# Understanding Employment Persistence* 

## Mike Elsby

University of Edinburgh

Ryan Michaels
University of Rochester

# David Ratner 

Federal Reserve Board

## [Preliminary and incomplete]

## CIGS Conference, Tokyo, May 2014

## Macroeconomic employment inertia

Employment is a lagging indicator (Okun).

## Question

What are the microeconomic origins of persistent aggregate employment dynamics?

Microeconomic employment inertia Inaction punctured by bursts of adjustment.

Are these linked?


Distribution of employment growth, QCEW 1992-2013

## Canonical approach

- Specify a model of lumpy adjustment costs.
- Match moments of the microdata.
- Draw out aggregate implications.
- Answer can depend on structure of model, moments matched etc.


## Our approach / Contributions / Roadmap

1. Diagnostic.

- Straightforward assessment of aggregate implications of popular class of theories; no estimation required.

2. Empirical application.

- Rich U.S. microdata on establishment employment dynamics cast doubt on role of canonical models.

3. Novel micro fact.

- Suggests the importance of replacement hiring.

4. Replacement hiring may matter for macro dynamics.

- Vacancy chains as an amplification mechanism.


## I. AGGREGATION

## Aggregation

The density of employment across firms $h(n)$ evolves according to:

$$
\begin{aligned}
\Delta h(n) & =\operatorname{Inflow}(n) \\
& -\operatorname{Outflow}(n)
\end{aligned}
$$

## Aggregation

The density of employment across firms $h(n)$ evolves according to:

$$
\begin{aligned}
\Delta h(n) & =\operatorname{Inflow}(n) \\
& -\operatorname{Outflow}(n)
\end{aligned}
$$

## Two themes

1. Adj. costs leave clear imprint on these flows.
2. We can measure these flows in microdata.

## Leading example: fixed costs

The density of employment across firms $h(n)$ evolves according to:

$$
\begin{aligned}
\Delta h(n) & =\operatorname{Pr}(\text { adjust to } n) h^{*}(n) \\
& -\operatorname{Outflow}(n) \prod_{\substack{\text { Density } \\
\text { implied fall } \\
\text { firms adjust }}}
\end{aligned}
$$

## Leading example: fixed costs

The density of employment across firms $h(n)$ evolves according to:

$$
\begin{aligned}
\Delta h(n) & =\operatorname{Pr}(\text { adjust to } n) h^{*}(n) \\
& -\operatorname{Pr}(\text { adjust from } n) h_{-1}(n)
\end{aligned}
$$

## Leading example: fixed costs

The density of employment across firms $h(n)$ evolves according to:

$$
\begin{aligned}
\Delta h(n) & =\operatorname{Pr}(\text { adjust to } n) h^{*}(n) \\
& -\operatorname{Pr}(\text { adjust from } n) h_{-1}(n)
\end{aligned}
$$



An $S s$ labor demand policy.

$\operatorname{Pr}($ adjust from $m)=1-H^{*}[U(m)]+H^{*}[L(m)]$

## Leading example: fixed costs

The density of employment across firms $h(n)$ evolves according to:

$$
\begin{aligned}
\Delta h(n) & =\operatorname{Pr}(\text { adjust to } n) h^{*}(n) \\
& -\operatorname{Pr}(\text { adjust from } n) h_{-1}(n)
\end{aligned}
$$



## Leading example: fixed costs

The density of employment across firms $h(n)$ evolves according to:

$$
\begin{aligned}
\Delta h(n) & =\operatorname{Pr}(\text { adjust to } n) h^{*}(n) \\
& -\operatorname{Pr}(\text { adjust from } n) h_{-1}(n)
\end{aligned}
$$

## Leading example: fixed costs

The density of employment across firms $h(n)$ evolves according to:

$$
\begin{aligned}
\Delta h(n) & =\operatorname{Pr}(\text { adjust to } n) h^{*}(n) \\
& -\operatorname{Pr}(\text { adjust from } n) h_{-1}(n)
\end{aligned}
$$



## Leading example: fixed costs

The density of employment across firms $h(n)$ evolves according to:

$$
\Delta h(n)=-\phi(n)\left[h_{-1}(n)-\hat{h}(n)\right]
$$

$\hat{h}(n)$ is a flow steady state that sets $\Delta h(n)=0$ :

$$
\hat{h}(n)=\frac{\tau(n)}{\phi(n)} h^{*}(n)
$$

## Leading example: fixed costs

The density of employment across firms $h(n)$ evolves according to:

$$
\Delta h(n)=-\phi(n)\left[h_{-1}(n)-\hat{h}(n)\right]
$$

$\hat{h}(n)$ is a flow steady state that sets $\Delta h(n)=0$ :

$$
\hat{h}(n)=\frac{\tau(n)}{\phi(n)} h^{*}(n)
$$

Claim:
This is useful

## II. A DIAGNOSTIC

## Flow steady state as a diagnostic

 Aggregate employment implied by $\hat{h}(n)$ informs path of frictionless aggregate employment:$$
\hat{h}(n)=\frac{\tau(n)}{\phi(n)} h^{*}(n)
$$

