

# On the optimal design of a Financial Stability Fund

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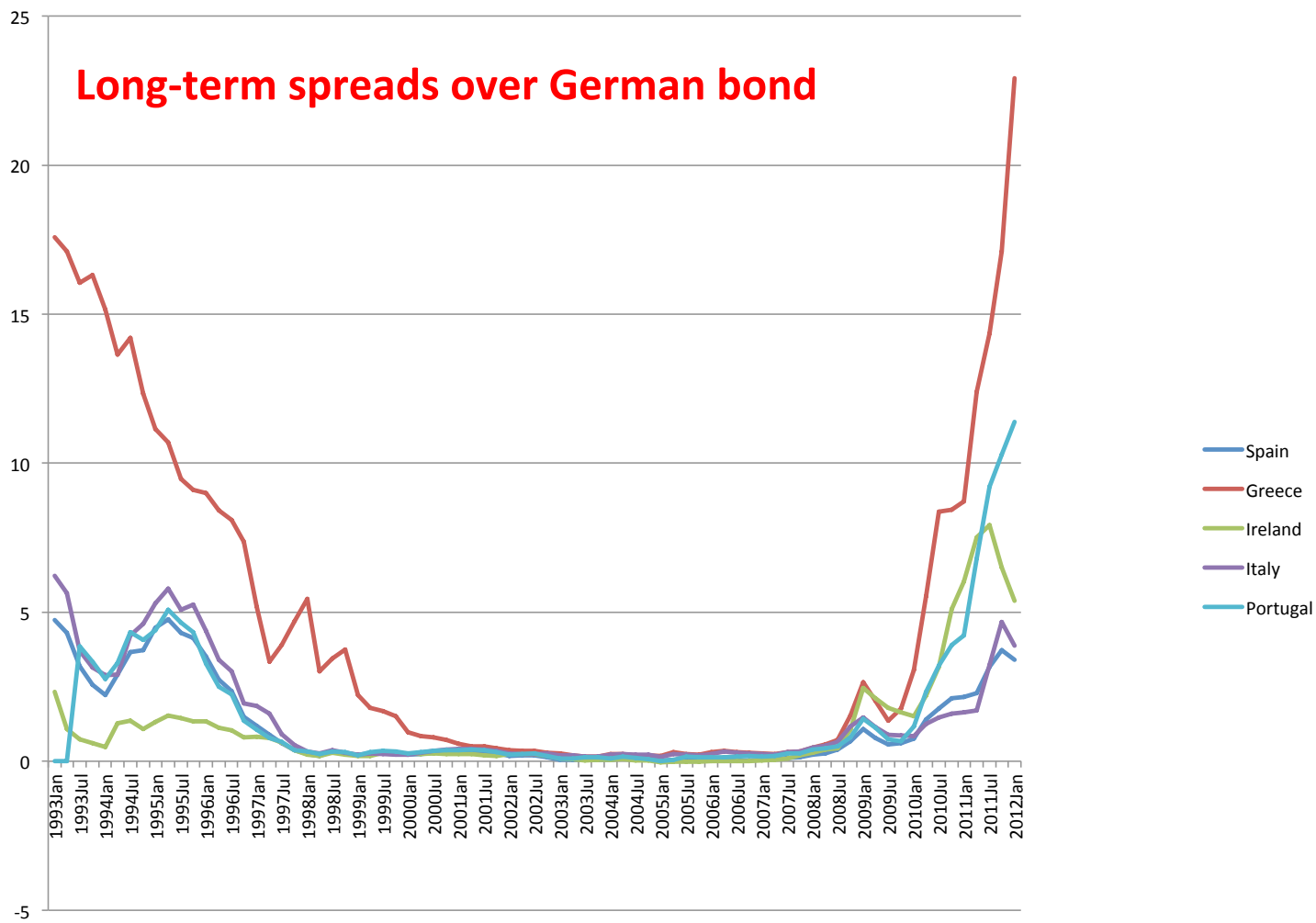
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# Will the Euro Zone Go Up In Smoke?

(Newsweek Magazine, May 21, 2012)

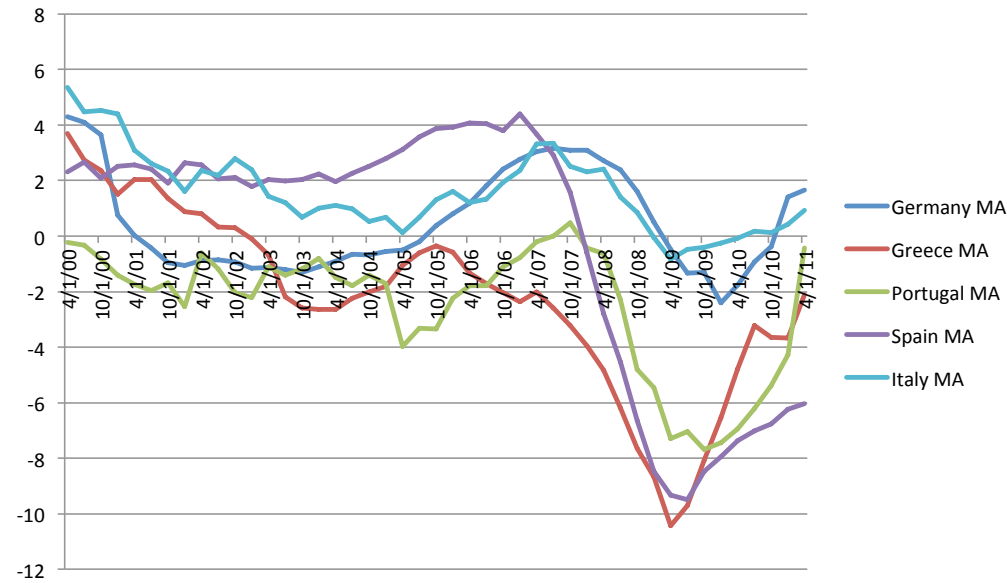




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## Primary deficit & surplus /GDP

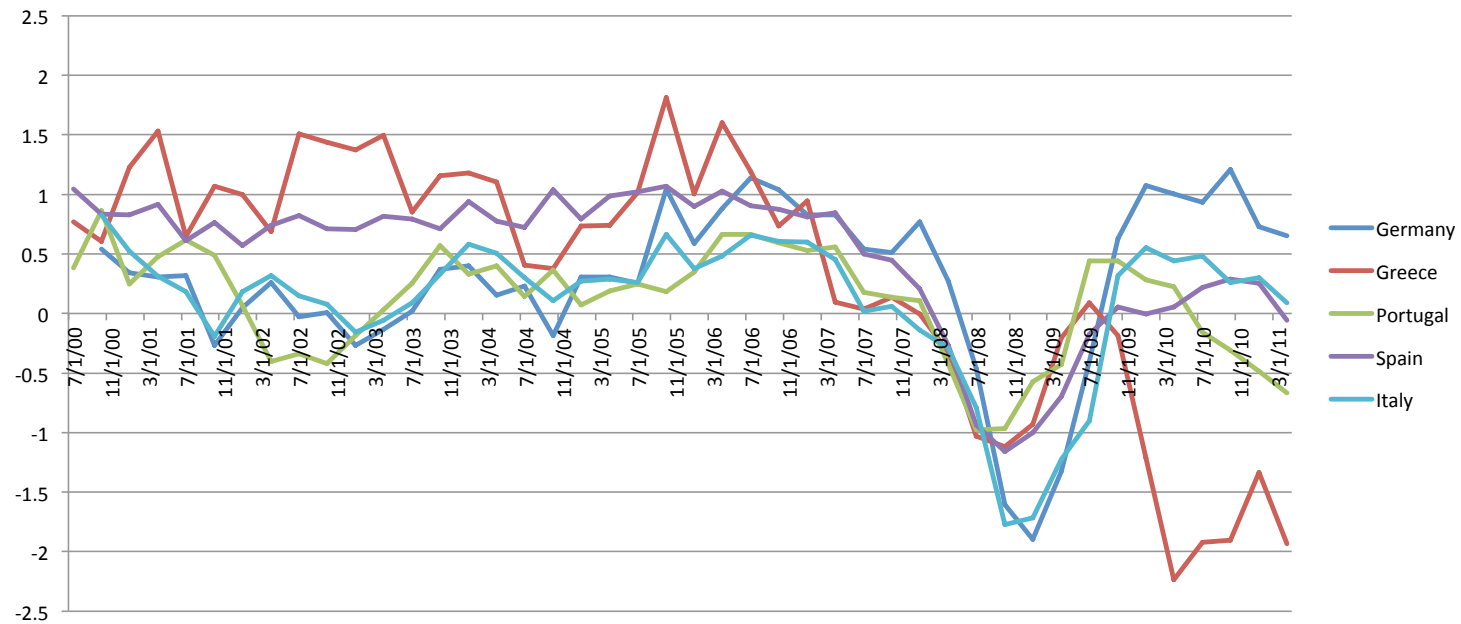
(MA 2000Q2 – 2011Q2 source ECB)



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# Not just a RBC recession?

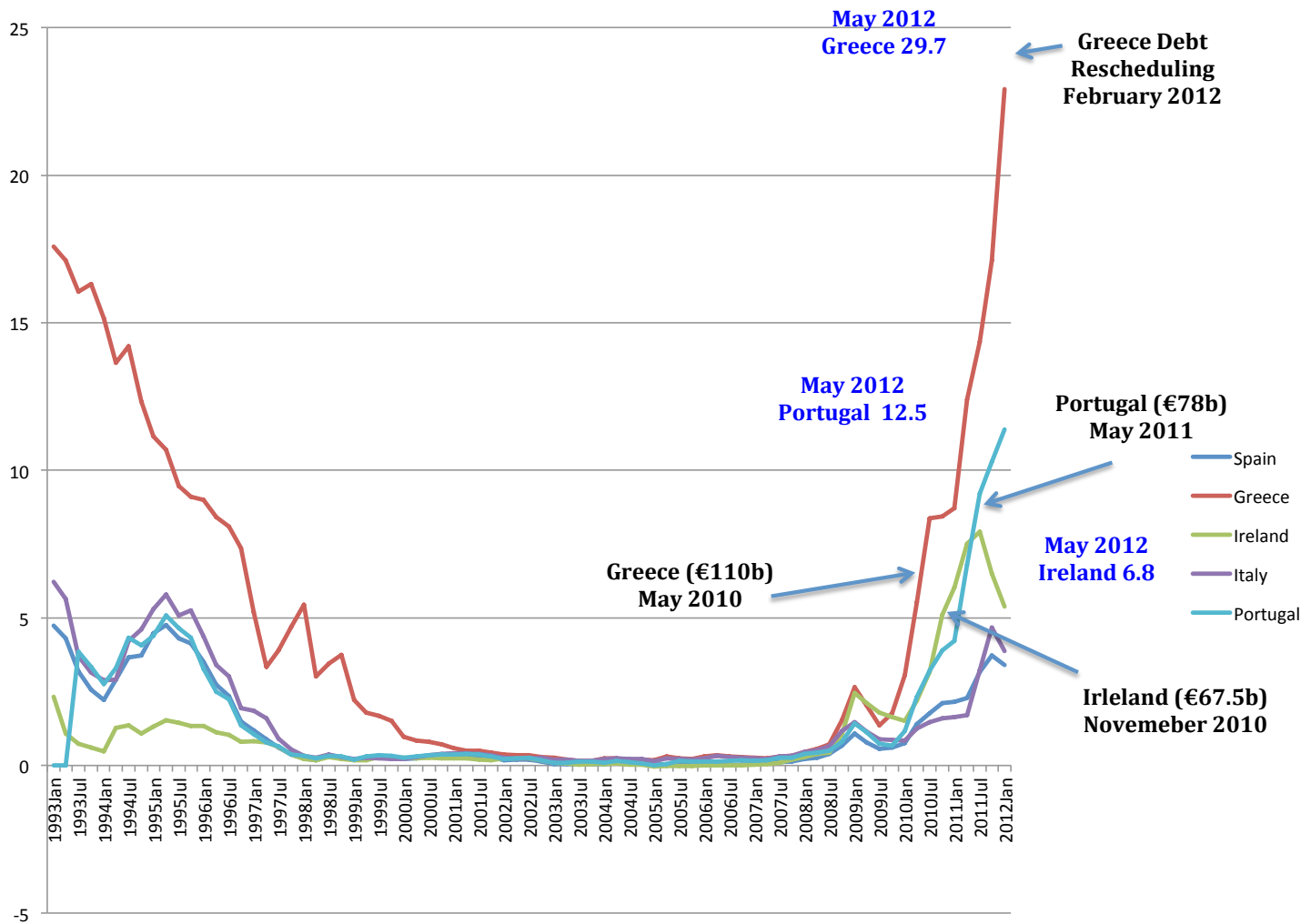
## GDP Growth rates (2000Q3 - 2011Q2)



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## The Euro policy responses

- Maintain ECB mandate of price stability
  - The indebted Euro countries keep using debt-financing (with very costly roll-overs)
  - In spite of the "no-bailout clause" in the EU Treaty (Art. 125), a country's default is perceived catastrophic (bail-out, or partial-bailout expectations)
  - Rescue packages with IMF: Greece, Ireland and Portugal  
IMF style: conditional (austerity) financial support (with Greece reschedule)
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**Long-term spreads over German bond**

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## The Euro policy responses

- In spite of the "monetary financing prohibition" (Art. 123), large ECB debt purchase interventions (Italy and Spain, not Greece 2011-12, Spain again?)
  - The **European Fiscal Compact** (2 March, 2012) setting deficit constraints in State constitutions (similar to US States)
  - The creation of the **European Stability Mechanism** as a *Financial Stability Fund*; starts July 2012 !
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## The Euro policy responses

