65 | 0.29 |

Means-tested SI
take-up rates
govt. outlays, \% GNP
12.9
0.75
24.1
6.0
23.7

| 1.50 | 0.30 | 1.44 |
| :--- | :--- | :--- |

## Robustness: Changes in the Scale of Means-tested SI

- Feldstein (1986) argues that if the scale of means-tested SI is small enough, individuals, especially the poor, will prefer SS.
- To evaluate this claim, we experiment with adding SS to economies with different consumption floors.
- We find:
- The floors have to be extremely low, $\approx \$ 5$ a year, for individuals to obtain small welfare gains from SS.
- If medical expenses are zero, there is no floor that will make SS preferred.


## Robustness: To Modeling Assumptions

- Foreseeing death and open economy
- Our results are robust to these two assumptions.
- We do not change the scale of Medicare
- exogenous medical expenses
- private insurance markets


## Robustness: To Modeling Assumptions

- Foreseeing death and open economy
- We do not change the scale of Medicare
- Since Medicare is a PAYG benefit program our conjecture is that, like SS, newborns would prefer an economy without it.
- Exogenous medical expenses
- Abstract from private insurance markets


## Robustness: To Modeling Assumptions

- Foreseeing death and open economy
- We do not change the scale of Medicare
- Exogenous medical expenses
- Modeling the market for medical care would be a significant extension of our model.
- Abstract from private insurance markets


## Robustness: To Modeling Assumptions

- Foreseeing death and open economy
- We do not change the scale of Medicare
- Exogenous medical expenses
- Abstract from private insurance markets
- There are significant supply-sides problems in some of these markets.
- Moreover, every society has to deal with the fact that some people will end up old, sick, alone and poor.


## Additional Impoverishment Transitions

- Poor health is associated with higher probabilities and persistence of impoverishment.


## Percentage of Retirees Moving from Each Quintile to Quintile 1

|  | $65-74$ Year-olds |  | $75-84$ Year-olds |  | $85+$ Year-olds |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Quintile | Healthy | Unhealthy | Healthy | Unhealthy | Healthy | Unhealthy |
| 1 | 69.7 | 80.9 | 70.8 | 79.3 | 67.8 | 73.1 |
| 2 | 15.6 | 22.6 | 15.1 | 22.1 | 17.7 | 27.5 |
| 3 | 3.4 | 5.5 | 3.8 | 7.2 | 7.8 | 8.2 |
| 4 | 0.9 | 2.2 | 1.3 | 4.1 | 4.1 | 4.7 |
| 5 | 0.4 | 1.5 | 0.5 | 1.3 | 1.4 | 2.8 |

Source: Authors' calculations using 1992-2010 HRS data on retirees 65+.

## Additional Impoverishment Transitions

- Hospital stays are associated with higher probabilities and persistence of impoverishment.


## Percentage of Retirees Moving from Each Quintile to Quintile 1

|  | $65-74$ Year-olds |  | $75-84$ Year-olds |  | $85+$ Year-olds |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Quintile | None | Hospital Stay | None | Hospital Stay | None | Hospital Stay |
| 1 | 75.3 | 79.0 | 73.1 | 78.8 | 71.0 | 70.8 |
| 2 | 18.1 | 18.9 | 16.9 | 18.2 | 20.9 | 22.9 |
| 3 | 3.6 | 5.1 | 3.8 | 6.6 | 7.8 | 7.7 |
| 4 | 0.9 | 1.6 | 1.7 | 2.5 | 4.0 | 4.3 |
| 5 | 0.6 | 0.4 | 0.6 | 0.6 | 2.2 | 1.3 |

Source: Authors' calculations using 1992-2010 HRS data on retirees 65+.

## Additional Impoverishment Transitions

- Widowhood is associated with higher probabilities and persistence of impoverishment.

Percentage of Retired Women Moving from Each Quintile to Quintile 1

|  | $65-74$ Year-olds |  | $75-84$ Year-olds |  | $85+$ Year-olds |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Quintile | Married | Widowed | Married | Widowed | Married | Widowed |
| 1 | 72.5 | 80.0 | 69.6 | 75.9 | 80.2 | 76.1 |
| 2 | 17.3 | 22.9 | 17.2 | 20.6 | 28.1 | 28.0 |
| 3 | 3.4 | 6.5 | 4.4 | 6.9 | 8.1 | 11.5 |
| 4 | 1.0 | 1.6 | 1.1 | 2.4 | 3.7 | 6.2 |
| 5 | 0.4 | 1.1 | 0.3 | 0.5 | 2.6 | 2.8 |

Source: Authors' calculations using 1992-2010 HRS data on retirees 65+.

- Men look very similar.


## Additional Impoverishment Transitions

- Widowhood is associated with higher probabilities and persistence of impoverishment.