## Flow steady state as a diagnostic

 Aggregate employment implied by $\hat{h}(n)$ informs path of frictionless aggregate employment:$$
\widehat{N}=\int n \hat{h}(n) d n=\int n \frac{\tau(n)}{\phi(n)} h^{*}(n) d n
$$

## Flow steady state as a diagnostic

 Aggregate employment implied by $\hat{h}(n)$ informs path of frictionless aggregate employment:$$
\widehat{N}=\int n \hat{h}(n) d n=\mathbb{E}_{h^{*}}\left[n \cdot \frac{\tau(n)}{\phi(n)}\right]
$$

## Flow steady state as a diagnostic

 Aggregate employment implied by $\hat{h}(n)$ informs path of frictionless aggregate employment:$$
\begin{gathered}
\widehat{N}=\int n \hat{h}(n) d n=\mathbb{E}_{h^{*}}\left[n \cdot \frac{\tau(n)}{\phi(n)}\right] \\
=N^{*}+\operatorname{cov}^{*}\left(n, \frac{\tau(n)}{\phi(n)}\right)
\end{gathered}
$$

## Intuition I. $\widehat{N}$ as a bound for $\boldsymbol{N}^{*}$

$$
\widehat{N}=N^{*}+\operatorname{cov}^{*}\left(n, \frac{\tau(n)}{\phi(n)}\right)
$$

E.g. positive aggregate shock $\Rightarrow$

$$
N^{*} \uparrow \quad \text { and } \quad \operatorname{cov}^{*}\left(n, \frac{\tau(n)}{\phi(n)}\right) \uparrow
$$

More likely to adjust to vs. from higher $n$ s.

## Intuition I. $\widehat{N}$ as a bound for $\boldsymbol{N}^{*}$

$$
\widehat{N}=N^{*}+\operatorname{cov}^{*}\left(n, \frac{\tau(n)}{\phi(n)}\right)
$$

E.g. negative aggregate shock $\Rightarrow$

$$
N^{*} \downarrow \quad \text { and } \quad \operatorname{cov}^{*}\left(n, \frac{\tau(n)}{\phi(n)}\right) \downarrow
$$

Less likely to adjust to vs. from higher $n \mathrm{~s}$.

## Intuition II. Jump dynamics of $\widehat{N}$

$$
\widehat{N}=N^{*}+\operatorname{cov}^{*}\left(n, \frac{\tau(n)}{\phi(n)}\right)
$$

- $\tau(n)$ and $\phi(n)$ determined by policy function.
- Policy function forward looking $\Rightarrow$ jump.
- $\widehat{N}$ will inherit jump dynamics.
- We think this logic generalizes to kinked costs.


## Some quantitative examples

1. Pure fixed adjustment cost.

- To see daylight b/w series, consider "large" $C$.
$-\operatorname{Pr}($ inaction $)=0.65$ per quarter. [Data suggest 0.5.]

2. Fixed and kinked adjustment costs.

- Fix inaction rate and vary size of kinked cost.
$-c / w \in\{0.08,0.16\}$. [Bloom (2009) finds 0.08.]
- All are for fixed aggregate state (i.e. wages).


Pure fixed adjustment cost, $\operatorname{Pr}($ inaction $)=0.65$


Fixed and small kinked costs, $\operatorname{Pr}($ inaction $)=0.65$


Fixed and small kinked costs, $\operatorname{Pr}($ inaction $)=0.8$


Fixed and large kinked costs, $\operatorname{Pr}($ inaction $)=0.65$


Fixed and large kinked costs, $\operatorname{Pr}($ inaction $)=0.8$

## III. EMPIRICAL APPLICATION

## Empirical approach

Aggregation result has clear empirical content: We can measure much of the law of motion:

$\Rightarrow$ Can estimate $\hat{h}(n)=\frac{\Delta h(n)}{\operatorname{Pr}(\text { (adjust from } n)}+h_{-1}(n)$.

## Data

- Quarterly Census of Employment and Wages.
- Census of all Ul-covered employment
$-\approx 98 \%$ of U.S. employment.
- Establishment microdata onsite at BLS.
- Excludes MA, NH, NY, WI, FL, IL, MS, OR, WY, PA.
- Restrict analysis to continuing, private estabs. [I.e. drop births and deaths.]
- Broad coverage $\Rightarrow$ natural establishment panel.