- Could have we done better?
  - Can we do better?
  - Will we learn?
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## ***A Financial Stability Fund as a Dynamic Mechanism Design problem***

- The finance theories on the 'optimality of the debt contract' do not apply to the long-term relationship of countries in an Economic Union.
  - Long-term contracts can provide risk-sharing and enhance investment opportunities.
  - A *FSF* can either use only its own financial resources, or act as a *maturity transformation* facility, transforming non-contingent loans (from international markets, Central Banks, or households) into *contingent* loans to participants in the *FSF*.
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## ***A Financial Stability Fund as a Dynamic Mechanism Design problem***

- However, a well designed *FSF* must take into account:

**The redistribution, or Hayek's, problem:** the *participation constraints* of all the *FSF* members (and the *FSF* as lender)

**The moral hazard problem:** the *incentive compatibility constraints* (not accounted for in this version)



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## The environment

- One risk-averse government-borrower & one risk-neutral fund-lender
  - Lender: at the risk-free rate  $r$
  - Borrower's technology: leisure,  $l = 1 - n$  & output,  $y = \theta f(n)$
  - Borrower's preferences:  $u(c) + U(1 - n)$  &  $\beta$ ,  $1/(1 + r) \geq \beta$
  - Markovian shocks: productivity,  $\theta$  & government expenditure,  $G$ ; i.e. an exogenous state  $s = (\theta, G)$ , with transition probability  $\pi(s'|s)$ .
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## Alternative borrowing & lending mechanisms

- *Complete markets* with full commitment ( $FB$ )
  - *Incomplete markets* with & without default, ( $IMD$ ) & ( $IM$ )
  - *Financial Stability Fund* ( $FSF$ ) with one-sided ( $1S$ ) & two-sided limited commitment ( $2S$ )
  - How would an  $IMD$  look if, with the same shocks, had a  $2S - FSF$ ? (Greece with a proper  $ESM$ ?)
  - How much would it gain?
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## *Incomplete markets without default*

$b$  = asset holdings at the beginning of the period (if  $b < 0$  we call it debt)

$$V^{bi}(b, \theta, G) = \max_{c, n, b'} \{u(c) + U(1 - n) + \beta E [V^{bi}(b', \theta', G') \mid \theta, G]\}$$

$$\text{s.t. } c + G + qb' \leq \theta f(n) + b$$

- Resulting in policies:  $c^i(b, \theta, G)$ ,  $n^i(b, \theta, G)$  and  $b'^i(b, \theta, G)$
  - Since the lender is risk neutral:  $q = \frac{1}{1+r}$
  - Notice there is an implicit no default technology.
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## *Incomplete markets with default.*

Following Arellano (2008), if the country does not default on its debt, the value of  $b$  at  $(\theta, G)$  is

$$V^{bid}(b, \theta, G) = \max_{c, n, b'} \{u(c) + U(1 - n) + \beta E [V^{bia}(b', \theta', G') \mid \theta, G]\}$$

s.t.  $c + G + q(\theta, G, b')b' \leq \theta f(n)$ ,

where, taking into account that default can occur next period,

$$V^{bia}(b, \theta, G) = \max\{V^{bid}(b, \theta, G), V^{ai}(b, \theta, G)\}$$

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## *Incomplete markets with default.*

- The value in autarky is given by

$$V^{ai}(\theta, G) = \max_n \{ u((\theta f(n) - G) + U(1 - n)) \\ + \beta E [(1 - \lambda) V^{ai}(\theta', G') + \lambda V^{bid}(0, \theta', G') \mid \theta, G] \}$$

- After default a government is in autarky, but can be re-enter the financial (incomplete) market with probability  $\lambda$ ;  $\lambda$  small.
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## *Incomplete markets with default*

- The choice of default:

$$D(\theta, G, b) = 1 \text{ if } V^{ai}(\theta, G) > V^{bid}(b, \theta, G) \text{ and } 0 \text{ otherwise,}$$

- The price of new debt:  $q(\theta, G, b') = \frac{1-d(\theta, G, b')}{1+r}$
  - The expected default rate:  $d(\theta, G, b') = \mathbb{E}[D(\theta, G, b') \mid \theta, G]$
  - The debt interest rate:  $r^i(\theta, G, b') = 1/q(\theta, G, b') - 1$
  - The spread:  $r^i(\theta, G, b') - r \geq 0$
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## *Incomplete markets accounting*

- **Primary surplus** (we also call it **transfers**,  $\tau$ , and **primary deficit** if negative)

$$qb' - b = \theta f(n) - (c + G) \text{ and, with default,}$$
$$q(\theta, G, b')b' - b = \theta f(n) - (c + G)$$

- **Surplus** = primary surplus + interest **repayment** (end of the period)

$$b' - b = (qb' - b) + qb'(1/q - 1)$$
$$= qb'(1 + r) - b \text{ and, with default,}$$
$$b' - b = q(\theta, G, b')b'(1 + r^i(\theta, G, b')) - b$$

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## The *Financial Stability Fund* as a long-term contract

$$\begin{aligned} & \max_{\{c(s^t), n(s^t)\}} \mathbb{E} \left[ \mu_{b,0} \sum_{t=0}^{\infty} \beta^t \left[ u(c(s^t)) + U(1 - n(s^t)) \right] \right. \\ & \quad \left. + \mu_{l,0} \sum_{t=0}^{\infty} \left( \frac{1}{1+r} \right)^t \tau(s^t) \mid s_0 \right] \\ \text{s.t.} \quad & \mathbb{E} \left[ \sum_{r=t}^{\infty} \beta^{r-t} \left[ u(c(s^r)) + U(1 - n(s^r)) \right] \mid s^t \right] \geq V^{af}(s_t) \\ & \mathbb{E} \left[ \sum_{r=t}^{\infty} \left( \frac{1}{1+r} \right)^{r-t} \tau(s^r) \mid s^t \right] \geq Z, \\ \text{and} \quad & \tau(s^t) = \theta(s^t) f(n(s^t)) - c(s^t) - G(s^t), \quad t \geq 0. \end{aligned}$$

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## The *Financial Stability Fund* as a long-term contract

- $V^{af}(s_t)$ , is defined as  $V^{ai}(s_t)$ , except that  $\lambda$  is, in this case, the probability of returning to the fund with  $b = 0$ .
  - $Z \leq 0$  is the outside value of the lender.
  - The solution to the *FSF* maximization problem is:
    - FB** A **first best contract**, when  $V^{af}(s_t)$  and  $Z$  are never binding, for  $t > 0$ .
    - 1S** A **one-sided limited enforcement contract**, when only  $Z$  is never binding, for  $t > 0$ .
    - 2S** A **two-sided limited enforcement contract**, when both participation constraints may bind, for  $t > 0$ .
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## The *Financial Stability Fund* as a long-term contract

Following Marcet & Marimon (1999, 2011), we can write the *FSF* contracting problem as:

$$\min_{\{\gamma_{b,t}, \gamma_{l,t}\}} \max_{\{c_t, n_t\}} \mathbb{E} \left[ \sum_{t=0}^{\infty} \beta^t \left( \mu_{b,t+1} [u(c_t) + U(1 - n_t)] - \gamma_{b,t} V^A(s_t) \right) + \sum_{t=0}^{\infty} \left( \frac{1}{1+r} \right)^t (\mu_{l,t+1} \tau_t - \gamma_{l,t} Z) \mid s_0 \right]$$

$$\mu_{i,t+1}(s^{t+1}) = \mu_{i,t}(s^t) + \gamma_{i,t}(s^t), \mu_{i,0}(s_0) \text{ is given, for } i = b, l,$$

$\gamma_{i,t}(s^t)$  is the Lagrange multiplier of the participation constraint of agent  $i$  in period  $t$ , state  $s^t$ ,

$\mu_{i,0}(s_0)$ ,  $i = b, l$ , is determined by the lender's *zero profit condition*.

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## The *Financial Stability Fund* as a long-term contract

Following Kehoe and Perri (2002), we can use as co-state variable  $x_t = \frac{\mu_{l,t}}{\mu_{b,t}\eta}$ , where  $\eta \equiv \beta(1+r) \leq 1$ , and  $v_i(x, s) = \gamma_i(x, s) / \mu_i(x, s)$ ,  $i = b, l..$

Resulting in policy functions  $c(x, s), n(x, s), \tau(x, s)$  and  $v_b(x, s), v_l(x, s)$ , satisfying

$$u'(c(x, s)) = x' = \frac{1 + v_l(x, s)x}{1 + v_b(x, s)\eta},$$

and

$$\frac{U'(1 - n(x, s))}{u'(c(x, s))} = \theta f'(n(x, s)).$$

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## The *Financial Stability Fund* as a long-term contract

The value function of the *FSF* contracting problem takes the form:

$$FV(x, s) = xV^{lf}(x, s) + V^{bf}(x, s); \text{ where,}$$

$$V^{bf}(x, s) = u(c(x, s)) + U(1 - n(x, s)) + \beta \mathbf{E} [V^{bf}(x', s') | s]$$

and

$$V^{lf}(x, s) = \tau(x, s) + \frac{1}{1+r} \mathbf{E} [V^{lf}(x', s') | s]$$

Furthermore,  $V^{bf}(x, s) \geq V^{af}(s)$ , with equality if  $v_b(x, s) > 0$  and, similarly,  $V^{lf}(x, s) \geq Z$  if  $v_l(x, s) > 0$ .

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## Decentralizing the *FSF* contract

Following Alvarez and Jermann (2000), we can find competitive prices to value *FSF* contracts and compare them with the *IM* and *IMD* contracts.

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## The dual competitive economy

Let the borrower have access to a complete set of one-period Arrow securities...

$$\begin{aligned} & \max_{\{c_b(s^t), n(s^t), a_b(s^{t+1})\}} \sum_{t=0} \sum_{s^t} \beta^t \pi(s^t) \left[ u(c_b(s^t)) + U(1 - n(s^t)) \right] \\ \text{s.t. } & c_b(s^t) + \sum_{s^{t+1}|s^t} q(s^{t+1}|s^t) a_b(s^{t+1}) = \theta(s^t) f(n(s^t)) - G(s^t) + a_b(s^t) \\ & a_b(s^{t+1}) \geq A_b(s^{t+1}) \end{aligned}$$

- $q(s^{t+1}|s^t)$  is the price of the one-period state contingent
  - $a_b(s^{t+1})$  are the asset (contingent claims) holdings
  - $A_b(s^{t+1})$  is an endogenous borrowing limit
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## The dual competitive economy

The borrower's choice satisfies

$$q(s^{t+1}|s^t) \geq \beta^t \pi(s^{t+1}|s^t) \frac{u'(c_b(s^{t+1}))}{u'(c_b(s^t))}$$

with equality if  $a_b(s^{t+1}) > A_b(s^{t+1})$ , as well as the present-value budget constraint.

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## The dual competitive economy

Similarly, let the lender have access to a complete set of Arrow securities...

$$\begin{aligned} & \max_{\{c_l(s^t), a_l(s^{t+1})\}} \sum_{t=0} \sum_{s^t} \left( \frac{1}{1+r} \right)^t \pi(s^t) c_l(s^t) \\ \text{s.t. } & c_l(s^t) + \sum_{s^{t+1}|s^t} q(s^{t+1}|s^t) a_l(s^{t+1}) = a_l(s^t) \\ & a_l(s^{t+1}) \geq A_l(s^{t+1}) \end{aligned}$$

The lender's choice satisfies, with equality if  $a_l(s^{t+1}) > A_l(s^{t+1})$ ,

$$q(s^{t+1}|s^t) \geq \left( \frac{1}{1+r} \right)^t \pi(s^{t+1}|s^t)$$

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## The dual competitive economy

The values for the borrower and the lender have a recursive form

$$W^b(a_b(s^t), s^t) = u(c_b(s^t)) + U(1 - n(s^t)) + \beta \sum_{s^{t+1}|s^t} \pi(s_{t+1}|s_t) W^b(a_b(s^{t+1}), s^{t+1})$$

$$W^l(a_l(s^t), s^t) = c_l(s^t) + \frac{1}{1+r} \sum_{s^{t+1}|s^t} \pi(s_{t+1}|s_t) W^l(a_l(s^{t+1}), s^{t+1})$$

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## The decentralized *FSF* contract

Let  $\{c^*(s^t), n^*(s^t), \tau^*(s^t)\}$  be the allocation of a *FSF* contract...

$$\begin{aligned} q^*(s^{t+1}|s^t) &= \max \left\{ \beta \pi(s_{t+1}|s_t) \frac{u'(c^*(s^{t+1}))}{u'(c^*(s^t))}, \left( \frac{1}{1+r} \right) \pi(s^{t+1}|s^t) \right\} \\ &= \max \left\{ \beta \pi(s_{t+1}|s_t) \frac{1 + v_l(x_{t+1}, s_{t+1})}{(1 + v_b(x_{t+1}, s_{t+1}))\eta}, \left( \frac{1}{1+r} \right) \pi(s_{t+1}|s_t) \right\} \\ &= \left( \frac{1}{1+r} \right) \pi(s_{t+1}|s_t) \max \left\{ \frac{1 + v_l(x_{t+1}, s_{t+1})}{1 + v_b(x_{t+1}, s_{t+1})}, 1 \right\} \end{aligned}$$

If the lender's participation constraint is not binding:  $\frac{1+v_l(x_{t+1}, s_{t+1})}{1+v_b(x_{t+1}, s_{t+1})} \leq 1$ .

The price of a one-period bond:  $q^f(s^t) = \sum_{s^{t+1}|s^t} q^*(s^{t+1}|s^t)$ .