Percentage of Retired Men Moving from Each Quintile to Quintile 1

|  | $65-74$ Year-olds |  | $75-84$ Year-olds |  | $85+$ Year-olds |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Quintile | Married | Widowed | Married | Widowed | Married | Widowed |
| 1 | 74.5 | 75.7 | 73.9 | 79.0 | 70.7 | 73.9 |
| 2 | 18.3 | 24.1 | 17.4 | 18.8 | 15.0 | 19.2 |
| 3 | 3.9 | 12.2 | 3.5 | 9.6 | 4.6 | 8.1 |
| 4 | 1.3 | 3.5 | 2.0 | 2.0 | 4.1 | 4.3 |
| 5 | 0.7 | 1.7 | 0.9 | 1.8 | 0.0 | 4.0 |

Source: Authors' calculations using 1992-2010 HRS data on retirees 65+.

## Working Household's Problem

Working-age household solves
$V\left(j, a, \overline{\mathbf{e}}, \varepsilon_{e}, \mathbf{s}\right)=\max _{c, l_{f}, a^{\prime}}\left\{U^{W}\left(c, l_{f}, \mathbf{s}\right)+\beta E\left[V\left(j+1, a^{\prime}, \overline{\mathbf{e}}^{\prime}, \varepsilon_{e}^{\prime}, \mathbf{s}\right) \mid \varepsilon_{e}\right]\right\}$
subject to ...

| age | $\mathfrak{j}$ |
| :--- | :--- |
| assets | $\mathfrak{a}$ |
| average earnings | $\overline{\mathbf{e}} \equiv\left\{\bar{e}^{m}, \bar{e}^{f}\right\}$ |
| productivity shocks | $\varepsilon_{\boldsymbol{e}} \equiv\left\{\varepsilon_{e}^{m}, \varepsilon_{e}^{f}\right\}$ |
| education types | $\mathbf{s} \equiv\left\{s^{m}, s^{\mathrm{f}}\right\}$ |

## Working Household's Problem

Working-age household solves

$$
V\left(j, a, \overline{\mathbf{e}}, \varepsilon_{e}, \mathbf{s}\right)=\max _{c, l_{f}, a^{\prime}}\left\{U\left(c, l_{f}, \mathbf{s}\right)+\beta E\left[V\left(j+1, a^{\prime}, \overline{\mathbf{e}}^{\prime}, \varepsilon_{e}^{\prime}, s\right) \mid \varepsilon_{e}\right]\right\}
$$

subject to

$$
\begin{aligned}
& c \geqslant 0, \quad 0 \leqslant l_{f} \leqslant 1, \quad a^{\prime} \geqslant 0, \\
& e^{-i}=\left(e^{i}+j \bar{e}^{-i}\right) /(j+1), \quad i \in\{m, f\}, \\
& c+a^{\prime}=a+y^{W}-T_{y}^{W}+\operatorname{Tr}^{W}, \\
& y^{W} \equiv e^{m}+e^{f}+\left(1-\tau_{c}\right) r a, \\
& e^{i} \equiv w \Omega^{i}\left(j, \varepsilon_{e}, s^{i}\right)\left(1-l_{f} \mathbf{I}_{i=f}\right), \quad i \in\{m, f\}, \\
& T_{y}^{W} \equiv \tau_{y}\left(y^{W}-\tau_{e}\left(e^{m}\right) e^{m}-\tau_{e}\left(e^{f}\right) e^{f}\right)+\tau_{e}\left(e^{m}\right) e^{m}+\tau_{e}\left(e^{f}\right) e^{f}, \\
& \operatorname{Tr}^{W} \equiv \max \left\{0, \underline{c}-\left[a+y^{W}-T_{y}^{W}\right]\right\} .
\end{aligned}
$$

## Utility Functions

- Utility of a working-age household is

$$
u^{W}\left(c, l_{f}, s\right)=2 \frac{(c /(1+\chi))^{1-\sigma}}{1-\sigma}+\psi(\mathbf{s}) \frac{l_{f}^{1-\gamma}}{1-\gamma}-\phi(s) \mathbf{I}\left(l_{f}<1\right)
$$

where $1-\chi \in[0,1]$ is the degree of joint consumption.

- Utility of a retired household is

$$
u^{\mathrm{R}}(\mathrm{c}, \mathrm{~d})=2^{\mathrm{N}-1} \frac{\left(\mathrm{c} /(1+\chi)^{\mathrm{N}-1}\right)^{1-\sigma}}{1-\sigma}+\psi^{\mathrm{R}} \frac{l_{f}^{1-\gamma}}{1-\gamma}
$$

where the number of household members N depends on d.

## Competitive Equilibrium

## We consider a steady-state competitive equilibrium of a small open economy.

Given a fiscal policy and a real interest rate $r$ in equilibrium

1. Individuals optimize
2. Firms maximize profits
3. Markets for goods and labor clear
4. Consistency conditions hold
5. Transfers to newborns equal accidental bequests
6. SS Benefits = SS Payroll Tax Revenue
7. GovtExp is such that:

IncomeTaxes + MedicareTaxes + CorporateTaxes $=$ Transfers + GovtExp


[^0]:    Source: Authors' calculations using 1992-2010 HRS data on retirees 65+.