Log aggregate employment


Log aggregate employment


## Actual vs. steady-state log aggregate employment, QCEW 1992-2013

Log aggregate employment


Log aggregate employment


## Actual vs. steady-state log aggregate employment, QCEW 1992-2013

Data


Model (large kinked cost)


## IV. SOME NEW FACTS

## Back to the data: $\mathbf{3}$ facts

1. Inaction over net changes.

- Even though quit rate is $6 \%$ per quarter (JOLTS).

2. Slow decay of inaction by frequency.

- Much slower than exponential decay.

3. Inaction correlated w/ job-to-job transitions.

- At both aggregate and industry levels.


Distribution of employment growth, QCEW 1992-2013

Share of establishments


Distribution of employment growth, QCEW 1992-2013


$$
\operatorname{Pr}\left(n_{t}=n_{t+\tau}\right), \text { QCEW average over 1992-2013 }
$$

## Slow decay of inaction

- Not captured in any of the baseline models.
- Decay in model is essentially exponential.

| Frequency <br> $\tau$ in <br> quarters | Data | Pure fixed <br> cost | $\operatorname{Pr}\left(n_{t}=n_{t+\tau}\right)$ <br> + small <br> kink | + larger <br> kink |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 0.53 | 0.64 | 0.67 | 0.65 |
| 2 | 0.46 | 0.41 | 0.45 | 0.43 |
| 3 | 0.43 | 0.27 | 0.30 | 0.28 |
| 4 | 0.41 | 0.18 | 0.2 | 0.18 |

## Slow decay of inaction

- Not an artefact of seasonality.
- Decay is slow between as well as within years.
- Similar decay in high vs. low seasonal industries.

| Frequency $\tau$ in | $\operatorname{Pr}\left(n_{t}=n_{t+\tau}\right) / \operatorname{Pr}\left(n_{t}=n_{t+1}\right)$ |  |
| :---: | :---: | :---: |
| quarters | High seasonal | Low seasonal |
| 1 | 1 | 1 |
| 2 | 0.82 | 0.84 |
| 3 | 0.74 | 0.75 |
| 4 | 0.70 | 0.69 |



Aggregate inaction and job-to-job transitions, QCEW and CPS

Inaction rate (quarterly)


Industry-level inaction and job-to-job transitions, QCEW and CPS

## V. REPLACEMENT HIRING

## Lessons from the data

- Firms appear to have reference levels of employment to which they return routinely.
- A lot of adjustment seen in the data is driven by high-frequency returns to reference level.
- Negative correlation w/ $E$-to- $E^{\prime}$ rate suggests role of replacement hiring.
- Could this matter?


## A prototype model of replacement hiring

$\Pi\left(n_{-1}, k_{-1}, x\right) \equiv$
$\max \{p x F(n)-w n \quad$ Revenue - costs
$n$

$$
\begin{array}{ll}
-c^{+}\left[n-(1-\delta) n_{-1}\right]^{+} & \text {Gross hiring } \\
-C \mathbb{1}_{\Delta k \neq 0} & \text { Capacity adj. } \\
-c^{-}[k-n]^{-} & \text {Slack capacity } \\
+ \text { Forward value }\} &
\end{array}
$$

s.t. $\Delta k=\left[n-k_{-1}\right]^{+}-\left[n-k_{-1}\right] \mathbb{1}_{n<(1-\delta) n_{-1}}$

## A prototype model of replacement hiring

$\Pi\left(n_{-1}, k_{-1}, x\right) \equiv$
$\max \{p x F(n)-w n$
$n$

$$
\begin{aligned}
& -c^{+}\left[n-(1-\delta) n_{-1}\right]^{+} \\
& -C \mathbb{1}_{\Delta k \neq 0} \\
& -c^{-}[k-n]^{-} \\
& + \text {Forward value }\}
\end{aligned}
$$

## Revenue - costs

Gross hiring
Capacity adj.
Slack capacity
s.t. $\Delta k=\left[n-k_{-1}\right]^{+}-\left[n-k_{-1}\right] \mathbb{1}_{n<(1-\delta) n_{-1}}$

## A prototype model of replacement hiring

$\Pi\left(n_{-1}, k_{-1}, x\right) \equiv$ Exogenous (for now) $\max \{p x F(n)-w n \quad$ Revenue - costs $n$

$$
\begin{aligned}
& -c^{+}\left[n-(1-\delta) n_{-1}\right]^{+} \\
& -C \mathbb{1}_{\Delta k \neq 0} \\
& -c^{-}[k-n]^{-} \\
& + \text {Forward value }\}
\end{aligned}
$$