When the lender's participation constraint is binding, for some  $s^{t+1}$ , the spread is negative.

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## The decentralized FSF contract

*asset holdings = present value of transfers*

$$Q^* (s^t | s_0) = q^* (s^1 | s_0) q^* (s^2 | s^1) \dots q^* (s^t | s^{t-1})$$

$$\begin{aligned} a_b (s^t) &= \sum_{n=0}^{\infty} \sum_{s^{t+n} | s^t} Q^* (s^{t+n} | s^t) \left[ c^* (s^{t+n}) - \left( \theta(s^{t+n}) f (n^*(s^{t+n})) - G (s^{t+n}) \right) \right] \\ &= - \sum_{n=0}^{\infty} \sum_{s^{t+n} | s^t} Q^* (s^{t+n} | s^t) \tau^* (s^{t+n}) \end{aligned}$$

$$a_l (s^t) = \sum_{n=0}^{\infty} \sum_{s^{t+n} | s^t} Q^* (s^{t+n} | s^t) c_l (s^{t+n}) = \sum_{n=0}^{\infty} \sum_{s^{t+n} | s^t} Q^* (s^{t+n} | s^t) \tau^* (s^{t+n})$$

$$a_l (s^t) = -a_b (s^t).$$

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## The decentralized FSF contract

Limited enforcement means, here, that the borrowing limits

$$A_b(s^{t+1}) = - \sum_{n=0}^{\infty} \sum_{s^{t+n}|s^t} Q(s^{t+n}|s^t) \left[ \theta(s^{t+n}) f(n^*(s^{t+n})) - G(s^{t+n}) \right]$$

$$A_l(s^{t+1}) \geq Z = \sum_{s^{t+n}|s^t} \left( \frac{1}{1+r} \right)^n (n^*(s^{t+n})),$$

satisfy

$$W^b(A_b(s^t), s^t) = V^{af}(s^t)$$

$$W^l(A_l(s^t), s^t) = Z$$

$\implies$  expected transfers to the lender at the states where his participation constraint are binding can not be negative.

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## The duality between the *FSF* contract and the competitive equilibrium

$$V^{bf}(x, s) = u(c(x, s)) + U(1 - n(x, s)) + \beta \sum_{s'} \pi(s'|s) V^{bf}(x', s')$$

$$V^{lf}(x, s) = \tau(x, s) + \frac{1}{1+r} \sum_{s'} \pi(s'|s) V^{lf}(x', s').$$

$$W^{bf}(a_b, s) = u(c_b(a_b, s)) + U(1 - n(a_b, s)) + \beta \sum_{s'} \pi(s'|s) W^{bf}(a'_b, s')$$

$$W^{lf}(a_l, s) = c_l(a_l, s) + \frac{1}{1+r} \sum_{s'} \pi(s'|s) W^{lf}(a'_l, s'),$$

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## *FSF* accounting

- **Primary surplus** (we also call it **transfers**,  $\tau$ , and **primary deficit** if negative)

$$\sum_{s'|s} q(s'|s) a_b(s') - a_b(s) = c_l(a_l, s) = \tau(x, s)$$

- **Surplus** = primary surplus + interest **repayment** (end of the period)

$$\begin{aligned} a_b(s') - a_b(s) &= \left[ \sum_{s'|s} q(s'|s) a_b(s') - a_b(s) \right] \\ &+ \left[ a_b(s') - \sum_{s'|s} q(s'|s) a_b(s') \right] \end{aligned}$$

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## Contrasting *debt contracts* and *FSF contracts*

$$\log(c) + \frac{\gamma(1-n)^{1-\sigma}}{1-\sigma},$$

with  $\sigma = 2$ ,  $\gamma = 1$

$$f(n) = n^\alpha, \text{ with } \alpha = 0.67.$$

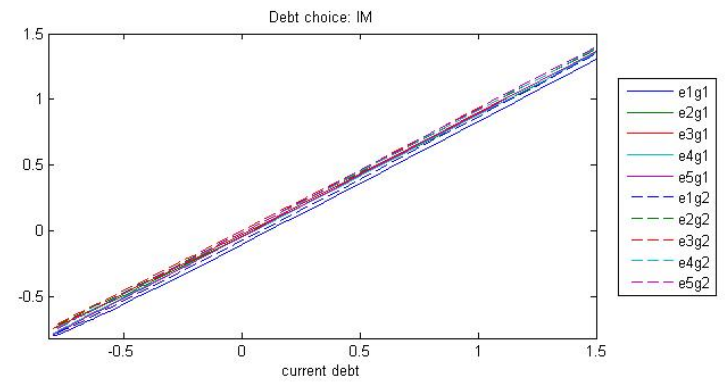
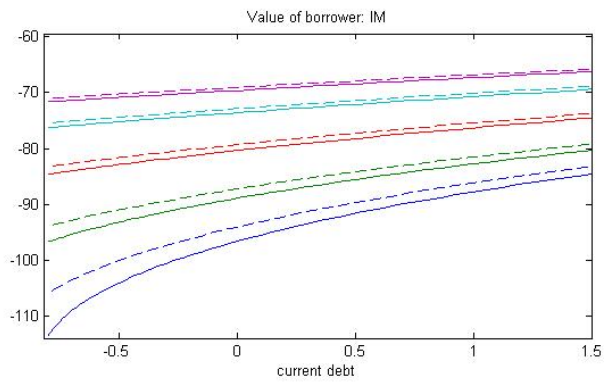
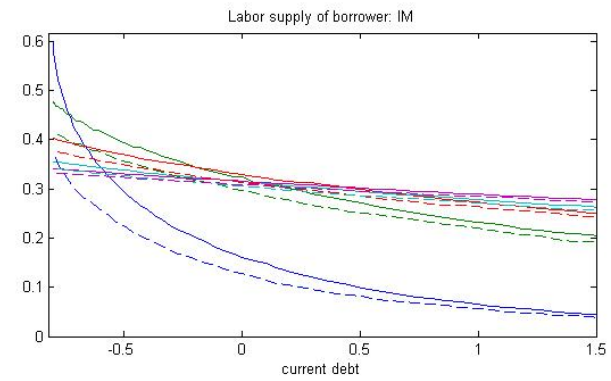
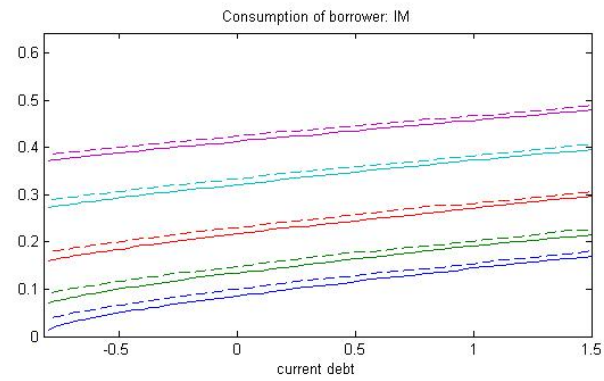
- Borrower's discount factor  $\beta = 0.96$ , while  $r = 0.01$ ;  
i.e.  $1/(1+r) = 0.9901$  and  $\eta = 0.9696$
  - The probability of returning to the market, or fund, after default is  $\lambda = 0.0$
  - In the two-sided limited enforcement contract (2S),  $Z = -0.8$
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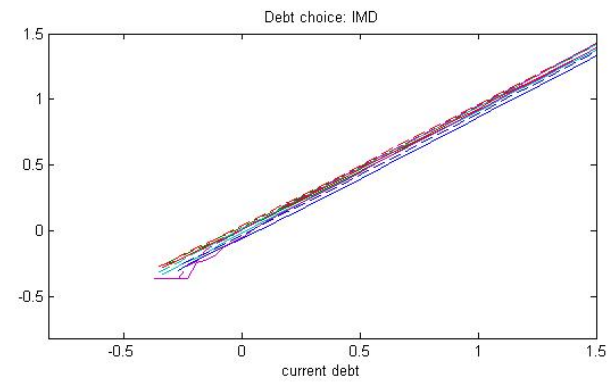
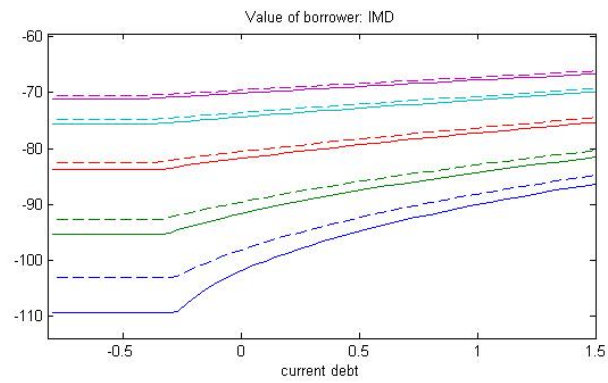
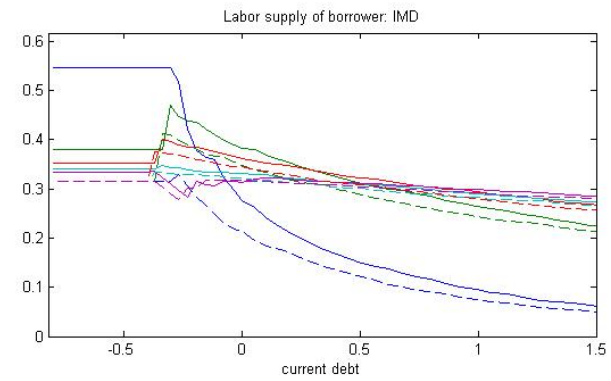
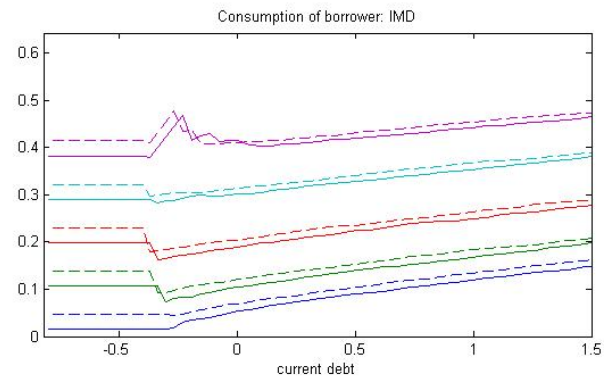
**Contrasting *debt contracts* and *FSF contracts*:**  
**POLICIES**

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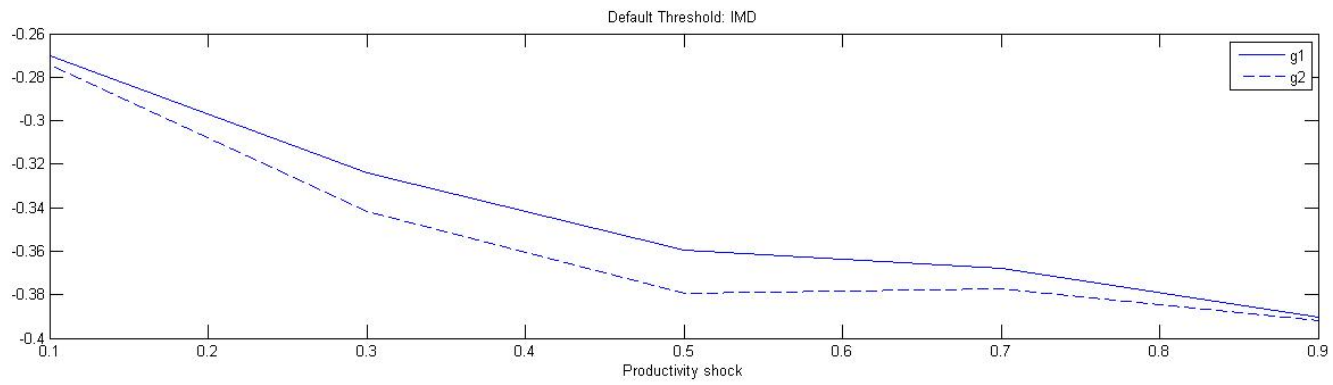
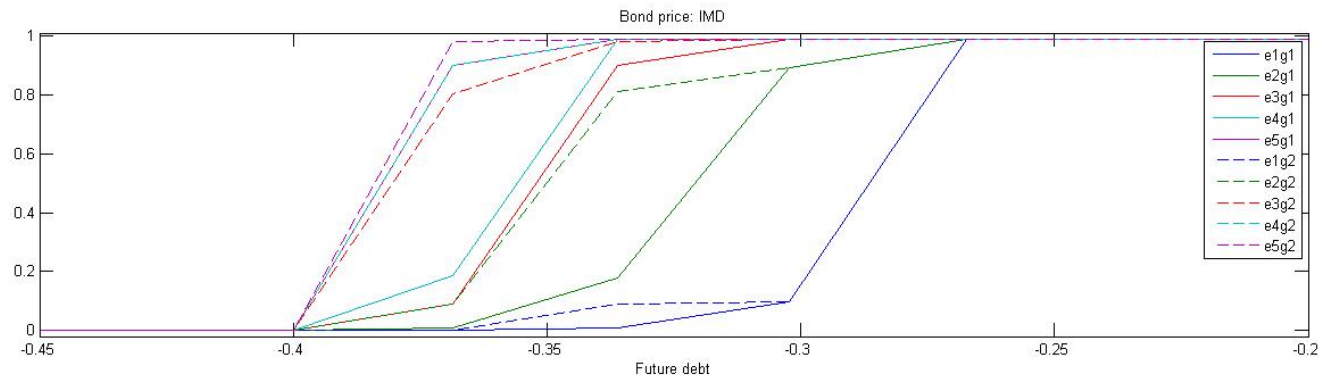


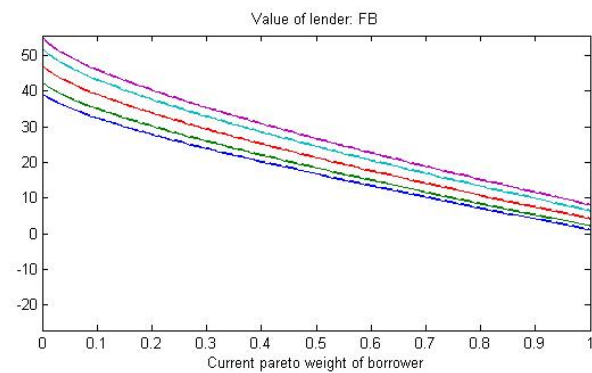
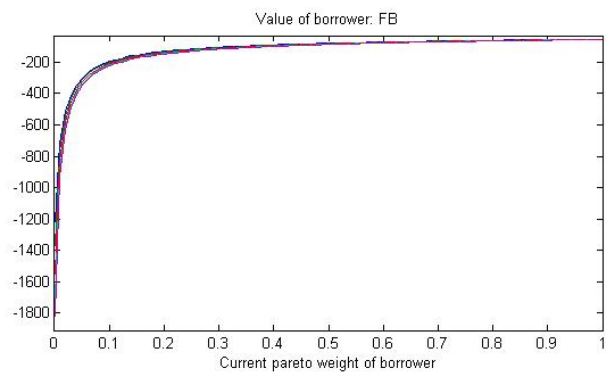
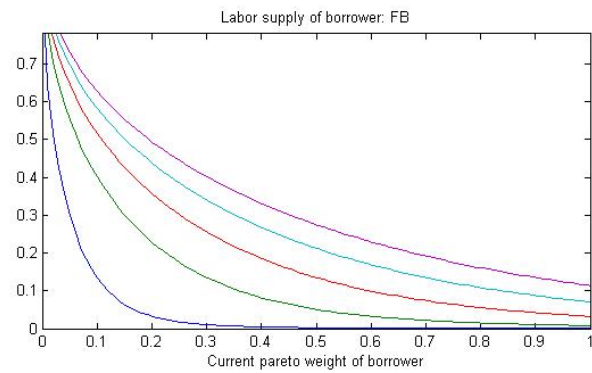
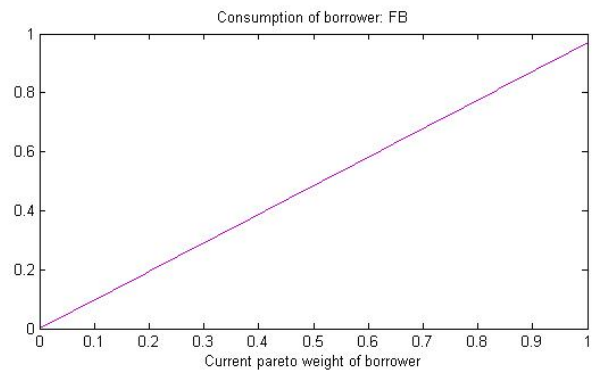
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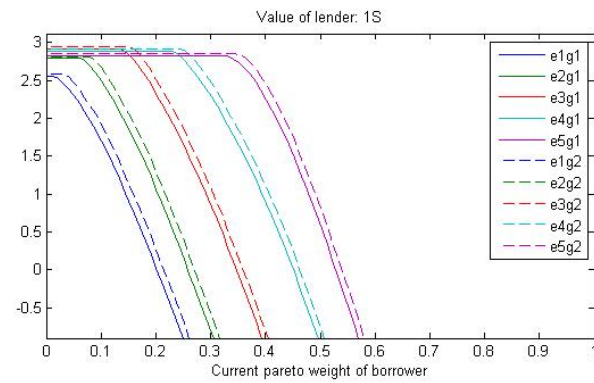
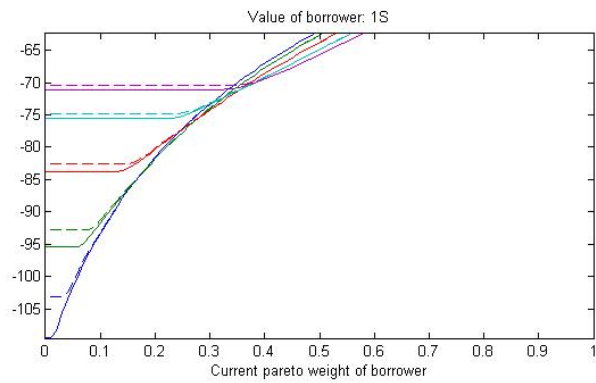
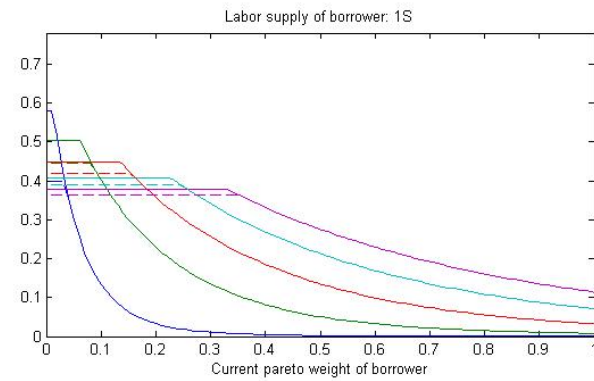
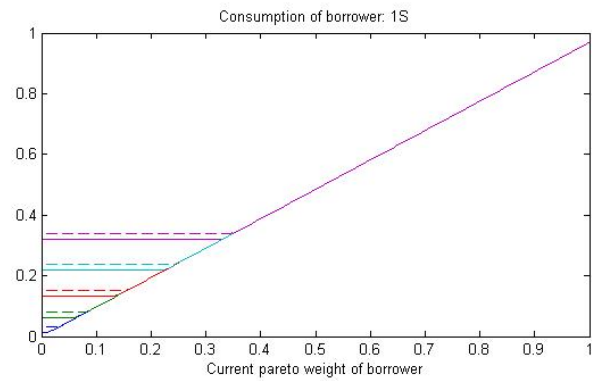
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- e4g2
- e5g2

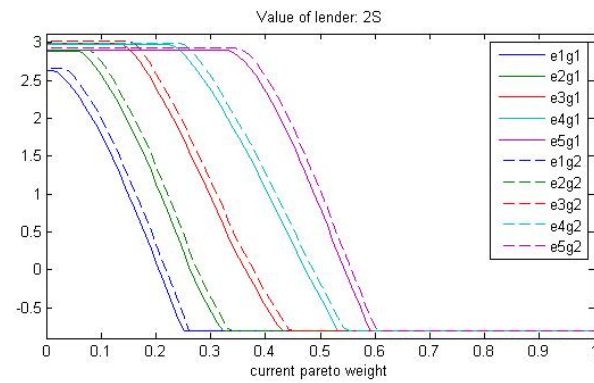
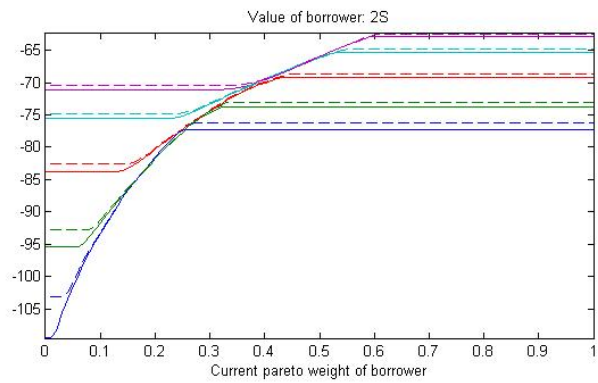
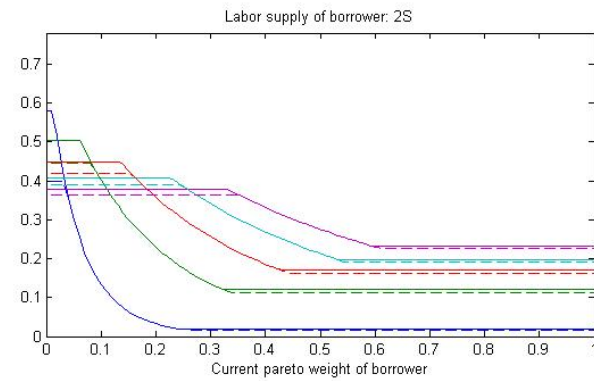
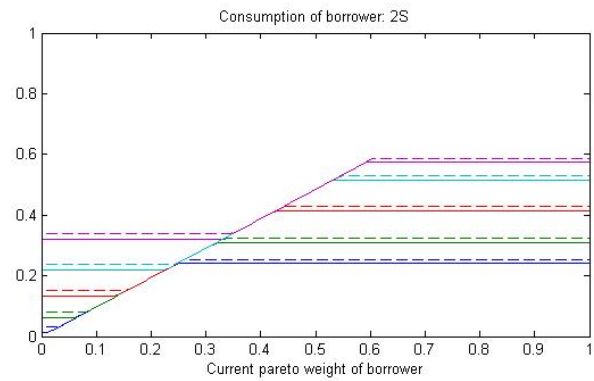