Gross hiring
Capacity adj.
Slack capacity
s.t. $\Delta k=\left[n-k_{-1}\right]^{+}-\left[n-k_{-1}\right] \mathbb{1}_{n<(1-\delta) n_{-1}}$

Saves a control variable


A prototype model of replacement hiring


## Model does better on slow decay of inaction

Frequency $\tau$ in $\quad \operatorname{Pr}\left(n_{t}=n_{t+\tau}\right) / \operatorname{Pr}\left(n_{t}=n_{t+1}\right)$
quarters
Model
Data

| 1 | 1 | 1 |
| :---: | :---: | :---: |
| 2 | 0.86 | 0.87 |
| 3 | 0.76 | 0.81 |
| 4 | 0.69 | 0.77 |

## Why replacement hiring might matter

Search models $\Rightarrow$ gross per-worker hiring cost:

$$
c^{+}=\frac{\text { vacancy cost }}{\text { vacancy filling rate }}=\frac{\gamma}{q(V)}
$$

1. More $V$ s reduce $q$, hiring cost $c^{+}$rises. $\rightarrow$ Negative feedback.

## Why replacement hiring might matter

Search models $\Rightarrow$ gross per-worker hiring cost:

$$
c^{+}=\frac{\text { vacancy cost }}{\text { vacancy filling rate }}=\frac{\gamma}{q(V)}
$$

1. More $V$ s reduce $q$, hiring cost $c^{+}$rises. $\rightarrow$ Negative feedback.
2. More $V$ s raise $\delta$, post further $V$ s to replace. $\rightarrow$ Positive feedback: Vacancy chains...

## A prototype model of replacement hiring

$\Pi\left(n_{-1}, k_{-1}, x\right) \equiv$
$\max \{p x F(n)-w n \quad$ Revenue - costs
$n$

$$
\begin{array}{ll}
-c^{+}\left[n-(1-\delta) n_{-1}\right]^{+} & \text {Gross hiring } \\
-C \mathbb{1}_{\Delta k \neq 0} & \text { Capacity adj. } \\
-c^{-}[k-n]^{-} & \text {Slack capacity } \\
+ \text { Forward value }\} &
\end{array}
$$

s.t. $\Delta k=\left[n-k_{-1}\right]^{+}-\left[n-k_{-1}\right] \mathbb{1}_{n<(1-\delta) n_{-1}}$

## A prototype model of replacement hiring

$\Pi\left(n_{-1}, k_{-1}, x ; V\right) \equiv$
$\max \{p x F(n)-w n \quad$ Revenue - costs

$$
\begin{array}{ll}
-\frac{\gamma}{q(V)}\left[n-(1-\delta(V)) n_{-1}\right]^{+} & \text {Gross hiring } \\
-C \mathbb{1}_{\Delta k \neq 0} & \text { Capacity adj. } \\
-c^{-}[k-n]^{-} & \text {Slack capacity } \\
+ \text { Forward value }\} &
\end{array}
$$

s.t. $\Delta k=\left[n-k_{-1}\right]^{+}-\left[n-k_{-1}\right] \mathbb{1}_{n<(1-\delta) n_{-1}}$

## A prototype model of replacement hiring

$\Pi\left(n_{-1}, k_{-1}, x ; V\right) \equiv$ $\max \{p x F(n)-w n$ $n$

$$
\begin{array}{ll}
-\frac{\gamma}{q(V)}\left[n-(1-\delta(V)) n_{-1}\right]^{+} & \text {Gross hiring } \\
-C \mathbb{1}_{\Delta k \neq 0} & \text { Capacity adj. } \\
-c^{-}[k-n]^{-} & \text {Slack capacity } \\
+ \text { Forward value }\} & \text {...and slack is costly. }
\end{array}
$$

## Revenue - costs

s.t. $\Delta k=\left[n-k_{-1}\right]^{+}-\left[n-k_{-1}\right] \mathbb{1}_{n<(1-\delta) n_{-1}}$


Without replacement hiring $\left(c^{-}=0\right)$


With replacement hiring $\left(c^{-}>0\right)$


Amplification: Vacancy chains

## A conjecture

- Absent vacancy chains, replacement hiring model just an exotic adj. cost model.
$\rightarrow$ Suspect $\widehat{N}$ diagnostic would remain jump.
- But, vacancy chains add another layer to the aggregate dynamics.
$\rightarrow$ Frictions spillover and multiply across firms.
$\rightarrow$ If process of poaching takes time $\Rightarrow$ persistence.
- Much more work to do: chiefly wage setting!


## Summary of contributions

- Toward a diagnostic for the aggregate effects of popular class of adjustment frictions.
- Empirical implementation suggests models unable to explain employment persistence.
- Microdata instead suggest pervasive replacement hiring.
- Prototype model suggests aggregate dynamics could look very different in this case.


## Extra slides







## Canonical model

Idiosyncratic


Fixed adj. cost

## Lemma (Gertler and Leahy, 2008)

The optimal labor demand policy approximately takes the Ss form,

$$
n=\left\{\begin{array}{ccc}
n^{*} & \text { if } & n^{*} \notin\left[L\left(n_{-1}\right), U\left(n_{-1}\right)\right] \\
n_{-1} & \text { if } & n^{*} \in\left[L\left(n_{-1}\right), U\left(n_{-1}\right)\right]
\end{array}\right.
$$

where

- $n^{*}(x, p)$ coincides with frictionless analogue;
- $L\left(n_{-1}\right)<U\left(n_{-1}\right)$ are time-invariant.


## Intuition

- $\underline{n}^{*}(x, p)$ coincides with frictionless analogue
- Envelope Theorem: Prob. of inaction $=O(\sqrt{C})$.
- Optimality: Return to inaction $\in[0, C]=O(C)$.
- Probability $\times$ Return $=O\left(C^{3 / 2}\right) \approx 0$.
- $L\left(n_{-1}\right)<U\left(n_{-1}\right)$ are time-invariant
$-n^{*}$ sufficient statistic for shocks to $\{x, p, w\}$.
$-L\left(n_{-1}\right)<U\left(n_{-1}\right)$ reflect curvature of $F(n)$.


## Proof of bounding result

Myopia is approximately optimal (Gertler/Leahy 2008):
$\mathbb{E}\left[\Pi^{\prime}\right]=\mathbb{E}\left[\Pi_{\text {adjust }}^{\prime}-C\right]$
$+\operatorname{Pr}($ inaction $) \mathbb{E}\left[\Pi_{\text {inaction }}^{\prime}-\Pi_{\text {adjust }}^{\prime}+C\right]$.


## Some quantitative examples

1. Pure fixed adjustment cost.

$$
\max \{p x F(n)-w n
$$ $n$

$$
\begin{aligned}
& -C \mathbb{1}_{\Delta n \neq 0} \\
& + \text { Forward value }\}
\end{aligned}
$$

Revenue - costs
Fixed adj. cost

Adjustment policy takes Ss form as above.

## Some quantitative examples

2. Fixed and kinked adjustment costs
[à la Cooper et al. (2007) and Bloom (2009)].
$\max \{p x F(n)-w n$
$n$

Revenue - costs
Fixed adj. cost
Kinked adj. cost +Forward value\}

Kinked costs attenuate size of adjustments.


Allowing for kinked adjustment costs

## Aggregation with kinked costs

The density of employment across firms $h(n)$ evolves according to:

$$
\Delta h(n)=-\phi(n)\left[h_{-1}(n)-\hat{h}(n)\right]
$$

$\hat{h}(n)$ is a flow steady state that sets $\Delta h(n)=0$ :

$$
\hat{h}(n)=\frac{\operatorname{Pr}(\text { down to } n) h_{l}^{*}(n)+\operatorname{Pr}(\text { up to } n) h_{u}^{*}(n)}{\operatorname{Pr}(\text { from } n)}
$$

## Aggregation with kinked costs

The density of employment across firms $h(n)$ evolves according to:

$$
\Delta h(n)=-\phi(n)\left[h_{-1}(n)-\hat{h}(n)\right]
$$

$\hat{h}(n)$ is a flow steady state that sets $\Delta h(n)=0$ :

$$
\hat{h}(n)=\frac{\left(1-H_{-1}\left[L^{-1} l(n)\right]\right) h_{l}^{*}(n)+H_{-1}\left[U^{-1} u(n)\right] h_{u}^{*}(n)}{1-H^{*}[U(n)]+H^{*}[L(n)]}
$$



Pure fixed adjustment cost, $\operatorname{Pr}($ inaction $)=0.5$


Pure fixed adjustment cost, $\operatorname{Pr}($ inaction $)=0.8$

## Dynamic correlations with output

Two steps:

1. Regress (HP-filtered) output on 4 lags of itself; residual is the "output innovation".
2. Regress (HP-filtered) employment on 4 lags of itself as well as the current and first, second, and thirdlagged values of the output innovation.

- Figure reports response to $1 \%$ output innovation.
- Do same for actual and flow steady-state employment in both data and model-generated time series.