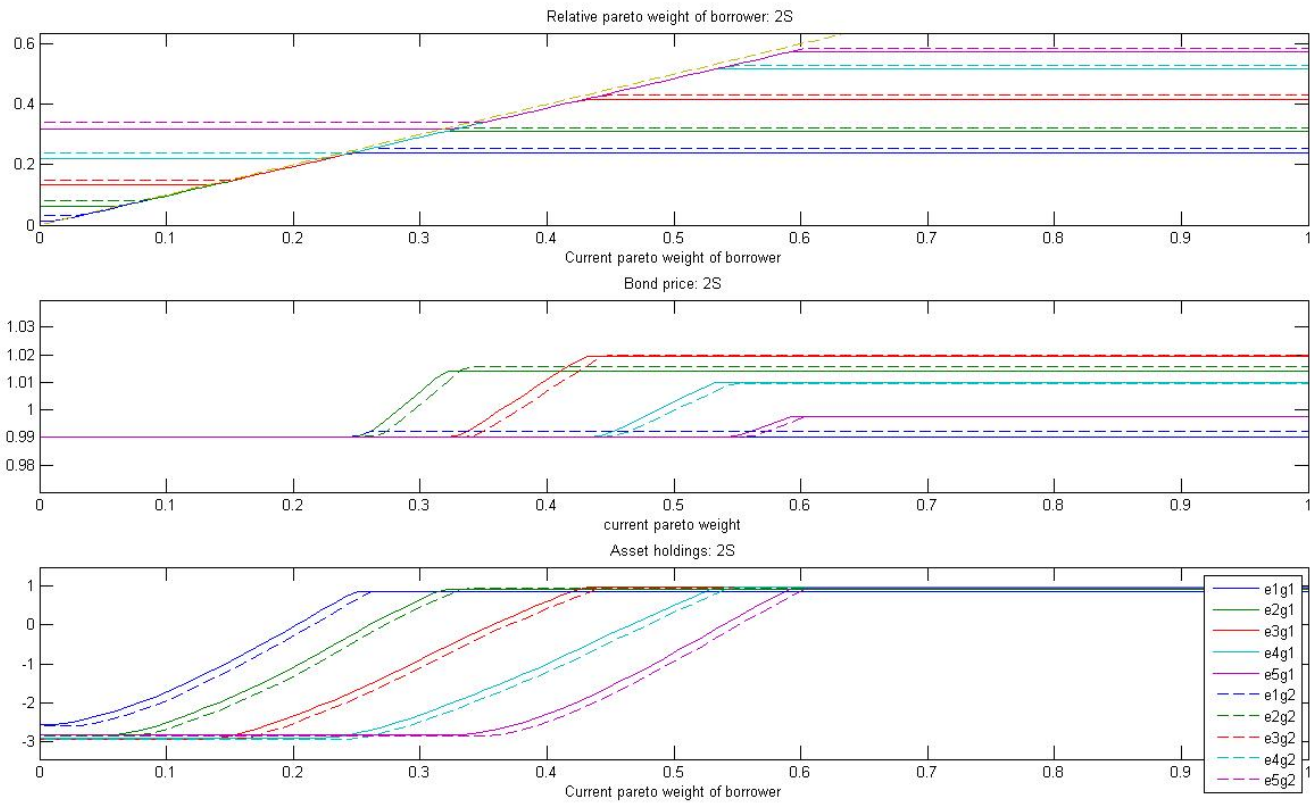




- e1g1
- e2g1
- e3g1
- e4g1
- e5g1
- e1g2
- e2g2
- e3g2
- e4g2
- e5g2









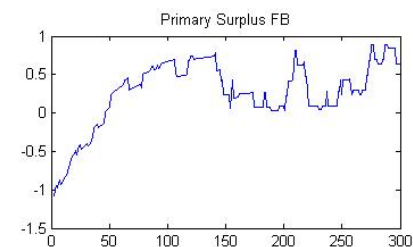
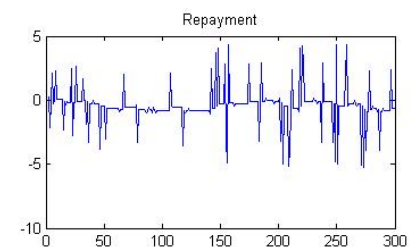
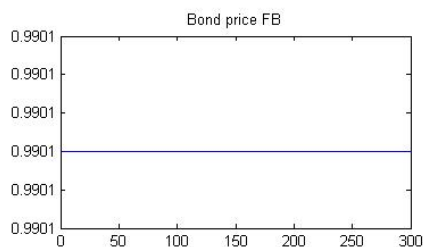
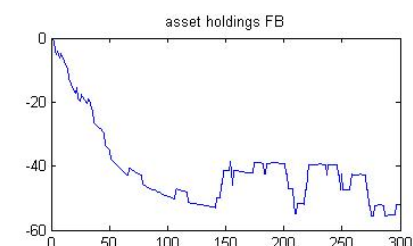
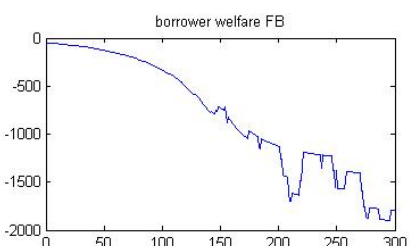
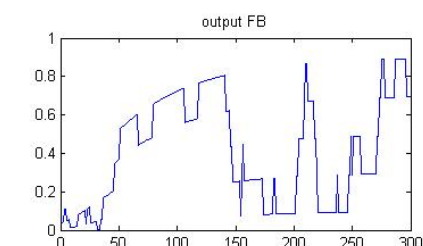
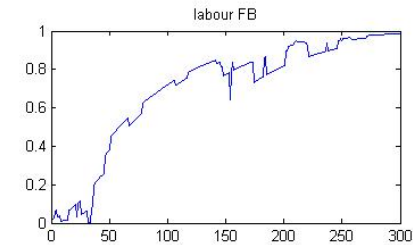
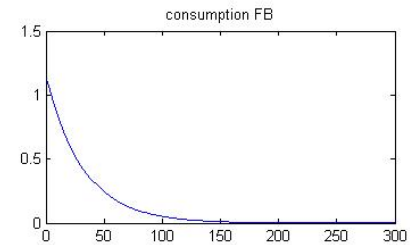
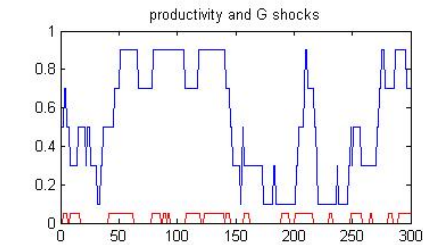
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**Contrasting *debt contracts* and *FSF contracts*:**  
**PATHS**

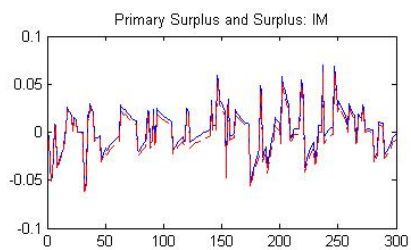
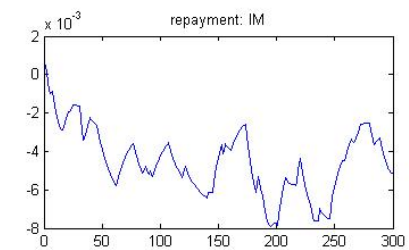
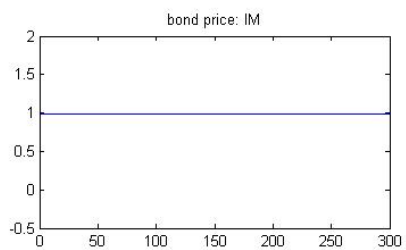
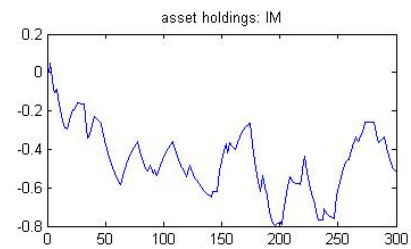
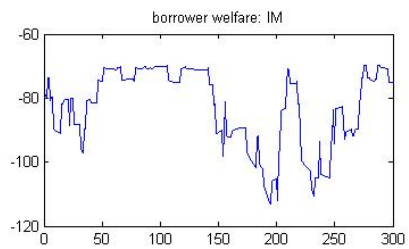
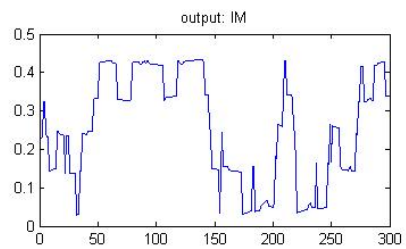
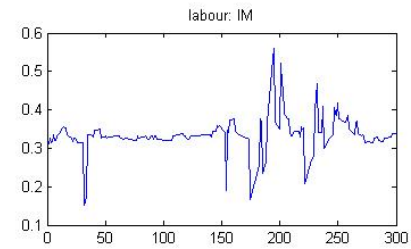
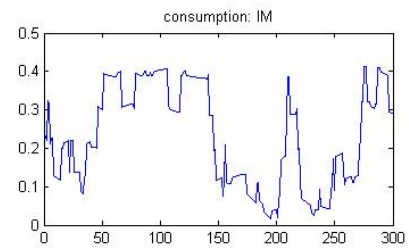
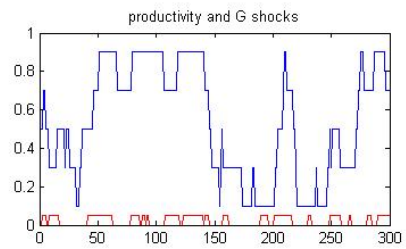
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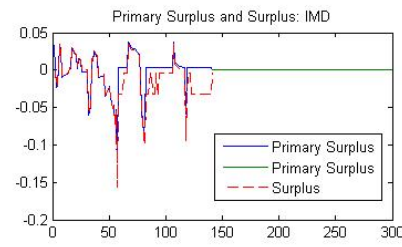
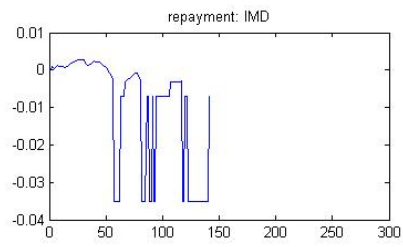
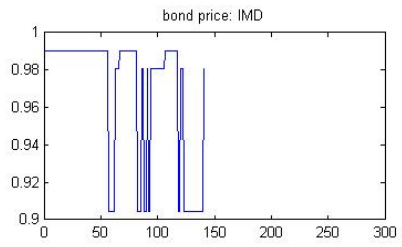
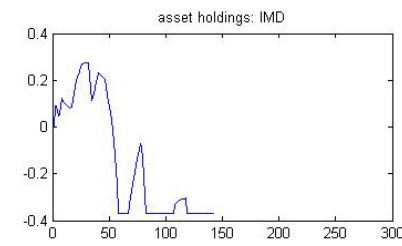
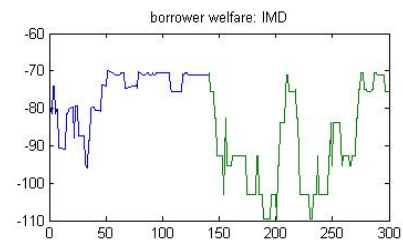
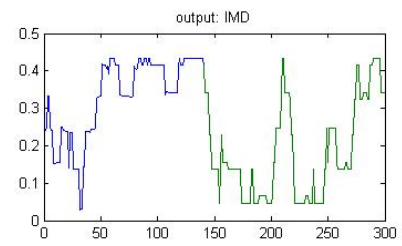
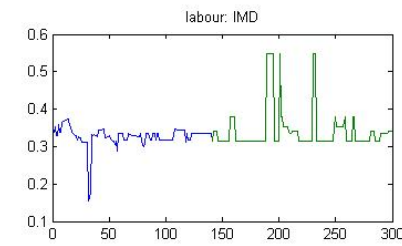
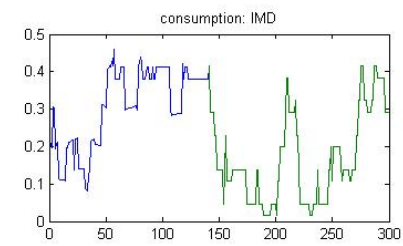
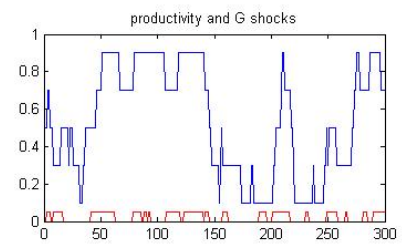


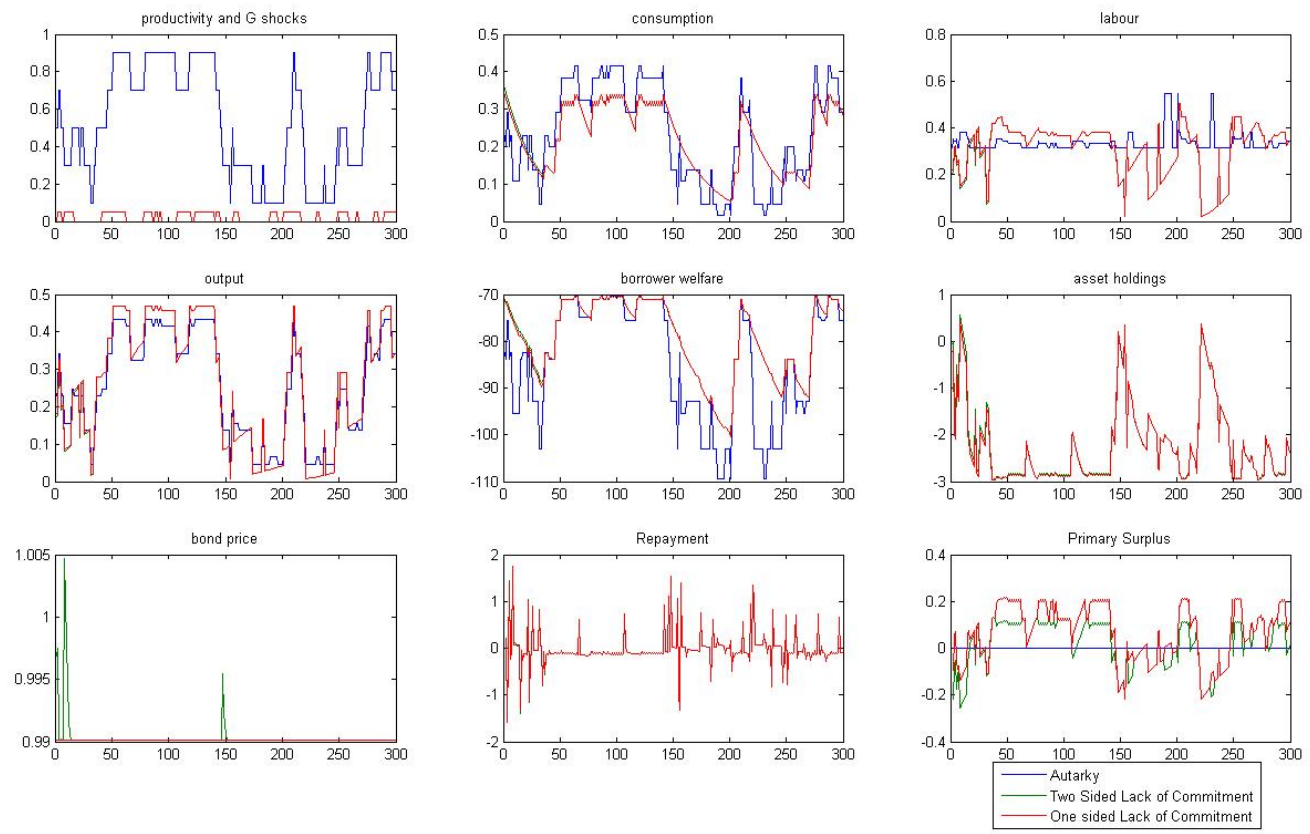


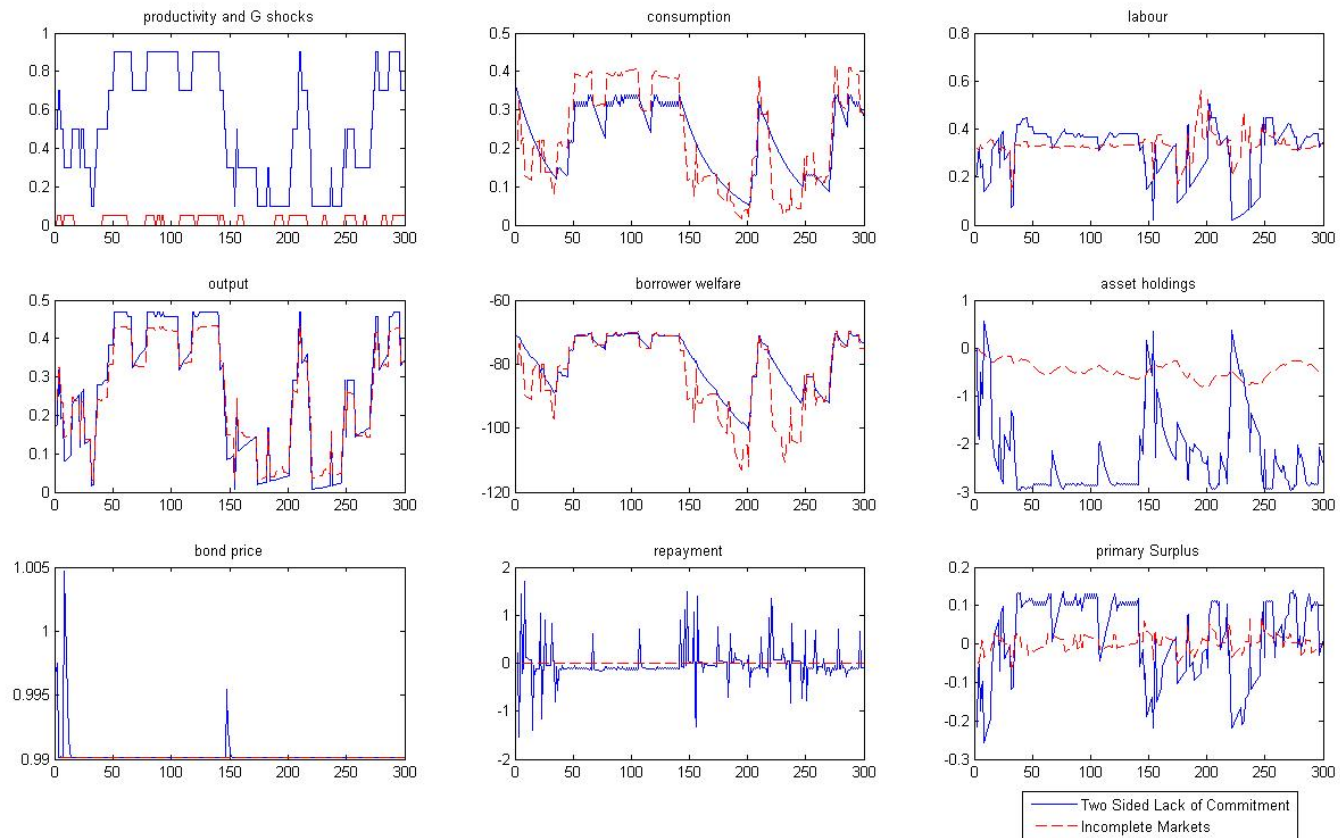
— First best

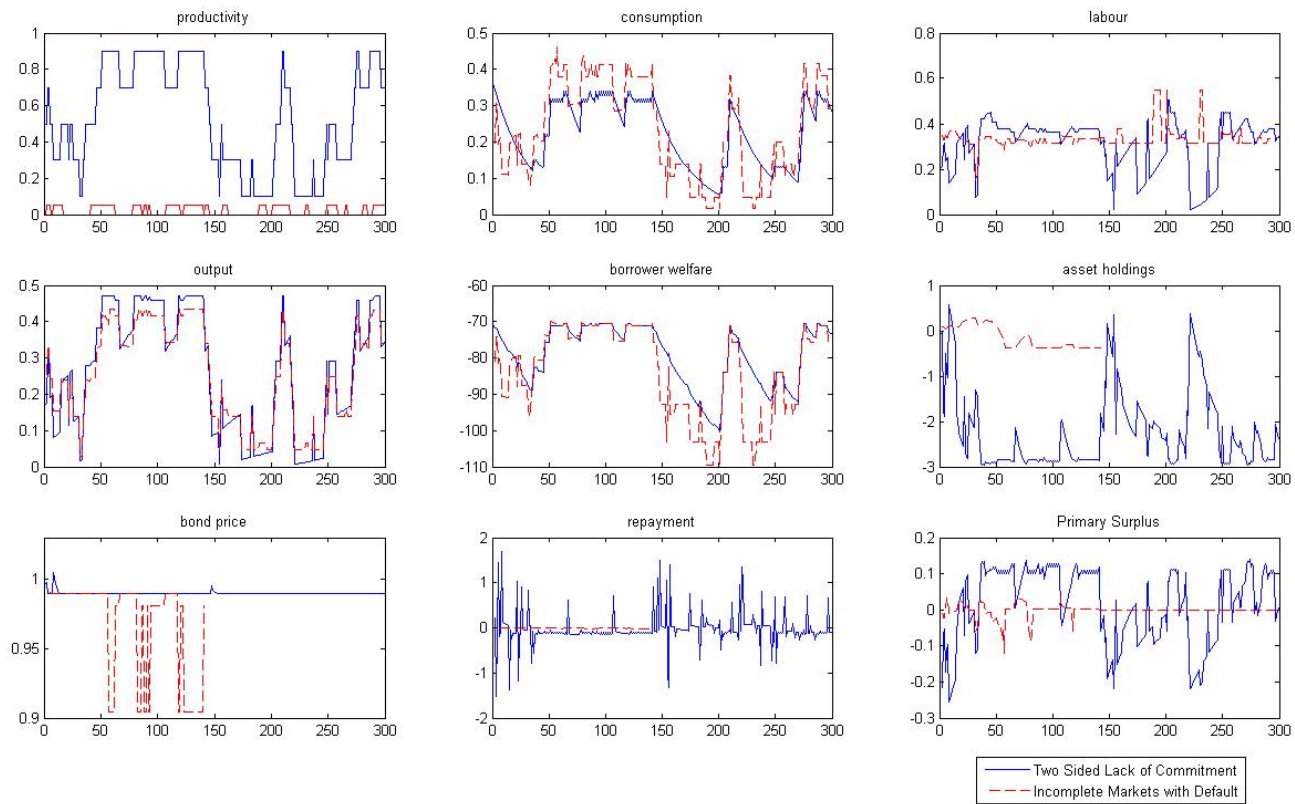


— Primary Surplus  
- - Surplus









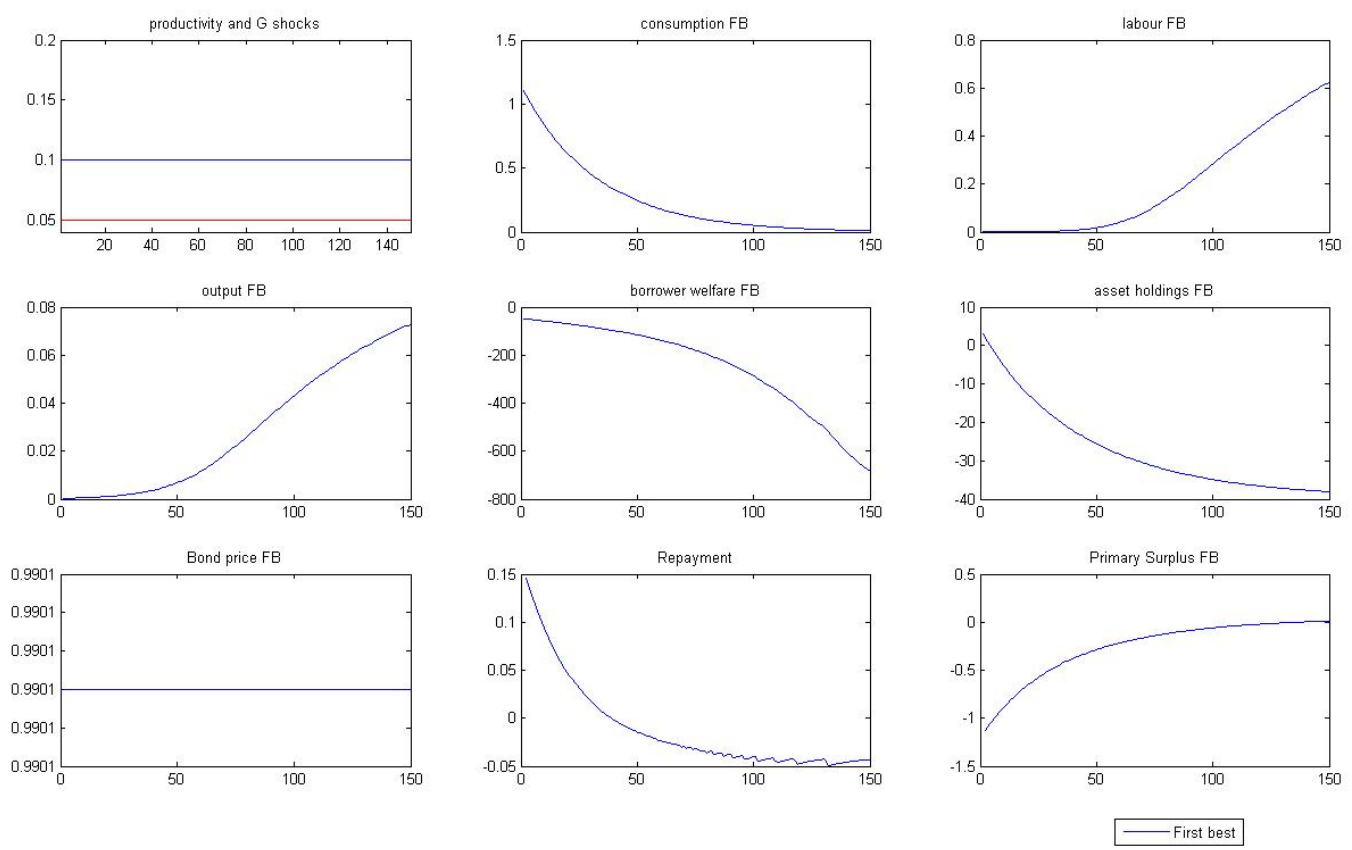
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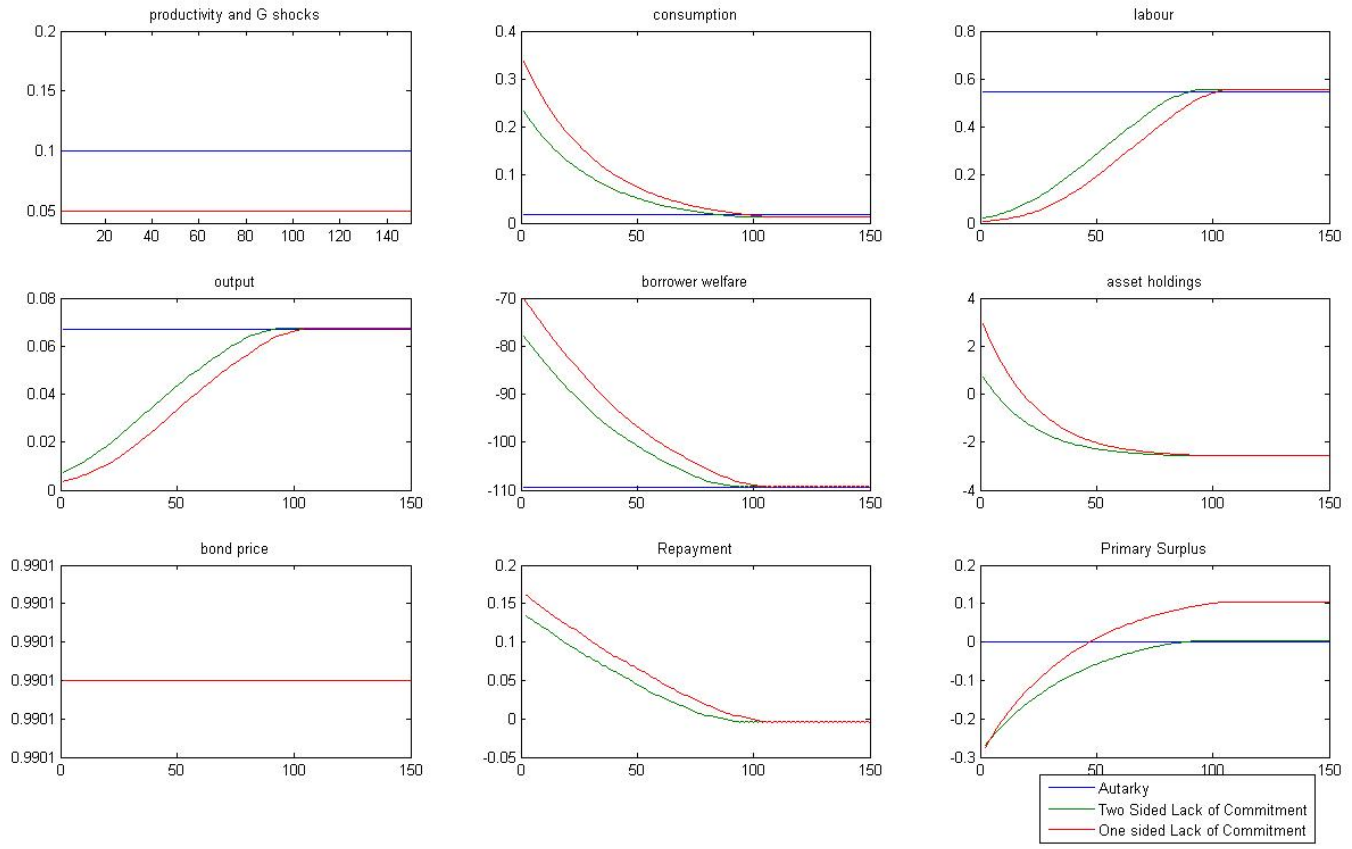
**Contrasting *debt contracts* and *FSF contracts*:  
PERSISTENT (-) SHOCK**

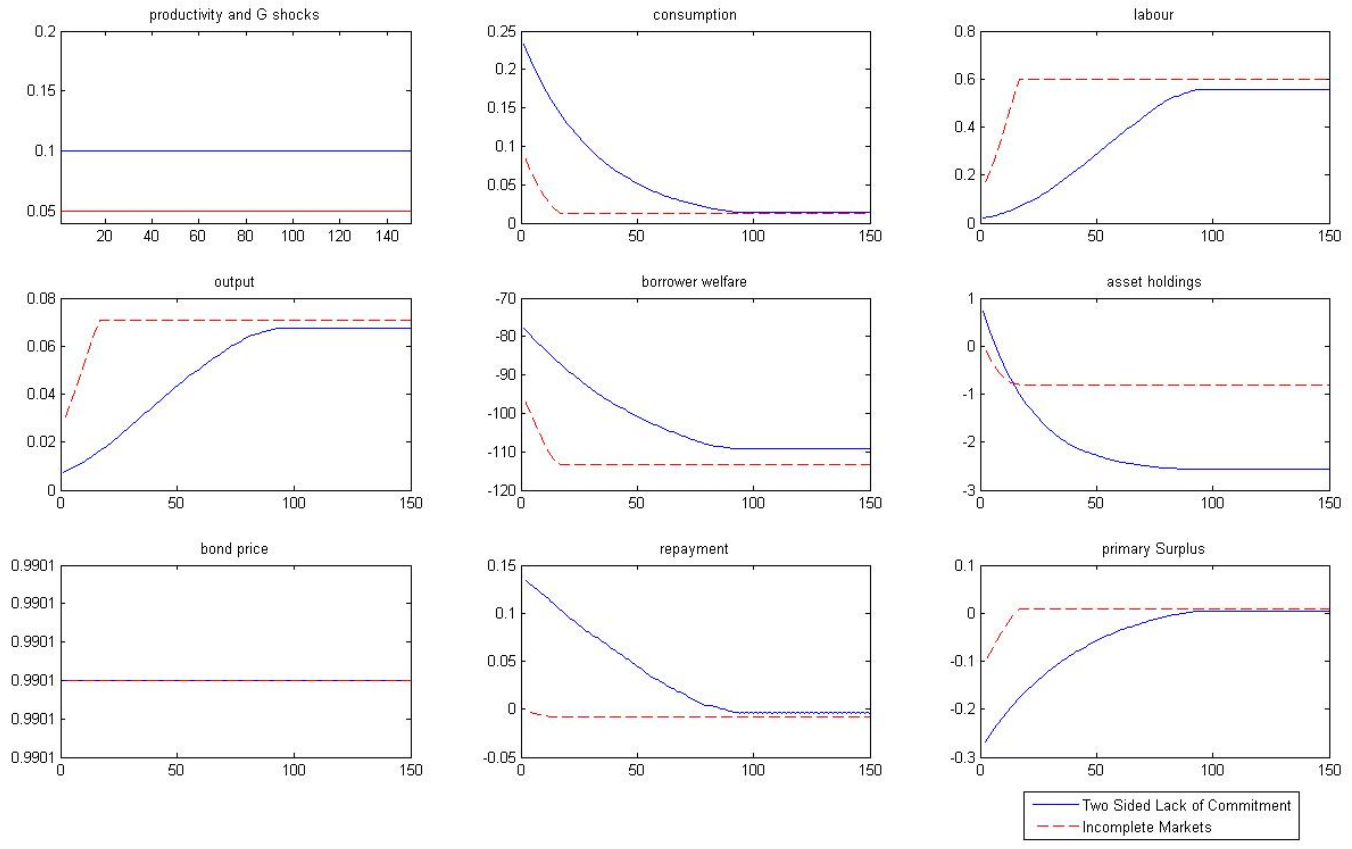
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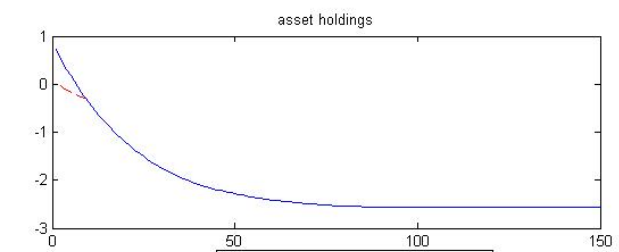
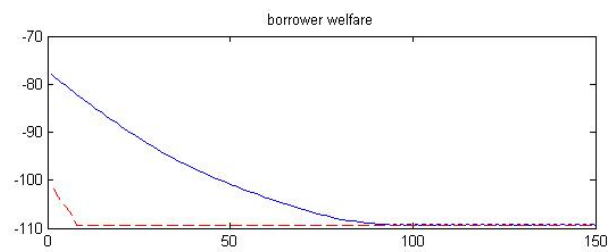
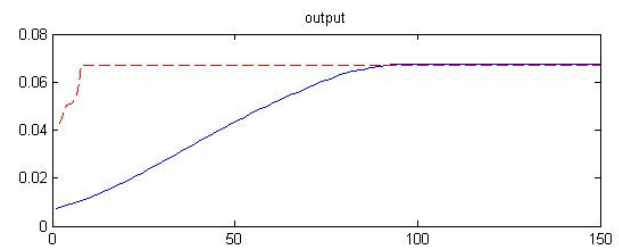
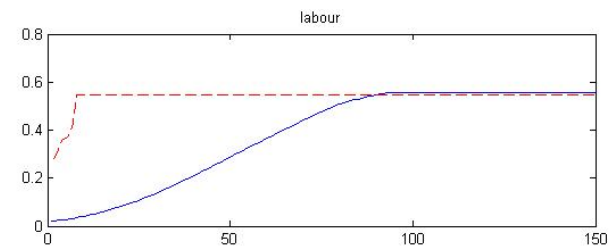
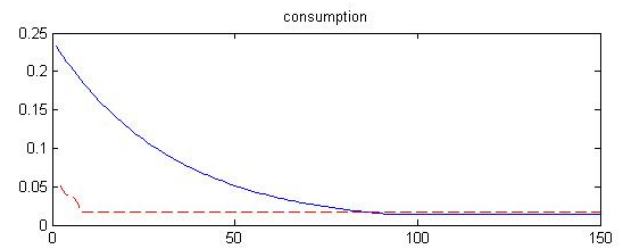
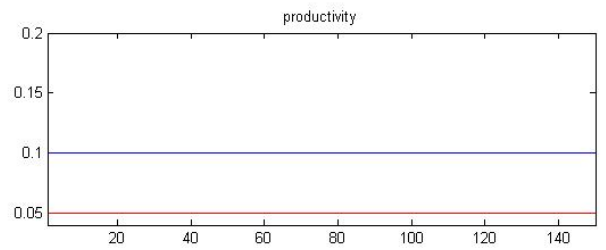












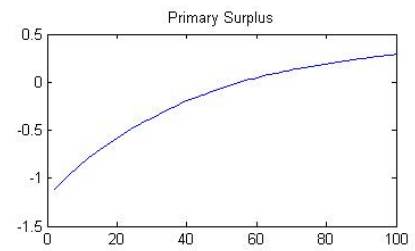
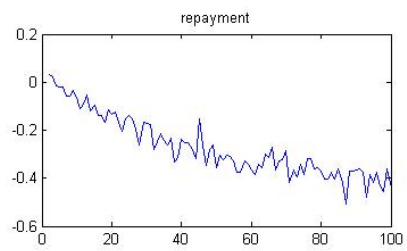
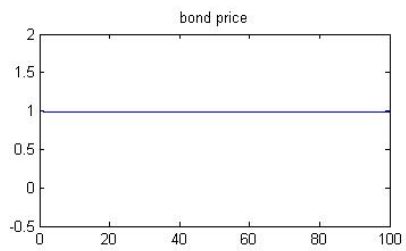
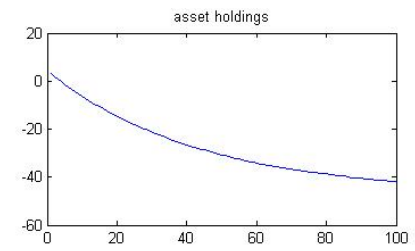
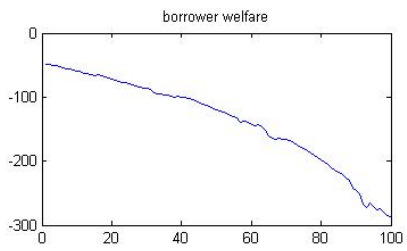
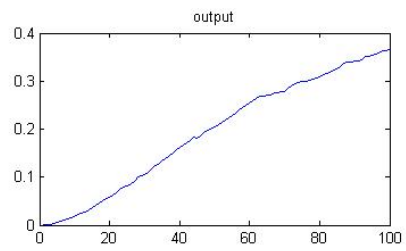
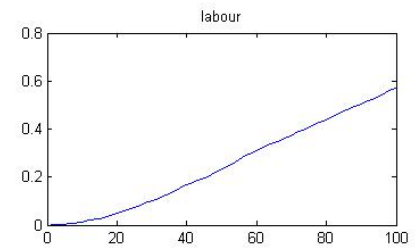
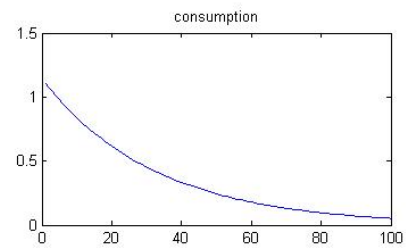
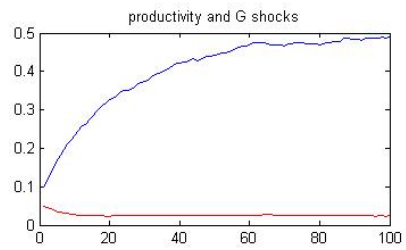
— Two Sided Lack of Commitment  
- - Incomplete Markets with Default

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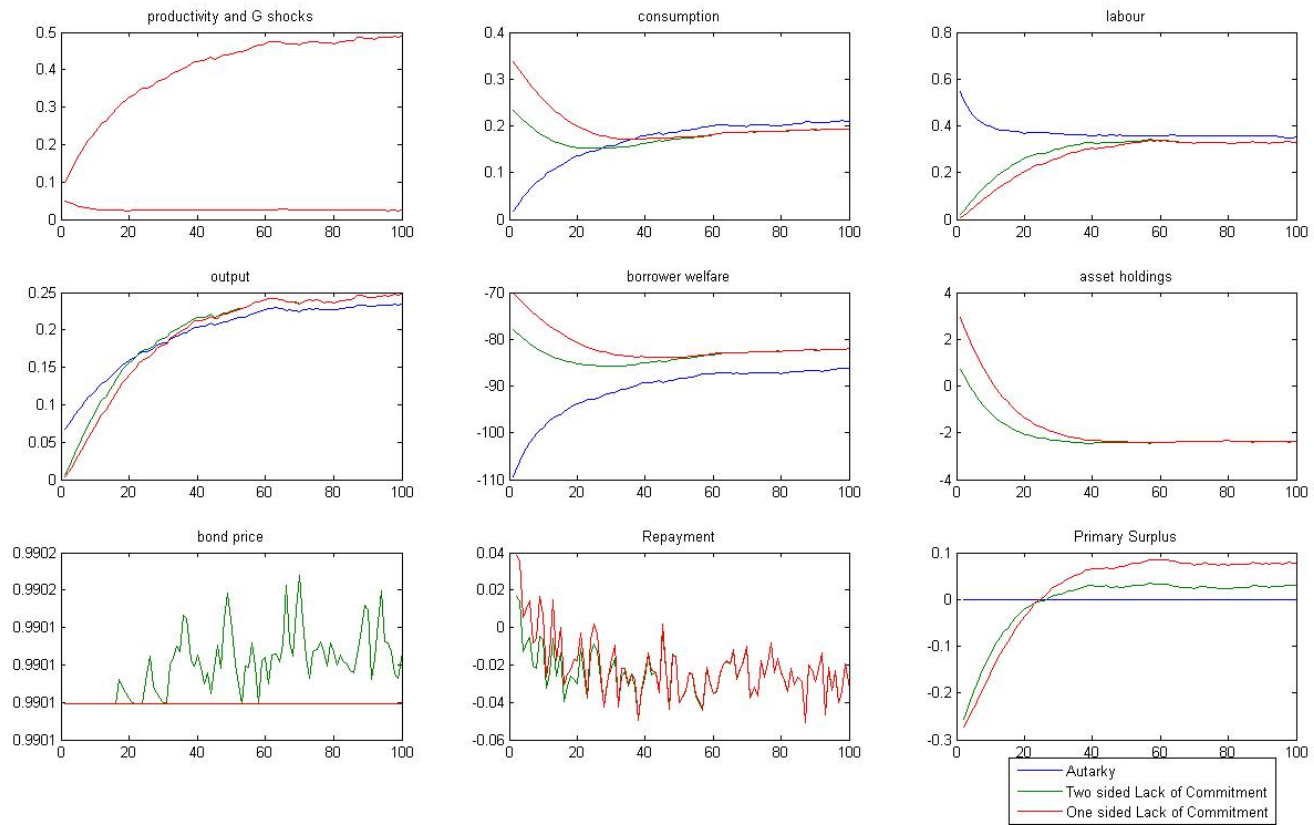
**Contrasting *debt contracts* and *FSF contracts*:  
REACTION TO (-) SHOCK (impulse responses)**

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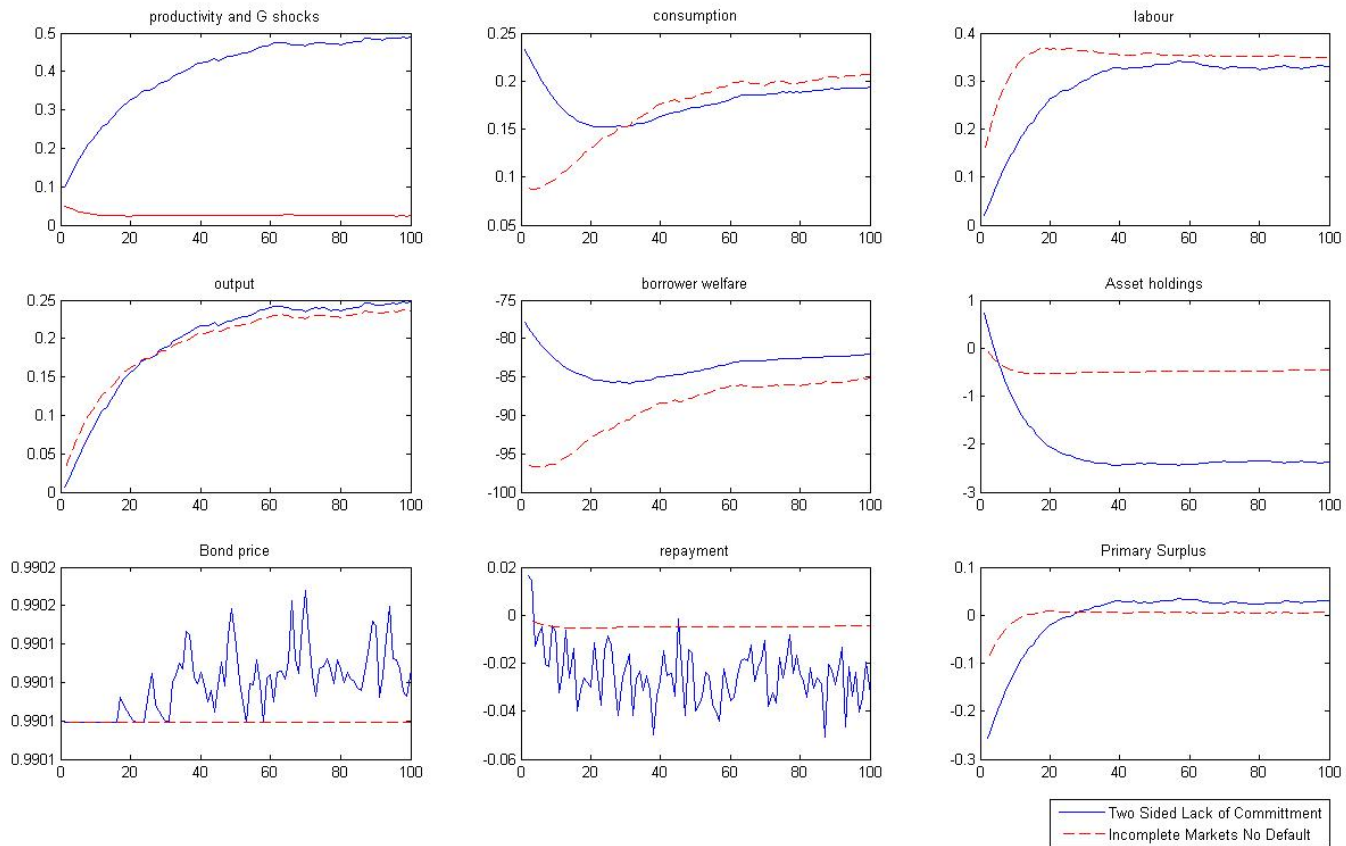


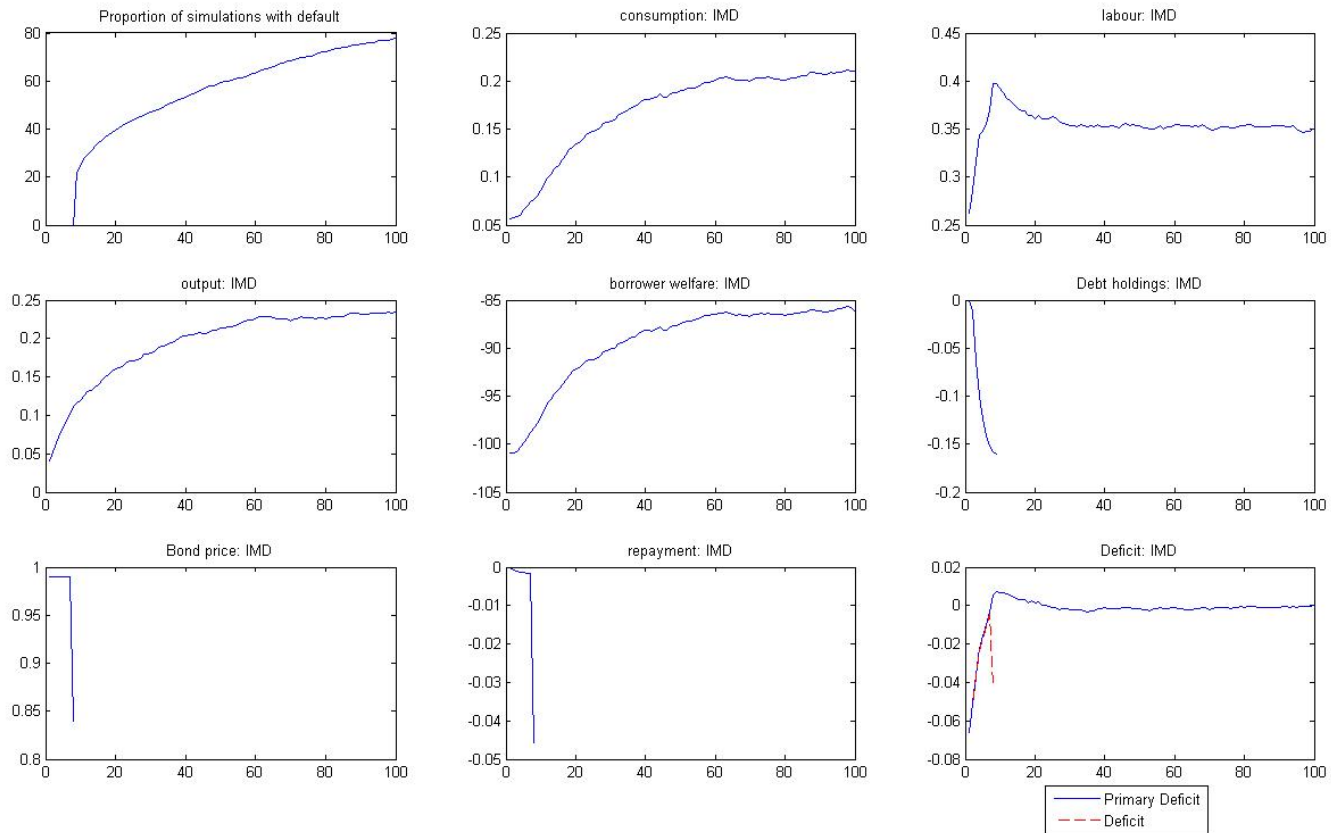


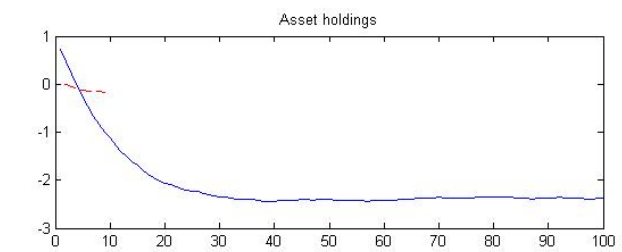
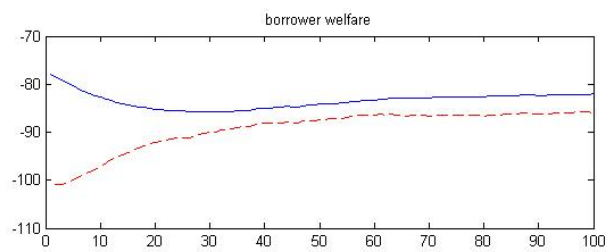
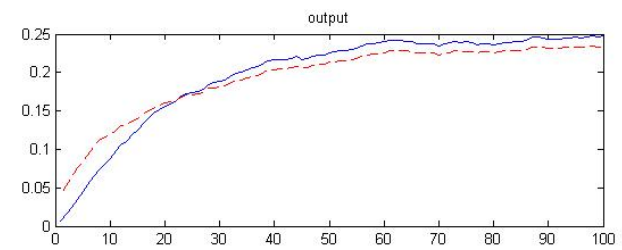
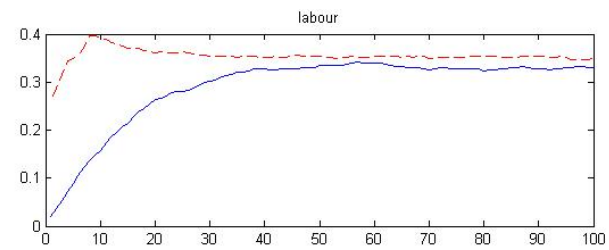
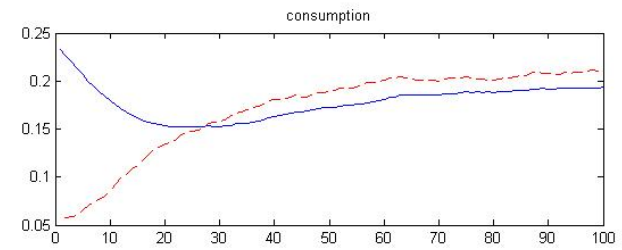
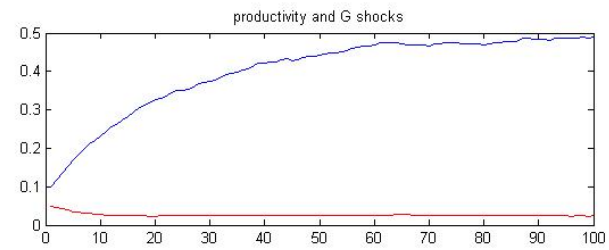
— First best











— Two Sided Lack of Commitment  
- - - Incomplete Markets Default

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## Contrasting *debt contracts* and *FSF contracts*: SUMMARY

- Efficiency, **FB**, calls for consumption decay (impatience) & smoothing, and labour responding to productivity. **1S** and **2S** achieve these to the extent that *limited enforcement constraints* allow them (e.g. no decay).
  - **IM** and **IMD** much less; in particular, when borrowers are close to their borrowing/default constraints.
  - With *FSF contracts*, if participation constraints are very low, borrowers may need to work more when productivity is low.
  - *FSF contracts* are able to exploit more (implicit) asset trading possibilities (e.g. more borrowing with **2S** than with **IM** or **IMD** )
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## Contrasting *debt contracts* and *FSF contracts*: SUMMARY

- Persistent crisis and bad shocks exacerbate the differences between:
    - *debt contracts* and *FSF contracts*,
    - **IM** and **IMD**,
    - **1S** and **2S**.
  - With the same underlying shocks, **recessions** are likely to be more severe with *incomplete markets*.
  - With the same underlying shocks, there may be frequent episodes of **positive spreads** in **IMD**, but few – and harmless – **negative spreads** with **2S**.
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**Contrasting *debt contracts* and *FSF contracts*:  
WELFARE**

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## ***Debt contracts vs. FSF contracts: WELFARE***

A simple measure,  $\chi$ , of *consumption equivalence*. *FSF with two-sided limited commitment vs. incomplete markets with and without default*

Taking advantage of the decomposition of the welfare functions

$$V_c^{bj} = \log(c_j) + \beta EV_c^{bj'} = E_0 \sum_{t=0}^{\infty} \beta^t \log(c_{j,t})$$

$$V_n^{bj} = \gamma \frac{(1-n)^{1-\sigma}}{1-\sigma} + \beta EV_n^{bj'}$$

where  $j = f, i$  for *FSF* and *incomplete markets*, respectively.  
Total welfare is then equal to

$$V^{bj} = V_c^{bj} + V_n^{bj}$$

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## Debt contracts vs. FSF contracts: WELFARE

$$\begin{aligned}V^{bf} &= E_0 \sum_{t=0}^{\infty} \beta^t \log((1 + \chi)c_t^i) + V_n^{bi} = \\&= \frac{\log(1 + \chi)}{1 - \beta} + E_0 \sum_{t=0}^{\infty} \beta^t \log(c_t^i) + V_n^{bi} = \\&= \frac{\log(1 + \chi)}{1 - \beta} + V_c^{bi} + V_n^{bi} \\&= \frac{\log(1 + \chi)}{1 - \beta} + V^{bi} \\&\rightarrow (1 + \chi) = \exp((V^{bf} - V^{bi})(1 - \beta))\end{aligned}$$

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## *Debt contracts vs. FSF contracts: WELFARE*

The welfare gains of a *FSF contract* can be very substantial!

	Average $\chi$	First Period $\chi$
Path Inc no def	0.174	0.378
Path Inc def	0.219	0.447
Pers Crisis Inc no def	0.594	1.060
Pers Crisis Inc def	0.414	1.513
Resp Shk Inc no def	0.317	1.060
Resp Shk Inc def	0.341	1.512

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## Conclusions

- This is preliminary work, but it is already very telling...
  - Even accounting for limited redistribution (2S) a *FSF* can substantially improve efficiency, with respect to debt financing.
  - Dynamic mechanism design provides a theoretical basis for *FSF* design.
  - Furthermore, costly default events may be prevented or mitigated, even if the economy is subject to the same shocks.
  - Similarly, the recession following a negative shock is substantially less severe with a *FSF*.
-

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## Conclusions

- While we have extensively borrowed from the existing theory, our analysis helps to better understand how different lending and borrowing mechanism work and compare.
  - For example, how positive and negative spreads can be associated with **IMD** and, **2S**, respectively.
  - In the end, the application revalues the theory...
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## Conclusions

- Yet, there is still work ahead:
  - To better calibrate the model to the Eurozone, or other economies.
  - To analyze the capacity of the *FSF* for absorbing existing debts (we always initialize asset holdings to zero).
  - Mostly, to account for *moral hazard*; e.g. changing  $G$  for  $G(e)$ ,  $G'(e) < 0$ , where  $e$  is costly, unverifiable, effort.
-



There is no future for the EMU, it will involve too much redistribution!

Using dynamic mechanism design, there should be a future for the EMU!



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**Thanks!**

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